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6 SPARK Tutorial 121

6.1 Writing SPARK Programs                                           121
6.1.1 Checking SPARK Legality Rules                                  123
6.1.2 Checking SPARK Initialization Policy                           126
6.1.3 Writing Functional Contracts                                  128
We begin with a very simple guide aimed at getting new users up and running with the SPARK tools. A small SPARK example program will be used for illustration.

Note: The online version of this User’s Guide applies to the latest development version of the SPARK toolset. If you’re using an official release, some of the described features may not apply. Refer to the version of the SPARK 2014 User’s Guide shipping with your release, available through Help → SPARK in GNAT Studio and GNATbench IDEs, or under share/doc/spark in your SPARK installation.

As a prerequisite, it is assumed that the SPARK tools have already been installed. As a minimum you should install:

- SPARK Pro, SPARK Discovery or SPARK Community
- GNAT Studio or the GNATbench plug-in of Eclipse

SPARK Pro is the most complete toolset for SPARK. SPARK Discovery is a reduced toolset that still allows to perform all analyses presented in this User’s Guide, but is less powerful than SPARK Pro. Compared to SPARK Pro, SPARK Discovery:

- only comes with one automatic prover instead of three
- does not include the static analyzer CodePeer
- does not generate counterexamples for failed proofs
- has limited proof support for programs using modular arithmetic or floating-point arithmetic
- comes without a lemma library for more difficult proofs

SPARK Community is a version packaged for free software developers, hobbyists, and students, which retains most of the capabilities of SPARK Pro. SPARK Community does not include the static analyzer CodePeer.

Note that GNAT Studio is not strictly required for SPARK as all the commands can be invoked from the command line, or from Eclipse using the GNATbench plug-in, but the instructions in this section assume that GNAT Studio is being used. If you are a supported user, you can get more information on how to install the tools in “AdaCore Installation Procedures” under the “Download” tab in GNAT Tracker, or by contacting AdaCore for further advice.

The key tools that we will use in this example are GNATprove and GNAT Studio. To begin with, launch GNAT Studio with a new default project and check that the SPARK menu is present in the menu bar.

Note: For SPARK 2005 users, this menu will appear under the name SPARK 2014, to avoid any confusion with the existing SPARK menu for SPARK 2005 toolset.

Now open a new file in GNAT Studio and type the following short program into it. Save this file as diff.adb.
procedure Diff (X, Y : in Natural; Z : out Natural) with
  SPARK_Mode,
  Depends => (Z => (X, Y))
is
begin
  Z := X - X;
end Diff;

The program is intended to calculate the difference between X and Y and store the result in Z. This is reflected in the aspect Depends which states that the output value of Z depends on the input values of X and Y, but, as you may have noticed, there is a bug in the code. Note the use of aspect SPARK_Mode to identify this as SPARK code to be analysed with the SPARK tools. To analyze this program, select SPARK → Examine File from the menu in GNAT Studio. GNATprove executes in flow analysis mode and reports:

```
diff.adb:1:20: warning: unused variable "Y"
diff.adb:1:36: info: initialization of "Z" proved
diff.adb:3:03: medium: missing dependency "null => Y"
diff.adb:3:24: medium: incorrect dependency "Z => Y"
```

These warnings are informing us that there is a discrepancy between the program’s contract (which says that the value of Z is obtained from the values of X and Y) and its implementation (in which the value of Z is derived only from the value of X, and Y is unused). In this case the contract is correct and the code is wrong, so fix the code by changing the assignment statement to Z := X - Y; and re-run the analysis. This time it should report no warnings or errors.

Having established that the program is free from flow errors, now let’s run the tools in proof mode to check for run-time errors. Select SPARK → Prove File from the menu in GNAT Studio, and click on Execute in the resulting dialog box. GNATprove now attempts to show, using formal verification, that the program is free from run-time errors. But it finds a problem and highlights the assignment statement in red, reporting:

```
diff2.adb:1:37: info: initialization of "Z" proved
diff2.adb:3:03: info: flow dependencies proved
diff2.adb:6:11: info: overflow check proved
diff2.adb:6:11: medium: range check might fail (e.g. when X = 0 and Y = 1) [possible explanation: subprogram at line 1 should mention X and Y in a precondition]
```

This means that the tools are unable to show that the result of subtracting one Natural number from another will be within the range of the type Natural, which is hopefully not too surprising! There are various ways in which this could be addressed depending on what the requirements are for this subprogram, but for now let’s change the type of parameter Z from Natural to Integer. If the analysis is re-run with this change in place then GNATprove will report no errors or warnings. All checks are proved so we can be confident that no exceptions will be raised by the execution of this code.

This short example was intended to give a flavor of the types of analysis that can be performed with the SPARK tools. A more in-depth example is presented later in SPARK Tutorial.
SPARK 2014 is a programming language and a set of verification tools designed to meet the needs of high-assurance software development. SPARK 2014 is based on Ada 2012, both subsetting the language to remove features that defy verification, but also extending the system of contracts and aspects to support modular, formal verification.

The new aspects support abstraction and refinement and facilitate deep static analysis to be performed including flow analysis and formal verification of an implementation against a specification.

SPARK 2014 is a much larger and more flexible language than its predecessor SPARK 2005. The language can be configured to suit a number of application domains and standards, from server-class high-assurance systems (such as air-traffic management applications), to embedded, hard real-time, critical systems (such as avionic systems complying with DO-178C Level A).

A major feature of SPARK 2014 is the support for a mixture of proof and other verification methods such as testing, which facilitates in particular the use of unit proof in place of unit testing; an approach now formalized in DO-178C and the DO-333 formal methods supplement. Certain units may be formally proven and other units validated through testing.

SPARK 2014 is supported by various tools in the GNAT toolsuite:

- the GNAT compiler
- the GNAT Studio integrated development environment
- the GNATTest tool for unit testing harness generation
- the GNATprove tool for formal program verification

In the rest of this document, we’ll simply say SPARK to refer to SPARK 2014.

The remainder of this document is structured as follows:

- **Installation of GNATprove** goes through the installation steps on different platforms.
- **Identifying SPARK Code** describes the various means to identify the part of the program in SPARK that should be analyzed.
- **Overview of SPARK Language** provides an overview of the SPARK language.
- **SPARK Tutorial** gives an introduction to writing, testing and proving SPARK programs.
- **Formal Verification with GNATprove** describes the use of the GNATprove formal verification tool.
- **Applying SPARK in Practice** lists the main objectives and project scenarios for using SPARK.
CHAPTER THREE

INSTALLATION OF GNATPROVE

In general, you will need to install a recent version of GNAT toolchain (that supports Ada 2012 syntax) to compile SPARK programs. You will need to install one toolchain for each platform that you target, for example one toolchain for native compilation on your machine and one toolchain for cross compilation to an embedded platform.

For analyzing SPARK programs, we recommend to first install GNAT Studio and then install GNATprove under the same location. Alternatively, you can install the GNATbench plug-in for Eclipse instead of GNAT Studio, using the Eclipse installation mechanism. The same version of GNAT Studio or GNATbench can support both native and cross compilations, as well as SPARK analysis.

If you choose to install GNATprove in a different location, you should also modify the environment variables GPR_PROJECT_PATH (if you installed GNAT). On Windows, edit the value of GPR_PROJECT_PATH under the Environnement Variables panel, and add to it the value of <GNAT install dir>/lib/gnat and <GNAT install dir>/share/gpr (so that SPARK can find library projects installed with GNAT) and <SPARK install dir>/lib/gnat (so that GNAT can find the SPARK lemma library project installed with SPARK, for details see Manual Proof Using SPARK Lemma Library). On Linux/Mac with Bourne shell, use:

```bash
export GPR_PROJECT_PATH=<GNAT install dir>/lib/gnat:<GNAT install dir>/share/gpr:
   ~<SPARK install dir>/lib/gnat:$GPR_PROJECT_PATH
```

or on Linux/Mac with C shell:

```bash
setenv GPR_PROJECT_PATH <GNAT install dir>/lib/gnat:<GNAT install dir>/share/gpr:
   ~<SPARK install dir>/lib/gnat:$GPR_PROJECT_PATH
```

See below for detailed installation instructions of GNAT Studio and GNATprove.

### 3.1 System Requirements

Formal verification is complex and time consuming, so GNATprove will benefit from all the speed (CPU) and memory (RAM) that can be made available. A minimum of 2 GB of RAM per core is recommended. More complex analyses will require more memory. A recommended configuration for running GNATprove on large systems is an x86-64 machine running Linux 64bits or Windows 64bits with at least 8 cores and 16 GB of RAM. Slower machines can be used to analyze small subsystems, but a minimum of 2.8GHz CPU and 2 GB of RAM is required.

In addition, if you want to use the integration of CodePeer static analysis in GNATprove (switch --codepeer=on) you will need approximately 1 GB of RAM per 10K SLOC of code. In other words, in order to analyze 300K SLOC of code with CodePeer, you will need a 64bits configuration with at least 30 GB of RAM. Note that these numbers will vary depending on the complexity of your code. If your code is very simple, you will need less memory. On the other hand if your code is very complex, then you will likely need more memory.
3.2 Installation under Windows

If not already done, first run the GNAT Studio installer by e.g. double clicking on `gnatstudio-<version>-i686-pc-mingw32.exe` and follow the instructions.

**Note:** If you’re using GNAT GPL instead of GNAT Pro, you should run instead the GNAT GPL installer, which installs GNAT Studio.

Then similarly run the GNATprove installer, by e.g. double clicking on `spark-<version>-x86-windows-bin.exe`.

You should have sufficient rights for installing the package (administrator or normal rights depending on whether it is installed for all users or a single user).

3.3 Installation under Linux/Mac

If not already done, you need to extract and install the GNAT Studio compressed tarball and then run the install, e.g.:

```
$ gzip -dc gnatstudio-<version>-<platform>-bin.tar.gz | tar xf -
$ cd gnatstudio-<version>-<platform>-bin
$ ./doinstall
```

Then follow the instructions displayed.

**Note:** If you’re using GNAT GPL instead of GNAT Pro, you should install instead the GNAT GPL package, which installs GNAT Studio.

Then do the same with the SPARK tarball, e.g.:

```
$ gzip -dc spark-<version>-<platform>-bin.tar.gz | tar xf -
$ cd spark-<version>-<platform>-bin
$ ./doinstall
```

Note that you need to have sufficient rights for installing the package at the chosen location (e.g. root rights for installing under `/opt/spark`).
IDENTIFYING SPARK CODE

In general a program can have some parts that are in SPARK (and follow all the rules in the SPARK Reference Manual), and some parts that are full Ada 2012. Pragma or aspect SPARK_Mode is used to identify which parts are in SPARK (by default programs are in full Ada).

This section contains a simple description of pragma and aspect SPARK_Mode. See Pragma SPARK_Mode for the complete description.

Note that GNATprove only analyzes parts of the code that are identified as being in SPARK using pragma or aspect SPARK_Mode.

4.1 Mixing SPARK Code and Ada Code

An Ada program unit or other construct is said to be “in SPARK” if it complies with the restrictions required to permit formal verification given in the SPARK Reference Manual. Conversely, an Ada program unit or other construct is “not in SPARK” if it does not meet these requirements, and so is not amenable to formal verification.

Within a single Ada unit, constructs which are “in” and “not in” SPARK may be mixed at a fine level in accordance with the following two general principles:

- SPARK code shall only reference SPARK declarations, but a SPARK declaration which requires a completion may have a non-SPARK completion.
- SPARK code may enclose non-SPARK code.
- non-SPARK code may enclose SPARK code only at library level. A subprogram body which is not in SPARK cannot contain SPARK code.

More specifically, non-SPARK completions of SPARK declarations are allowed for subprogram declarations, package declarations, task type declarations, protected type declarations, private type declarations, private extension declarations, and deferred constant declarations. [Strictly speaking, the private part of a package, a task type or a protected type is considered to be part of its completion for purposes of the above rules; this is described in more detail below].

When a non-SPARK completion is provided for a SPARK declaration, the user has an obligation to ensure that the non-SPARK completion is consistent (with respect to the semantics of SPARK) with its SPARK declaration. For example, SPARK requires that a function call has no side effects. If the body of a given function is in SPARK, then this rule is enforced via various language rules; otherwise, it is the responsibility of the user to ensure that the function body does not violate this rule. As with other such constructs (notably pragma Assume), failure to meet this obligation can invalidate any or all analysis (proofs and/or flow analysis) associated with the SPARK portion of a program. A non-SPARK completion meets this obligation if it is semantically equivalent (with respect to dynamic semantics) to some notional completion that could have been written in SPARK.

When a non-SPARK package declaration or body is included in a SPARK subprogram or package, the user has an obligation to ensure that the non-SPARK declaration is consistent (with respect to the semantics of SPARK) with
a hypothetical equivalent SPARK declaration. For example, SPARK requires that package elaboration code cannot modify variables defined outside of the package.

The SPARK semantics (specifically including flow analysis and proof) of a “mixed” program which meets the aforementioned requirement are well defined - they are the semantics of the equivalent 100% SPARK program. For the semantics of other “mixed” programs refer to the Ada Reference Manual.

In the case of a package, a task type, or a protected type, the specification/completion division described above is a simplification of the true situation. For instance, a package is divided into 4 sections, not just 2: its visible part, its private part, the declarations of its body, and the statement list of its body. For a given package and any number N in the range 0..4, the first N sections of the package might be in SPARK while the remainder is not.

For example, the following combinations may be typical:

- Package specification in SPARK. Package body not in SPARK.
- Visible part of package specification in SPARK. Private part and body not in SPARK.
- Package specification in SPARK. Package body almost entirely in SPARK, with a small number of subprogram bodies not in SPARK.
- Package specification in SPARK, with all subprogram bodies imported from another language.
- Package specification contains a mixture of declarations which are in SPARK and not in SPARK. The latter declarations are only visible and usable from client units which are not in SPARK.

Task types and protected types are similar to packages but only have 3 sections instead of 4. The statement list section of the body is missing.

Another typical use is to exempt part of a subprogram from analysis by isolating it in a local subprogram whose body is not in SPARK.

Such patterns are intended to allow for application of formal verification to a subset of a program, and the combination of formal verification with more traditional testing (see Applying SPARK in Practice).

4.2 Project File Setup

The project file is used to identify coarsely which parts of a program are in SPARK. To get more details on project file setup, see section Setting Up a Project File.

4.2.1 Setting the Default SPARK_Mode

There are two possible defaults:

1. No value of SPARK_Mode is specified as a configuration pragma. In that case, only the parts of the program explicitly marked with SPARK_Mode => On are in SPARK. This default is recommended if only a small number of units or subprograms are in SPARK.

2. A value of SPARK_Mode => On is specified as a configuration pragma. In that case, all the program should be in SPARK, except for those parts explicitly marked with SPARK_Mode => Off. This mode is recommended if most of the program is in SPARK.

Here is how to specify a value of SPARK_Mode => On as a configuration pragma:

```ada
project My_Project is
  package Builder is
    for Global_Configuration_Pragmas use "spark.adc";
  end Builder;
end My_Project;
```
where spark.adc is a configuration file containing at least the following line:

```plaintext
pragma SPARK_Mode (On);
```

### 4.2.2 Specifying Files To Analyze

By default, all files from a project are analyzed by GNATprove. It may be useful to restrict the set of files to analyze to speedup analysis if only a subset of the files contain SPARK code.

The set of files to analyze can be identified by specifying a different value of various project attributes in the mode used for formal verification:

- **Source_Dirs**: list of source directory names
- **Source_Files**: list of source file names
- **Source_List_File**: name of a file listing source file names

For example:

```plaintext
project My_Project is
    type Modes is ("Compile", "Analyze");
    Mode : Modes := External ("MODE", "Compile");
    case Mode is
        when "Compile" =>
            for Source_Dirs use (...);
        when "Analyze" =>
            for Source_Dirs use ("dir1", "dir2");
            for Source_Files use ("file1.ads", "file2.ads", "file1.adb", "file2.adb");
    end case;
end My_Project;
```

Then, GNATprove should be called by specifying the value of the MODE external variable as follows:

```plaintext
gnatprove -P my_project -XMODE=Analyze
```

### 4.2.3 Excluding Files From Analysis

When choosing a default value of SPARK_Mode => On, it may be needed to exclude some files from analysis (for example, because they contain non-SPARK code, or code that does not need to be formally analyzed).

The set of files to exclude can be identified by specifying a different value of various project attributes in the mode used for formal verification:

- **Excluded_Source_Dirs**: list of excluded source directory names
- **Excluded_Source_Files**: list of excluded source file names
- **Excluded_Source_List_File**: name of a file listing excluded source file names

For example:

```plaintext
project My_Project is
    package Builder is
        for Global_Configuration_Pragsmas use "spark.adc";
```
end Builder;

type Modes is ("Compile", "Analyze");
Mode : Modes := External ("MODE", "Compile");

case Mode is
  when "Compile" =>
    null;
  when "Analyze" =>
    for Excluded_Source_Files use ("file1.ads", "file1.adb", "file2.adb");
end case;
end My_Project;

Then, GNATprove should be called by specifying the value of the MODE external variable as follows:

gnatprove -P my_project -XMODE=Analyze

4.2.4 Using Multiple Projects

Sometimes, it is more convenient to analyze a subset of the source files with the default SPARK_Mode => On and the rest of the source files with no setting for SPARK_Mode. In that case, one can use two project files with different defaults, with each source file in one of the projects only. Files in one project can still refer to files in the other project by using a limited with clause between projects, as follows:

limited with "project_b"
project My_Project_A is
  package Compiler is
    for Local_Configuration_Pragmas use "spark.adc";
  end Compiler;
  for Source_Files use ("file1.ads", "file2.ads", "file1.adb", "file2.adb");
end My_Project_A;

limited with "project_a"
project My_Project_B is
end My_Project_B;

where spark.adc is a configuration file containing at least the following line:

pragma SPARK_Mode (On);

4.3 Using SPARK_Mode in Code

The pragma or aspect SPARK_Mode can be used in the code to identify precisely which parts of a program are in SPARK.

4.3.1 Basic Usage

The form of a pragma SPARK_Mode is as follows:
**pragma SPARK_Mode [ (On | Off) ]**

For example:

```
pragma SPARK_Mode (On);
package P is
```

The form of an aspect **SPARK_Mode** is as follows:

```
with SPARK_Mode => [ On | Off ]
```

For example:

```
package P with
  SPARK_Mode => On
is
```

A default argument of On is assumed for any **SPARK_Mode** pragma or aspect for which no argument is explicitly specified.

For example:

```
package P is
  pragma SPARK_Mode; -- On is implicit here
```

or

```
package P with
  SPARK_Mode -- On is implicit here
is
```

We say that a package or a subprogram is library-level if it is either top-level or defined in a library-level package. The **SPARK_Mode** pragma can be used in the following places in the code:

- as a configuration pragma at unit level (even before with-clauses) in particular for unit-level generic instantiations
- immediately within a library-level package spec
- immediately within a library-level package body
- immediately following the `private` keyword of a library-level package spec
- immediately following the `begin` keyword of a library-level package body
- immediately following a library-level subprogram spec
- immediately within a library-level subprogram body
- immediately within a library-level task spec
- immediately within a library-level task body
- immediately following the `private` keyword of a library-level task spec
- immediately within a library-level protected spec
- immediately within a library-level protected body
- immediately following the `private` keyword of a library-level protected spec

The **SPARK_Mode** aspect can be used in the following places in the code:
• on a library-level package spec or body
• on a library-level subprogram spec or body
• on a library-level task spec or body
• on a library-level protected spec or body

If a SPARK_Mode pragma or aspect is not specified for a subprogram, package, task or protected spec/body, then its value is inherited from the current mode that is active at the point where the declaration occurs.

Note that a generic package instance is considered to be declared at its instantiation point. For example, a generic package cannot be both marked SPARK_Mode and instantiated in a subprogram body.

### 4.3.2 Consistency Rules

The basic rule is that you cannot turn SPARK_Mode back On, once you have explicitly turned it Off. So the following rules apply:

If a subprogram spec has SPARK_Mode Off, then the body cannot have SPARK_Mode On.

For a package, we have four parts:

1. the package public declarations
2. the package private part
3. the body of the package
4. the elaboration code after begin

For a package, the rule is that if you explicitly turn SPARK_Mode Off for any part, then all the following parts cannot have SPARK_Mode On. Note that this may require repeating a pragma SPARK_Mode (Off) in the body. For example, if we have a configuration pragma SPARK_Mode (On) that turns the mode On by default everywhere, and one particular package spec has pragma SPARK_Mode (Off), then that pragma will need to be repeated in the package body.

Task types and protected types are handled similarly. If SPARK_Mode is set to Off on one part, it cannot be set to On on the following parts, among the three parts:

1. the spec
2. the private part
3. the body

There is an exception to this rule, when SPARK_Mode occurs in the code of a generic instantiated in code where SPARK_Mode is Off. In that case, occurrences of SPARK_Mode in the generic are ignored for this instance.

### 4.3.3 Examples of Use

#### Verifying Selected Subprograms

If only a few selected subprograms are in SPARK, then it makes sense to set no default for SPARK_Mode, and instead set SPARK_Mode => On directly on the subprograms of interest. For example:

```plaintext
package Selected_Subprograms is

    procedure Critical_Action with
    SPARK_Mode => On;
```
Note that, although the bodies of procedures Sub_Action and Non_Critical_Action are not analyzed, it is valid to call Sub_Action in the body of procedure Critical_Action, even without specifying SPARK_Mode => On on the spec of Sub_Action. Indeed, GNATprove checks in that case that the spec of Sub_Action is in SPARK.

Verifying Selected Units

If only a few selected units are in SPARK, then it makes sense to set no default for SPARK_Mode, and instead set SPARK_Mode => On directly on the units of interest. For example:
Note that procedure `Sub_Action` can be called inside SPARK code, because its spec is in SPARK, even though its body is marked `SPARK_Mode => Off`. On the contrary, procedure `Non_Critical_Action` whose spec is marked `SPARK_Mode => Off` cannot be called inside SPARK code.

```plaintext
package body Selected_Units with
  SPARK_Mode => On
is

  procedure Critical_Action is
    -- this procedure body is analyzed
    X : Boolean;
  begin
    Sub_Action (X);
    pragma Assert (X = True);
  end Critical_Action;

  procedure Sub_Action (X : out Boolean) with
    SPARK_Mode => Off
  is
    begin
      -- this procedure body is not analyzed
      X := True;
    end Sub_Action;

  procedure Non_Critical_Action with
    SPARK_Mode => Off
  is
    begin
      -- this procedure body is not analyzed
      null;
    end Non_Critical_Action;
end Selected_Units;
```

### Excluding Selected Unit Bodies

If a unit spec is in SPARK, but its body is not in SPARK, the spec can be marked with `SPARK_Mode => On` and the body with `SPARK_Mode => Off`. This allows client code in SPARK to use this unit. If `SPARK_Mode` is On by default, then it need not be repeated on the unit spec.

```plaintext
package Exclude_Unit_Body with
  SPARK_Mode => On
is

  type T is private;

  function Get_Value return Integer;

  procedure Set_Value (V : Integer) with
    Post => Get_Value = V;

private
  pragma SPARK_Mode (Off);

  -- the private part of the package spec is not analyzed
end Exclude_Unit_Body;
```
Note that the private part of the spec (which is physically in the spec file, but is logically part of the implementation) can be excluded as well, by using a pragma `SPARK_Mode (Off)` at the start of the private part.

```vhdl
package body Exclude_Unit_Body with
    SPARK_Mode => Off
is
    -- this package body is not analyzed
    Value : T := new Integer;
    
    function Get_Value return Integer is
    begin
        return Value.all;
    end Get_Value;
    
    procedure Set_Value (V : Integer) is
    begin
        Value.all := V;
    end Set_Value;
end Exclude_Unit_Body;
```

This scheme also works on generic units, which can then be instantiated both in code where `SPARK_Mode` is On, in which case only the body of the instantiated generic is excluded, or in code where `SPARK_Mode` is Off, in which case both the spec and the body of the instantiated generic are excluded.

```vhdl
generic
    type T is private;
package Exclude_Generic_Unit_Body with
    SPARK_Mode => On
is
    procedure Process (X : in out T);
end Exclude_Generic_Unit_Body;

package body Exclude_Generic_Unit_Body with
    SPARK_Mode => Off
is
    -- this package body is not analyzed
    procedure Process (X : in out T) is
    begin
        null;
    end Process;
end Exclude_Generic_Unit_Body;
```

```vhdl
with Exclude_Generic_Unit_Body;
pragma Elaborate_All (Exclude_Generic_Unit_Body);

package Use_Generic with
    SPARK_Mode => On
is
    -- the spec of this generic instance is analyzed
    package G1 is new Exclude_Generic_Unit_Body (Integer);
    
    procedure Do_Nothing;
```
package body Use_Generic with
  SPARK_Mode => Off
is
  type T is access Integer;
  -- this generic instance is not analyzed
  package G2 is new Exclude_Generic_Unit_Body (T);

  procedure Do_Nothing is
  begin
    null;
  end Do_Nothing;
end Use_Generic;

Excluding Selected Parts of a Unit

If most units are in SPARK except from some subprograms and packages, it makes sense to set the default to
SPARK_Mode (On), and set SPARK_Mode => Off on non-SPARK declarations. We assume here that a value of
SPARK_Mode => On is specified as a configuration pragma.

```plaintext
package Exclude_Selected_Parts is
  procedure Critical_Action;
  procedure Non_Critical_Action;
  package Non_Critical_Data with
    SPARK_Mode => Off
  is
    type T is access Integer;
    X : T;
    function Get_X return Integer;
  end Non_Critical_Data;
end Exclude_Selected_Parts;
```

Note that procedure Non_Critical_Action can be called inside SPARK code, because its spec is in SPARK,
even though its body is marked SPARK_Mode => Off.

Note also that the local package Non_Critical_Data can contain any non-SPARK types, variables and subpro-
grams, as it is marked SPARK_Mode => Off. It may be convenient to define such a local package to gather non-
SPARK declarations, which allows to mark globally the unit Exclude_Selected_Parts with SPARK_Mode
=> On.

```plaintext
package body Exclude_Selected_Parts is
  procedure Critical_Action is
  begin
    -- this procedure body is analyzed
    Non_Critical_Action;
  end Critical_Action;
```
procedure Non_Critical_Action with
  SPARK_Mode => Off
is
begin
  -- this procedure body is not analyzed
  null;
end Non_Critical_Action;

package body Non_Critical_Data with
  SPARK_Mode => Off
is
  -- this package body is not analyzed
  function Get_X return Integer is
    begin
      return X.all;
    end Get_X;
  end Non_Critical_Data;
end Exclude_Selected_Parts;
This chapter provides an overview of the SPARK language, detailing for each feature its consequences in terms of execution and formal verification. This is not a reference manual for the SPARK language, which can be found in:

- the Ada Reference Manual (for Ada features), and
- the SPARK 2014 Reference Manual (for SPARK-specific features)

More details on how GNAT compiles SPARK code can be found in the GNAT Reference Manual.

SPARK can be seen as a large subset of Ada with additional aspects/pragmas/attributes. It includes in particular:

- rich types (subtypes with bounds not known statically, discriminant records, subtype predicates, access types)
- flexible features to structure programs (function and operator overloading, early returns and exits, raise statements)
- code sharing features (generics, expression functions)
- object oriented features (tagged types, dispatching)
- concurrency features (tasks, protected objects)

In the rest of this chapter, the marker [Ada 2005] (resp. [Ada 2012]) is used to denote that a feature defined in Ada 2005 (resp. Ada 2012) is supported in SPARK, and the marker [Ravenscar] is used to denote that a concurrency feature from Ada which belongs to the Ravenscar profile is supported in SPARK. The marker [SPARK] is used to denote that a feature is specific to SPARK. Both the GNAT compiler and GNATprove analyzer support all features listed here.

Some code snippets presented in this section are available in the example called gnatprove_by_example distributed with the SPARK toolset. It can be found in the share/examples/spark directory below the directory where the toolset is installed, and can be accessed from the IDE (either GNAT Studio or GNATBench) via the Help → SPARK → Examples menu item.

5.1 Language Restrictions

5.1.1 Excluded Ada Features

To facilitate formal verification, SPARK enforces a number of global simplifications to Ada. The most notable simplifications are:

- Uses of access types and allocators must follow an ownership policy, so that only one access object has read-write permission to some allocated memory at any given time, or only read-only permission for that allocated memory is granted to possibly multiple access objects. See Memory Ownership Policy.
- All expressions (including function calls) are free of side-effects. Functions with side-effects are more complex to treat logically and may lead to non-deterministic evaluation due to conflicting side-effects in sub-expressions of an enclosing expression. Functions with side-effects should be written as procedures in SPARK.
• Aliasing of names is not permitted. Aliasing may lead to unexpected interferences, in which the value denoted locally by a given name changes as the result of an update to another locally named variable. Formal verification of programs with aliasing is less precise and requires more manual work. See *Absence of Interferences*.

• The backward goto statement is not permitted. Backward gotos can be used to create loops, which require a specific treatment in formal verification, and thus should be precisely identified. See *Loop Invariants* and *Loop Variants*.

• The use of controlled types is not permitted. Controlled types lead to the insertion of implicit calls by the compiler. Formal verification of implicit calls makes it harder for users to interact with formal verification tools, as there is no source code on which information can be reported.

• Handling of exceptions is not permitted. Exception handling gives raise to numerous interprocedural control-flow paths. Formal verification of programs with exception handlers requires tracking properties along all those paths, which is not doable precisely without a lot of manual work. But raising exceptions is allowed (see *Raising Exceptions and Other Error Signaling Mechanisms*).

• Unless explicitly specified as (possibly) nonreturning, subprograms should always terminate when called on inputs satisfying the subprogram precondition. While care is taken in GNATprove to reduce possibilities of unsoundness resulting from nonreturning subprograms, it is possible that axioms generated for nonreturning subprograms not specified as such may lead to unsoundness. See *Nonreturning Procedures*.

• Generic code is not analyzed directly. Doing so would require lengthy contracts on generic parameters, and would restrict the kind of code that can be analyzed, e.g. by forcing the variables read/written by a generic subprogram parameter. Instead, instantiations of generic code are analyzed in SPARK. See *Analysis of Generics*.

The features listed above are excluded from SPARK because, currently, they defy formal verification. As formal verification technology advances the list will be revisited and it may be possible to relax some of these restrictions. There are other features which are technically feasible to formally verify but which are currently not supported in SPARK, such as access-to-subprogram types.

Uses of these features in SPARK code are detected by GNATprove and reported as errors. Formal verification is not possible on subprograms using these features. But these features can be used in subprograms in Ada not identified as SPARK code, see *Identifying SPARK Code*.

### 5.1.2 Partially Analyzed Ada Features

SPARK reinforces the strong typing of Ada with a stricter initialization policy (see *Data Initialization Policy*), and thus provides no means currently of specifying that some input data may be invalid. As a result, the following features are allowed in SPARK, but only partially analyzed by GNATprove:

• The result of a call to *Unchecked_Conversion* is assumed to be a valid value of the resulting type.

• The evaluation of attribute *Valid* is assumed to always return True.

This is illustrated in the following example:

```ada
package Validity with SPARK_Mode is
  procedure Convert (X : Integer; Y : out Float);
end Validity;

with Ada.Unchecked_Conversion;

package body Validity with SPARK_Mode
```

Uses of these features in SPARK code are detected by GNATprove and reported as errors. Formal verification is not possible on subprograms using these features. But these features can be used in subprograms in Ada not identified as SPARK code, see *Identifying SPARK Code*.
GNATprove proves both assertions, but issues warnings about its assumptions that the evaluation of attribute \texttt{Valid} on both input parameter \texttt{X} and the result of the call to \texttt{Unchecked_Conversion} return True:

```
validity.adb:11:22: warning: attribute Valid is assumed to return True
validity.adb:13:22: warning: attribute Valid is assumed to return True
validity.ads:5:36: info: initialization of "Y" proved
```

### 5.1.3 Data Initialization Policy

Modes on parameters and data dependency contracts (see \textit{Data Dependencies}) in SPARK have a stricter meaning than in Ada:

- Parameter mode \texttt{in} (resp. global mode \texttt{Input}) indicates that the object denoted in the parameter (resp. data dependencies) should be completely initialized before calling the subprogram. It should not be written in the subprogram.
- Parameter mode \texttt{out} (resp. global mode \texttt{Output}) indicates that the object denoted in the parameter (resp. data dependencies) should be completely initialized before returning from the subprogram. It should not be read in the program prior to initialization.
- Parameter mode \texttt{in out} (resp. global mode \texttt{In_Out}) indicates that the object denoted in the parameter (resp. data dependencies) should be completely initialized before calling the subprogram. It can be written in the subprogram.
- Global mode \texttt{Proof_In} indicates that the object denoted in the data dependencies should be completely initialized before calling the subprogram. It should not be written in the subprogram, and only read in contracts and assertions.

Hence, all inputs should be completely initialized at subprogram entry, and all outputs should be completely initialized at subprogram output. Similarly, all objects should be completely initialized when read (e.g. inside subprograms), at the exception of record subcomponents (but not array subcomponents) provided the subcomponents that are read are initialized.

A consequence of the rules above is that a parameter (resp. global variable) that is partially written in a subprogram should be marked as \texttt{in out} (resp. \texttt{In_Out}), because the input value of the parameter (resp. global variable) is \texttt{read} when returning from the subprogram.

GNATprove will issue check messages if a subprogram does not respect the aforementioned data initialization policy.

For example, consider a procedure \texttt{Proc} which has a parameter and a global item of each mode:
is

  type Data is record
    Val : Float;
    Num : Natural;
  end record;

G1, G2, G3 : Data;

procedure Proc
  (P1 : in Data;
   P2 : out Data;
   P3 : in out Data) with
  Global => (Input => G1,
             Output => G2,
             In_Out => G3);

procedure Call_Proc with
  Global => (Output => (G1, G2, G3));

end Data_Initialization;

Procedure Proc should completely initialize its outputs P2 and G2, but it only initializes them partially. Similarly, procedure Call_Proc which calls Proc should completely initialize all of Proc’s inputs prior to the call, but it only initializes G1 completely.

package body Data_Initialization with
  SPARK_Mode
is

  procedure Proc
    (P1 : in Data;
     P2 : out Data;
     P3 : in out Data) is
  begin
    P2.Val := 0.0;
    G2.Num := 0;
    -- fail to completely initialize P2 and G2 before exit
  end Proc;

  procedure Call_Proc is
    X1, X2, X3 : Data;
  begin
    X1.Val := 0.0;
    X3.Num := 0;
    G1.Val := 0.0;
    G1.Num := 0;
    -- fail to completely initialize X1, X3 and G3 before call
    Proc (X1, X2, X3);
  end Call_Proc;

end Data_Initialization;

On this program, GNATprove issues 6 high check messages, corresponding to the violations of the data initialization policy:

While a user can justify individually such messages with pragma Annotate (see section Justifying Check Messages), it is under her responsibility to then ensure correct initialization of subcomponents that are read, as GNATprove relies during proof on the property that data is properly initialized before being read.

Note also the various warnings that GNATprove issues on unused parameters, global items and assignments, also based on the stricter SPARK interpretation of parameter and global modes.

5.1.4 Memory Ownership Policy

In SPARK, access values (a.k.a. pointers) are only allowed to alias in known ways, so that formal verification can be applied as if allocated memory pointed to by access values was a component of the access value seen as a record object.

In particular, assignment between access objects operates a transfer of ownership, where the source object loses its permission to read or write the underlying allocated memory.

For example, in the following example:

```ada
procedure Ownership_Transfer with
   SPARK_Mode
is
   type Int_Ptr is access Integer;
   X : Int_Ptr;
   Y : Int_Ptr;
   Tmp : Integer;
begin
   X := new Integer'(1);
   X.all := X.all + 1;
   Y := X;
   Y.all := Y.all + 1;
   X.all := X.all + 1; -- illegal
   X.all := 1; -- illegal
```
GNATprove correctly detects that `X.all` can neither be read nor written after the assignment of `X` to `Y` and issues corresponding messages:

```plaintext
ownership_transfer.adb:5:04: info: initialization of "X" proved
ownership_transfer.adb:6:04: info: initialization of "Y" proved
ownership_transfer.adb:13:06: insufficient permission on dereference from "X"
ownership_transfer.adb:13:15: insufficient permission on dereference from "X"
ownership_transfer.adb:14:06: insufficient permission on dereference from "X"
ownership_transfer.adb:14:15: object was moved at line 11
ownership_transfer.adb:15:15: insufficient permission on dereference from "X"
ownership_transfer.adb:15:15: object was moved at line 11
```

At call site, ownership is similarly transferred to the callee’s parameters for the duration of the call, and returned to the actual parameters (a.k.a. arguments) when returning from the call.

For example, in the following example:

```plaintext
procedure Ownership_Transfer_At_Call with
  SPARK_Mode
is
  type Int_Ptr is access Integer;
  X : Int_Ptr;

  procedure Proc (Y : in out Int_Ptr)
  with Global => (In_Out => X)
  is
  begin
    Y.all := Y.all + 1;
    X.all := X.all + 1;
  end Proc;

begin
  X := new Integer'(1);
  X.all := X.all + 1;
  Proc (X); -- illegal
end Ownership_Transfer_At_Call;
```

GNATprove correctly detects that the call to `Proc` cannot take `X` in argument as `X` is already accessed as a global variable by `Proc`.

```plaintext
ownership_transfer_at_call.adb:5:04: info: initialization of "X" proved
ownership_transfer_at_call.adb:8:11: info: data dependencies proved
ownership_transfer_at_call.adb:18:10: high: formal parameter "Y" and global "X" are ↪ → aliased (SPARK RM 6.4.2)
```

It is also possible to transfer the ownership of an object temporarily, for the duration of the lifetime of a local object. This can be achieved by declaring a local object of an anonymous access type and initializing it with a part of an existing object. In the following example, `B` temporarily borrows the ownership of `X`:

```plaintext
procedure Ownership_Borrowing with
  SPARK_Mode
is
  type Int_Ptr is access Integer;
```
During the lifetime of B, it is incorrect to either read or modify X, but complete ownership is restored to X when B goes out of scope. GNATprove correctly detects that reading or assigning to X in the scope of B is incorrect.

It is also possible to only transfer read access to a local variable. This happens when the variable has an anonymous access-to-constant type, as in the following example:

In this case, we say that B observes the value of X. During the lifetime of an observer, it is illegal to move or modify the observed object. GNATprove correctly flags the write inside X in the scope of B as illegal. Note that reading X is still possible in the scope of B:

Only pool-specific access types are allowed in SPARK, so it is not possible to declare access types with the qualifiers all or const, as these define general access types. This ensures in particular that access values in SPARK always point to dynamically-allocated memory, and thus can be freed when not null.
5.1.5 Absence of Interferences

In SPARK, an assignment to a variable cannot change the value of another variable. This is enforced by restricting the
use of access types (pointers) in SPARK, and by restricting aliasing between parameters and global variables so that
only benign aliasing is accepted (i.e. aliasing that does not cause interference).

The precise rules detailed in SPARK RM 6.4.2 can be summarized as follows:

• Two mutable parameters should never be aliased.
• An immutable and a mutable parameters should not be aliased, unless the immutable parameter is always passed
  by copy.
• A mutable parameter should never be aliased with a global variable referenced by the subprogram.
• An immutable parameter should not be aliased with a global variable referenced by the subprogram, unless the
  immutable parameter is always passed by copy.

An immutable parameter is either an input parameter that is not of an access type, or an anonymous access-to-constant
parameter. Except for parameters of access types, the immutable/mutable distinction is the same as the input/output
one.

These rules extend the existing rules in Ada RM 6.4.1 for restricting aliasing, which already make it illegal to call
a procedure with problematic (non-benign) aliasing between parameters of scalar type that are known to denote the
same object (a notion formally defined in Ada RM).

For example, in the following example:

```plaintext
package Aliasing with
  SPARK_Mode
is
  Glob : Integer;
  procedure Whatever (In_1, In_2 : Integer; Out_1, Out_2 : out Integer) with
    Global => Glob;
end Aliasing;
```

Procedure `Whatever` can only be called on arguments that satisfy the following constraints:

1. Arguments for `Out_1` and `Out_2` should not be aliased.
2. Variable `Glob` should not be passed in argument for `Out_1` and `Out_2`.

Note that there are no constraints on input parameters `In_1` and `In_2`, as these are always passed by copy (being of
a scalar type). This would not be the case if these input parameters were of a record or array type.

For example, here are examples of correct and illegal (according to Ada and SPARK rules) calls to procedure
`Whatever`:

```plaintext
with Aliasing; use Aliasing;

procedure Check_Param_Aliasing with
  SPARK_Mode
is
  X, Y, Z : Integer := 0;
begin
  Whatever (In_1 => X, In_2 => X, Out_1 => X, Out_2 => X); -- illegal
  Whatever (In_1 => X, In_2 => X, Out_1 => X, Out_2 => Y); -- correct
  Whatever (In_1 => X, In_2 => X, Out_1 => Y, Out_2 => X); -- correct
  Whatever (In_1 => Y, In_2 => Z, Out_1 => X, Out_2 => X); -- illegal
end Check_Param_Aliasing;
```
GNATprove (like GNAT compiler, since these are also Ada rules) correctly detects the two illegal calls and issues errors:

check_param_aliasing.adb:8:45: writable actual for "Out_1" overlaps with actual for "Out_2"
check_param_aliasing.adb:11:45: writable actual for "Out_1" overlaps with actual for "Out_2"

Here are other examples of correct and incorrect calls (according to SPARK rules) to procedure `Whatever`:

```ada
with Aliasing; use Aliasing;

procedure Check_Aliasing with SPARK_Mode is
  X, Y, Z : Integer := 0;
begin
  Whatever (In_1 => X, In_2 => X, Out_1 => X, Out_2 => Glob); -- incorrect
  Whatever (In_1 => X, In_2 => Y, Out_1 => Z, Out_2 => Glob); -- incorrect
  Whatever (In_1 => Glob, In_2 => Glob, Out_1 => X, Out_2 => Y); -- correct
end Check_Aliasing;
```

GNATprove correctly detects the two incorrect calls and issues high check messages:

check_aliasing.adb:8:57: high: formal parameter "Out_2" and global "Glob" are aliased
check_aliasing.adb:9:57: high: formal parameter "Out_2" and global "Glob" are aliased

### 5.1.6 Raising Exceptions and Other Error Signaling Mechanisms

Raising an exception is allowed in SPARK to signal an error, but handling the exception raised to perform recovery or mitigation actions is outside of the SPARK subset. Typically, such exception handling code should be added to top-level subprograms in full Ada, or to a last chance handler called by the runtime when an exception is raised, none of which is analyzed by GNATprove.

GNATprove treats raising an exception specially:

- in flow analysis, the program paths that lead to a `raise_statement` are not considered when checking the contract of the subprogram, which is only concerned with executions that terminate normally; and
- in proof, a check is generated for each `raise_statement`, to prove that no such program point is reachable.

Multiple error signaling mechanisms are treated the same way:

- raising an exception
- `pragma Assert (X)` where X is an expression statically equivalent to `False`
- calling a procedure with an aspect or `pragma No_Return` that has no outputs (unless the call is itself inside a (possibly) nonreturning procedure, see `Nonreturning Procedures`, in which case the check is only generated on the call to the enclosing error-signaling procedure if any)

For example, consider the artificial subprogram `Check_OK` which raises an exception when parameter `OK` is `False`:

```ada
package Abnormal_Terminations with SPARK_Mode is
```

G1, G2 : Integer := 0;

procedure Check_OK (OK : Boolean) with
    Global => (Output => G1),
    Pre => OK;
end Abnormal_Terminations;

Note that, although G2 is assigned in Check_OK, its assignment is directly followed by a raise_statement, so G2 is never assigned on an execution of Check_OK that terminates normally. As a result, G2 is not mentioned in the data dependencies of Check_OK. During flow analysis, GNATprove verifies that the body of Check_OK implements its declared data dependencies.

During proof, GNATprove generates a check that the raise_statement on line 11 is never reached. Here, it is proved thanks to the precondition of Check_OK which states that parameter OK should always be True on entry:

5.1.7 Nonreturning Procedures

GNATprove assumes that, unless explicitly specified as (possibly) nonreturning, subprograms should always terminate when called on inputs satisfying the subprogram precondition. In particular, functions should always terminate. Procedures might not terminate, in which case they should be annotated with a suitable pragma or aspect:

- No_Return to specify that the procedure never returns. This is a nonreturning procedure.
- Annotate Might_Not_Return to specify that the procedure might not return in some cases. This is a possibly nonreturning procedure.

Nonreturning and possibly nonreturning procedures are handled differently. It is an error to call a possibly nonreturning procedure from a function or from a procedure that is not itself (possibly) nonreturning. Calling a nonreturning procedure from a procedure that is not itself (possibly) nonreturning leads to a check that the call is unreachable. Such a call is in effect interpreted as an error signaling mechanism (see Raising Exceptions and Other Error Signaling Mechanisms).
For example, consider the procedure `Conditional.Exit` which conditionally calls the nonterminating `Always.Exit` procedure:

```ada
package Possibly_Nonreturning with
  SPARK_Mode
is
  procedure Always.Exit with No_Return, Import;
  procedure Conditional.Exit (Cond : Boolean) with
    Annotate => (GNATprove, Might_Not_Return);
  procedure Regular;
end Possibly_Nonreturning;
```

```ada
package body Possibly_Nonreturning with
  SPARK_Mode
is
  procedure Conditional.Exit (Cond : Boolean) is
    begin
      if Cond then
        Always.Exit;
      end if;
    end Conditional.Exit;
  procedure Regular is
    begin
      Conditional.Exit (True);
    end Regular;
end Possibly_Nonreturning;
```

GNATprove issues an error here on the call to the possibly nonreturning procedure `Conditional.Exit` in procedure `Regular`:

```ada
possibly_nonreturning.adb:14:07: call to possibly nonreturning procedure outside a
  (possibly) nonreturning procedure
possibly_nonreturning.adb:14:07: consider annotating caller "Regular" with Might_Not_Return
```

It would be legal to call the nonreturning procedure `Always.Exit` from procedure `Regular` though, in which case it will be interpreted as an error signaling mechanism, and GNATprove will attempt to prove that the call is unreachable.

Note that it is also possible to specify explicitly that a subprogram terminates, in which case GNATprove will verify that it indeed terminates. See `Subprogram Termination`.

### 5.1.8 Analysis of Generics

GNATprove does not directly analyze the code of generics. The following message is issued if you call GNATprove on a generic unit:

```ada
warning: no bodies have been analyzed by GNATprove
enable analysis of a non-generic body using SPARK_Mode
```
The advice given is to use `SPARK_Mode` on non-generic code, for example an instantiation of the generic unit. As `SPARK_Mode` aspect cannot be attached to a generic instantiation, it should be specified on the enclosing context, either through a pragma or aspect.

For example, consider the following generic increment procedure:

```plaintext
generic
  type T is range <>;
procedure Generic_Increment (X : in out T) with
  SPARK_Mode,
  Pre => X < T'Last,
  Post => X = X'Old + 1;
```

```plaintext
procedure Generic_Increment (X : in out T) with
  SPARK_Mode
is
begin
  X := X + 1;
end Generic_Increment;
```

Procedure `Instance_Increment` is a specific instance of `Generic_Increment` for the type `Integer`:

```plaintext
pragma SPARK_Mode;
with Generic_Increment;
procedure Instance_Increment is new Generic_Increment (Integer);
```

GNATprove analyzes this instantiation and reports messages on the generic code, always stating to which instantiation the messages correspond to:

```
generic_increment.adb:5:11: info: overflow check proved, in instantiation at instance_increment.ads:4
generic_increment.adb:6:11: info: postcondition proved, in instantiation at instance_increment.ads:4
generic_increment.adb:6:21: info: overflow check proved, in instantiation at instance_increment.ads:4
```

Thus, it is possible that some checks are proved on an instance and not on another one. In that case, the chained locations in the messages issued by GNATprove allow you to locate the problematic instantiation. In order to prove a generic library for all possible uses, you should choose extreme values for the generic parameters such that, if these instantiations are proved, any other choice of parameters will be provable as well.

### 5.2 Subprogram Contracts

The most important feature to specify the intended behavior of a SPARK program is the ability to attach a contract to subprograms. In this document, a subprogram can be a procedure, a function or a protected entry. This contract is made up of various optional parts:

- The **precondition** introduced by aspect `Pre` specifies constraints on callers of the subprogram.
- The **postcondition** introduced by aspect `Post` specifies (partly or completely) the functional behavior of the subprogram.
- The **contract cases** introduced by aspect `Contract_Cases` is a way to partition the behavior of a subprogram. It can replace or complement a precondition and a postcondition.
The data dependencies introduced by aspect Global specify the global data read and written by the subprogram.

The flow dependencies introduced by aspect Depends specify how subprogram outputs depend on subprogram inputs.

Which contracts to write for a given verification objective, and how GNATprove generates default contracts, is detailed in *How to Write Subprogram Contracts*.

The contract on a subprogram describes the behavior of successful calls. Executions that end up by signalling an error, as described in *Raising Exceptions and Other Error Signaling Mechanisms*, are not covered by the subprogram’s contract. A call to a subprogram is successful if execution terminates normally, or if execution loops without errors for a subprogram marked with aspect No_Return that has some outputs (this is typically the case of a non-terminating subprogram implementing the main loop of a controller).

### 5.2.1 Preconditions

[Ada 2012]

The precondition of a subprogram specifies constraints on callers of the subprogram. Typically, preconditions are written as conjunctions of constraints that fall in one of the following categories:

- exclusion of forbidden values of parameter, for example \( X \neq 0 \) or \( Y \notin \text{Active States} \)
- specification of allowed parameter values, for example \( X \in 1 .. 10 \) or \( Y \in \text{Idle States} \)
- relations that should hold between parameter values, for example (if \( Y \in \text{Active State} \) then \( Z \neq \text{Null State} \))
- expected values of global variables denoting the state of the computation, for example \( \text{Current State} \in \text{Active States} \)
- invariants about the global state that should hold when calling this subprogram, for example \( \text{Is Complete (State Mapping)} \)
- relations involving the global state and input parameters that should hold when calling this subprogram, for example \( X \in \text{Next States (Global Map, Y)} \)

When the program is compiled with assertions (for example with switch -gnata in GNAT), the precondition of a subprogram is checked at run time every time the subprogram is called. An exception is raised if the precondition fails. Not all assertions need to be enabled though. For example, a common idiom is to enable only preconditions (and not other assertions) in the production binary, by setting pragma `Assertion_Policy` as follows:

```plaintext
pragma Assertion_Policy (Pre => Check);
```

When a subprogram is analyzed with GNATprove, its precondition is used to restrict the contexts in which it may be executed, which is required in general to prove that the subprogram’s implementation:

- is free from run-time errors (see *Writing Contracts for Program Integrity*); and
- ensures that the postcondition of the subprogram always holds (see *Writing Contracts for Functional Correctness*).

In particular, the default precondition of True used by GNATprove when no explicit one is given may not be precise enough, unless it can be analyzed in the context of its callers by GNATprove (see *Contextual Analysis of Subprograms Without Contracts*). When a caller is analyzed with GNATprove, it checks that the precondition of the called subprogram holds at the point of call. And even when the implementation of the subprogram is not analyzed with GNATprove, it may be necessary to add a precondition to the subprogram for analyzing its callers (see *Writing Contracts on Imported Subprograms*).
For example, consider the procedure `Add_To_Total` which increments global counter `Total` by the value given in parameter `Incr`. To ensure that there are no integer overflows in the implementation, `Incr` should not be too large, which a user can express with the following precondition:

```ada
procedure Add_To_Total (Incr : in Integer) with
  Pre => Incr >= 0 and then Total <= Integer'Last - Incr;
```

To ensure that the value of `Total` remains non-negative, one should also add the condition `Total >= 0` to the precondition:

```ada
procedure Add_To_Total (Incr : in Integer) with
  Pre => Incr >= 0 and then Total in 0 .. Integer'Last - Incr;
```

Finally, GNATprove also analyzes preconditions to ensure that they are free from run-time errors in all contexts. This may require writing the precondition in a special way. For example, the precondition of `Add_To_Total` above uses the shortcut boolean operator `and then` instead of `and`, so that calling the procedure in a context where `Incr` is negative does not result in an overflow when evaluating `Integer'Last - Incr`. Instead, the use of `and then` ensures that a precondition failure will occur before the expression `Integer'Last - Incr` is evaluated.

---

**Note:** It is good practice to use the shortcut boolean operator `and then` instead of `and` in preconditions. This is required in some cases by GNATprove to prove absence of run-time errors inside preconditions.

---

### 5.2.2 Postconditions

[Ada 2012]

The postcondition of a subprogram specifies partly or completely the functional behavior of the subprogram. Typically, postconditions are written as conjunctions of properties that fall in one of the following categories:

- possible values returned by a function, using the special attribute `Result` (see `Attribute Result`), for example `Get'Result in Active_States`
- possible values of output parameters, for example `Y in Active_States`
- expected relations between output parameter values, for example `if Success then Y /= Null_State`
- expected relations between input and output parameter values, possibly using the special attribute `Old` (see `Attribute Old`), for example `if Success then Y /= Y'Old`
- expected values of global variables denoting updates to the state of the computation, for example `Current_State in Active_States`
- invariants about the global state that should hold when returning from this subprogram, for example `Is_Complete (State_Mapping)`
- relations involving the global state and output parameters that should hold when returning from this subprogram, for example `X in Next_States (Global_Map, Y)`

When the program is compiled with assertions (for example with switch `-gnata` in GNAT), the postcondition of a subprogram is checked at run time every time the subprogram returns. An exception is raised if the postcondition fails. Usually, postconditions are enabled during tests, as they provide dynamically checkable oracles of the intended behavior of the program, and disabled in the production binary for efficiency.

When a subprogram is analyzed with GNATprove, it checks that the postcondition of a subprogram cannot fail. This verification is modular: GNATprove considers all calling contexts in which the precondition of the subprogram holds for the analysis of a subprogram. GNATprove also analyzes postconditions to ensure that they are free from run-time errors, like any other assertion.
For example, consider the procedure `Add_To_Total` which increments global counter `Total` with the value given in parameter `Incr`. This intended behavior can be expressed in its postcondition:

```plaintext
procedure Add_To_Total (Incr : in Integer) with
    Post => Total = Total'Old + Incr;
```

The postcondition of a subprogram is used to analyze calls to the subprograms. In particular, the default postcondition of `True` used by GNATprove when no explicit one is given may not be precise enough to prove properties of its callers, unless it analyzes the subprogram’s implementation in the context of its callers (see Contextual Analysis of Subprograms Without Contracts).

Recursive subprograms and mutually recursive subprograms are treated in this respect exactly like non-recursive ones. Provided the execution of these subprograms always terminates (a property that is not verified by GNATprove), then GNATprove correctly checks that their postcondition is respected by using this postcondition for recursive calls.

Special care should be exercised for functions that return a boolean, as a common mistake is to write the expected boolean result as the postcondition:

```plaintext
function Total_Above_Threshold (Threshold : in Integer) return Boolean with
    Post => Total > Threshold;
```

while the correct postcondition uses Attribute Result:

```plaintext
function Total_Above_Threshold (Threshold : in Integer) return Boolean with
    Post => Total_Above_Threshold'Result = Total > Threshold;
```

Both GNAT compiler and GNATprove issue a warning on the semantically correct but likely functionally wrong postcondition.

### 5.2.3 Contract Cases

[SPARK]

When a subprogram has a fixed set of different functional behaviors, it may be more convenient to specify these behaviors as contract cases rather than a postcondition. For example, consider a variant of procedure `Add_To_Total` which either increments global counter `Total` by the given parameter value when possible, or saturates at a given threshold. Each of these behaviors can be defined in a contract case as follows:

```plaintext
procedure Add_To_Total (Incr : in Integer) with
    Contract_Cases => (Total + Incr < Threshold => Total = Total'Old + Incr,
                        Total + Incr >= Threshold => Total = Threshold);
```

Each contract case consists in a guard and a consequence separated by the symbol `=>`. When the guard evaluates to `True` on subprogram entry, the corresponding consequence should also evaluate to `True` on subprogram exit. We say that this contract case was enabled for the call. Exactly one contract case should be enabled for each call, or said equivalently, the contract cases should be disjoint and complete.

For example, the contract cases of `Add_To_Total` express that the subprogram should be called in two distinct cases only:

- on inputs that can be added to `Total` to obtain a value strictly less than a given threshold, in which case `Add_To_Total` adds the input to `Total`.
- on inputs whose addition to `Total` exceeds the given threshold, in which case `Add_To_Total` sets `Total` to the threshold value.
When the program is compiled with assertions (for example with switch -gnata in GNAT), all guards are evaluated on entry to the subprogram, and there is a run-time check that exactly one of them is True. For this enabled contract case, there is another run-time check when returning from the subprogram that the corresponding consequence evaluates to True.

When a subprogram is analyzed with GNATprove, it checks that there is always exactly one contract case enabled, and that the consequence of the contract case enabled cannot fail. If the subprogram also has a precondition, GNATprove performs these checks only for inputs that satisfy the precondition, otherwise for all inputs.

In the simple example presented above, there are various ways to express an equivalent postcondition, in particular using Conditional Expressions:

```plaintext
procedure Add_To_Total (Incr : in Integer) with
  Post => (if Total'Old + Incr < Threshold then
    Total = Total'Old + Incr
  else
    Total = Threshold);
```

```plaintext
procedure Add_To_Total (Incr : in Integer) with
  Post => Total = (if Total'Old + Incr < Threshold then Total'Old + Incr else
  Threshold);
```

```plaintext
procedure Add_To_Total (Incr : in Integer) with
  Post => Total = Integer'Min (Total'Old + Incr, Threshold);
```

In general, an equivalent postcondition may be cumbersome to write and less readable. Contract cases also provide a way to automatically verify that the input space is partitioned in the specified cases, which may not be obvious with a single expression in a postcondition when there are many cases.

The guard of the last case may be others, to denote all cases not captured by previous contract cases. For example, the contract of Add_To_Total may be written:

```plaintext
procedure Add_To_Total (Incr : in Integer) with
  Contract_Cases => (Total + Incr < Threshold => Total = Total'Old + Incr,
  others => Total = Threshold);
```

When others is used as a guard, there is no need for verification (both at run-time and using GNATprove) that the set of contract cases covers all possible inputs. Only disjointness of contract cases is checked in that case.

### 5.2.4 Data Dependencies

[SPARK]

The data dependencies of a subprogram specify the global data that a subprogram is allowed to read and write. Together with the parameters, they completely specify the inputs and outputs of a subprogram. Like parameters, the global variables mentioned in data dependencies have a mode: Input for inputs, Output for outputs and In_Out for global variables that are both inputs and outputs. A last mode of Proof_In is defined for inputs that are only read in contracts and assertions. For example, data dependencies can be specified for procedure Add_To_Total which increments global counter Total as follows:

```plaintext
procedure Add_To_Total (Incr : in Integer) with
  Global => (In_Out => Total);
```

For protected subprograms, the protected object is considered as an implicit parameter of the subprogram:

- it is an implicit parameter of mode in of a protected function; and
- it is an implicit parameter of mode in out of a protected procedure or a protected entry.
Data dependencies have no impact on compilation and the run-time behavior of a program. When a subprogram is analyzed with GNATprove, it checks that the implementation of the subprogram:

- only reads global inputs mentioned in its data dependencies,
- only writes global outputs mentioned in its data dependencies, and
- always completely initializes global outputs that are not also inputs.

See Data Initialization Policy for more details on this analysis of GNATprove. During its analysis, GNATprove uses the specified data dependencies of callees to analyze callers, if present, otherwise a default data dependency contract is generated (see Generation of Dependency Contracts) for callees.

There are various benefits when specifying data dependencies on a subprogram, which gives various reasons for users to add such contracts:

- GNATprove verifies automatically that the subprogram implementation respects the specified accesses to global data.
- GNATprove uses the specified contract during flow analysis, to analyze the data and flow dependencies of the subprogram’s callers, which may result in a more precise analysis (less false alarms) than with the generated data dependencies.
- GNATprove uses the specified contract during proof, to check absence of run-time errors and the functional contract of the subprogram’s callers, which may also result in a more precise analysis (less false alarms) than with the generated data dependencies.

When data dependencies are specified on a subprogram, they should mention all global data read and written in the subprogram. When a subprogram has neither global inputs nor global outputs, it can be specified using the null data dependencies:

```plaintext
function Get (X : T) return Integer with
  Global => null;
```

When a subprogram has only global inputs but no global outputs, it can be specified either using the Input mode:

```plaintext
function Get_Sum return Integer with
  Global => (Input => (X, Y, Z));
```

or equivalently without any mode:

```plaintext
function Get_Sum return Integer with
  Global => (X, Y, Z);
```

Note the use of parentheses around a list of global inputs or outputs for a given mode.

Global data that is both read and written should be mentioned with the In_Out mode, and not as both input and output. For example, the following data dependencies on Add_To_Total are illegal and rejected by GNATprove:

```plaintext
procedure Add_To_Total (Incr : in Integer) with
  Global => (Input => Total, Output => Total); -- INCORRECT
```

Global data that is partially written in the subprogram should also be mentioned with the In_Out mode, and not as an output. See Data Initialization Policy.

### 5.2.5 Flow Dependencies

[SPARK]
The flow dependencies of a subprogram specify how its outputs (both output parameters and global outputs) depend on its inputs (both input parameters and global inputs). For example, flow dependencies can be specified for procedure `Add_To_Total` which increments global counter `Total` as follows:

```
procedure Add_To_Total (Incr : in Integer) with
  Depends => (Total => (Total, Incr));
```

The above flow dependencies can be read as “the output value of global variable `Total` depends on the input values of global variable `Total` and parameter `Incr`”.

Outputs (both parameters and global variables) may have an implicit input part depending on their type:

- an unconstrained array `A` has implicit input bounds `A'First` and `A'Last`
- a discriminated record `R` has implicit input discriminants, for example `R.Discr`

Thus, an output array `A` and an output discriminated record `R` may appear in input position inside a flow-dependency contract, to denote the input value of the bounds (for the array) or the discriminants (for the record).

For protected subprograms, the protected object is considered as an implicit parameter of the subprogram which may be mentioned in the flow dependencies, under the name of the protected unit (type or object) being declared:

- as an implicit parameter of mode `in` of a protected function, it can be mentioned on the right-hand side of flow dependencies; and
- as an implicit parameter of mode `in out` of a protected procedure or a protected entry, it can be mentioned on both sides of flow dependencies.

Flow dependencies have no impact on compilation and the run-time behavior of a program. When a subprogram is analyzed with GNATprove, it checks that, in the implementation of the subprogram, outputs depend on inputs as specified in the flow dependencies. During its analysis, GNATprove uses the specified flow dependencies of callees to analyze callers, if present, otherwise a default flow dependency contract is generated for callees (see Generation of Dependency Contracts).

When flow dependencies are specified on a subprogram, they should mention all flows from inputs to outputs. In particular, the output value of a parameter or global variable that is partially written by a subprogram depends on its input value (see Data Initialization Policy).

When the output value of a parameter or global variable depends on its input value, the corresponding flow dependency can use the shorthand symbol `+` to denote that a variable’s output value depends on the variable’s input value plus any other input listed. For example, the flow dependencies of `Add_To_Total` above can be specified equivalently:

```
procedure Add_To_Total (Incr : in Integer) with
  Depends => (Total =>+ Incr);
```

When an output value depends on no input value, meaning that it is completely (re)initialized with constants that do not depend on variables, the corresponding flow dependency should use the `null` input list:

```
procedure Init_Total with
  Depends => (Total => null);
```

### 5.2.6 State Abstraction and Contracts

[SPARK]

The subprogram contracts mentioned so far always used directly global variables. In many cases, this is not possible because the global variables are defined in another unit and not directly visible (because they are defined in the private part of a package specification, or in a package implementation). The notion of abstract state in SPARK can be used in that case (see State Abstraction) to name in contracts global data that is not visible.
State Abstraction and Dependencies

Suppose the global variable *Total* incremented by procedure *Add_To_Total* is defined in the package implementation, and a procedure *Cash_Tickets* in a client package calls *Add_To_Total*. Package *Account* which defines *Total* can define an abstract state *State* that represents *Total*, as seen in *State Abstraction*, which allows using it in *Cash_Tickets*’s data and flow dependencies:

```plaintext
procedure Cash_Tickets (Tickets : Ticket_Array) with
  Global => (Output => Account.State),
  Depends => (Account.State => Tickets);
```

As global variable *Total* is not visible from clients of unit *Account*, it is not visible either in the visible part of *Account*’s specification. Hence, externally visible subprograms in *Account* must also use abstract state *State* in their data and flow dependencies, for example:

```plaintext
procedure Init_Total with
  Global => (Output => State),
  Depends => (State => null);

procedure Add_To_Total (Incr : in Integer) with
  Global => (In_Out => State),
  Depends => (State =>+ Incr);
```

Then, the implementations of *Init_Total* and *Add_To_Total* can define refined data and flow dependencies introduced respectively by *Refined_Global* and *Refined_Depends*, which give the precise dependencies for these subprograms in terms of concrete variables:

```plaintext
procedure Init_Total with
  Refined_Global => (Output => Total),
  Refined_Depends => (Total => null)
is
begin
  Total := 0;
end Init_Total;

procedure Add_To_Total (Incr : in Integer) with
  Refined_Global => (In_Out => Total),
  Refined_Depends => (Total =>+ Incr)
is
begin
  Total := Total + Incr;
end Add_To_Total;
```

Here, the refined dependencies are the same as the abstract ones where *State* has been replaced by *Total*, but that’s not always the case, in particular when the abstract state is refined into multiple concrete variables (see *State Abstraction*). GNATprove checks that:

- each abstract global input has at least one of its constituents mentioned by the concrete global inputs
- each abstract global in_out has at least one of its constituents mentioned with mode input and one with mode output (or at least one constituent with mode in_out)
- each abstract global output has to have all its constituents mentioned by the concrete global outputs
- the concrete flow dependencies are a subset of the abstract flow dependencies

GNATprove uses the abstract contract (data and flow dependencies) of *Init_Total* and *Add_To_Total* when analyzing calls outside package *Account* and the more precise refined contract (refined data and flow dependencies) of *Init_Total* and *Add_To_Total* when analyzing calls inside package *Account*. 
Refined dependencies can be specified on both subprograms and tasks for which data and/or flow dependencies that are specified include abstract states which are refined in the current unit.

State Abstraction and Functional Contracts

If global variables are not visible for data dependencies, they are not visible either for functional contracts. For example, in the case of procedure Add_To_Total, if global variable Total is not visible, we cannot express anymore the precondition and postcondition of Add_To_Total as in Preconditions and Postconditions. Instead, we define accessor functions to retrieve properties of the state that we need to express, and we use these in contracts. For example here:

```plaintext
function Get_Total return Integer;

procedure Add_To_Total (Incr : in Integer) with
  Pre => Incr >= 0 and then Get_Total in 0 .. Integer'Last - Incr,
  Post => Get_Total = Get_Total'Old + Incr;
```

Function Get_Total may be defined either in the private part of package Account or in its implementation. It may take the form of a regular function or an expression function (see Expression Functions), for example:

```plaintext
Total : Integer;
function Get_Total return Integer is (Total);
```

Although no refined preconditions and postconditions are required on the implementation of Add_To_Total, it is possible to provide a refined postcondition introduced by Refined_Post in that case, which specifies a more precise functional behavior of the subprogram. For example, procedure Add_To_Total may also increment the value of a counter Call_Count at each call, which can be expressed in the refined postcondition:

```plaintext
procedure Add_To_Total (Incr : in Integer) with
  Refined_Post => Total = Total'Old + Incr and Call_Count = Call_Count'Old + 1
is
  ...
end Add_To_Total;
```

A refined postcondition can be given on a subprogram implementation even when the unit does not use state abstraction, and even when the default postcondition of True is used implicitly on the subprogram declaration.

GNATprove uses the abstract contract (precondition and postcondition) of Add_To_Total when analyzing calls outside package Account and the more precise refined contract (precondition and refined postcondition) of Add_To_Total when analyzing calls inside package Account.

5.3 Package Contracts

Subprograms are not the only entities to bear contracts in SPARK. Package contracts are made up of various optional parts:

- The state abstraction specifies how global variables defined in the package are referred to abstractly where they are not visible. Aspect Abstract_State introduces abstract names and aspect Refined_State specifies the mapping between these names and global variables.

- The package initialization introduced by aspect Initializes specifies which global data (global variables and abstract state) defined in the package is initialized at package startup.
• The package initial condition introduced by aspect Initial_Condition specifies the properties holding after package startup.

Package startup (a.k.a. package elaboration in Ada RM) consists in the evaluation of all declarations in the package specification and implementation, in particular the evaluation of constant declarations and those variable declarations which contain an initialization expression, as well as the statements sometimes given at the end of a package body that are precisely executed at package startup.

5.3.1 State Abstraction

[SPARK]
The state abstraction of a package specifies a mapping between abstract names and concrete global variables defined in the package. State abstraction allows to define Subprogram Contracts at an abstract level that does not depend on a particular choice of implementation (see State Abstraction and Contracts), which is better both for maintenance (no need to change contracts) and scalability of analysis (contracts can be much smaller).

Basic State Abstraction

One abstract name may be mapped to more than one concrete variable, but no two abstract names can be mapped to the same concrete variable. When state abstraction is specified on a package, all non-visible global variables defined in the private part of the package specification and in its implementation should be mapped to abstract names. Thus, abstract names correspond to a partitioning of the non-visible global variables defined in the package.

The simplest use of state abstraction is to define a single abstract name (conventionally called State) to denote all non-visible global variables defined in the package. For example, consider package Account defining a global variable Total in its implementation, which is abstracted as State:

```ada
package Account with
  Abstract_State => State
is
  ...
end Account;

package body Account with
  Refined_State => (State => Total)
is
  Total : Integer;
  ...
end Account;
```

The aspect Refined_State maps each abstract name to a list of concrete global variables defined in the package. The list can be simply null to serve as placeholder for future definitions of global variables. Instead of concrete global variables, one can also use abstract names for the state of nested packages and private child packages, whose state is considered to be also defined in the parent package.

If global variable Total is defined in the private part of Account’s package specification, then the declaration of Total must use the special aspect Part_Of to declare its membership in abstract state State:

```ada
package Account with
  Abstract_State => State
is
  ...
private
  Total : Integer with Part_Of => State;
```
This ensures that Account’s package specification can be checked by GNATprove even if its implementation is not in SPARK, or not available for analysis, or not yet developed.

A package with state abstraction must have a package body that states how abstract states are refined in aspect Refined_State, unless the package body is not in SPARK. If there is no other reason for the package to have a body, then one should use pragma Elaborate_Body in the package spec to make it legal for the package to have a body on which to express state refinement.

In general, an abstract name corresponds to multiple global variables defined in the package. For example, we can imagine adding global variables to log values passed in argument to procedure Add_To_Total, that are also mapped to abstract name State:

```plaintext
package Account with
  Abstract_State => State
is
  ...
end Account;

package body Account with
  Refined_State => (State => (Total, Log, Log_Size))
is
  Total  : Integer;
  Log    : Integer_Array;
  Log_Size : Natural;
  ...
end Account;
```

We can also imagine defining different abstract names for the total and the log:

```plaintext
package Account with
  Abstract_State => (State, Internal_State)
is
  ...
end Account;

package body Account with
  Refined_State => (State => Total,
                   Internal_State => (Log, Log_Size))
is
  Total  : Integer;
  Log    : Integer_Array;
  Log_Size : Natural;
  ...
end Account;
```

The abstract names defined in a package are visible everywhere the package name itself is visible:

- in the scope where the package is declared, for a locally defined package
- in units that have a clause with <package>;
- in units that have a clause limited with <package>;

The last case allows subprograms in two packages to mutually reference the abstract state of the other package in their data and flow dependencies.
Special Cases of State Abstraction

Global constants with a statically known value are not part of a package’s state. On the contrary, *constant with variable inputs* are constants whose value depends on the value of either a variable or a subprogram parameter. Since they participate in the flow of information between variables, constants with variable inputs are treated like variables: they are part of a package’s state, and they must be listed in its state refinement whenever they are not visible. For example, constant `Total_Min` is not part of the state refinement of package `Account` below, while constant with variable inputs `Total_Max` is part of it:

```plaintext
package body Account with
  Refined_State => (State => (Total, Total_Max))
is
  Total   : Integer;
  Total_Min : constant Integer := 0;
  Total_Max : constant Integer := Compute_Total_Max(...);
... end Account;
```

Global variables are not always the only constituents of a package’s state. For example, if a package `P` contains a nested package `N`, then `N`’s state is part of `P`’s state. As a consequence, if `N` is hidden, then its state must be listed in `P`’s refinement. For example, we can nest `Account` in the body of the `Account_Manager` package as follows:

```plaintext
package Account_Manager with
  Abstract_State => State
is
  ... end Account_Manager;

package body Account_Manager with
  Refined_State => (State => Account.State)
is
  package Account with
    Abstract_State => State
    is
      ... end Account;
  ... end Account_Manager;
```

State In The Private Part

Global variables and nested packages which themselves contain state may be declared in the private part of a package. For each such global variable and nested package state, it is mandatory to identify, using aspect `Part_Of`, the abstract state of the enclosing package of which it is a constituent:

```plaintext
package Account_Manager with
  Abstract_State => (Totals, Details)
is
  ... private
    Total_Accounts : Integer with Part_Of => Totals;

    package Account with
      Abstract_State => (State with Part_Of => Details)
      is
        Total : Integer with Part_Of => Totals;
```

The purpose of using `Part_Of` is to enforce that each constituent of an abstract state is known at the declaration of the constituent (not having to look at the package body), which is useful for both code understanding and tool analysis (including compilation).

As the state of a private child package is logically part of its parent package, aspect `Part_Of` must also be specified in that case:

```plaintext
private package Account_Manager.Account with
    Abstract_State => (State with Part_Of => Details)
is
    Total : Integer with Part_Of => Totals;
...
end Account_Manager.Account;
```

Aspect `Part_Of` can also be specified on a generic package instantiation inside a private part, to specify that all the state (visible global variables and abstract states) of the package instantiation is a constituent of an abstract state of the enclosing package:

```plaintext
package Account_Manager with
    Abstract_State => (Totals, Details)
is
    ...
    private
    package Account is new Generic_Account (Max_Total) with Part_Of => Details;
    ...
end Account_Manager;
```

### 5.3.2 Package Initialization

[SPARK]

The package initialization specifies which global data (global variables, constant with variable inputs, and abstract state) defined in the package is initialized at package startup. The corresponding global variables may either be initialized at declaration, or by the package body statements. Thus, package initialization can be seen as the output data dependencies of the package elaboration procedure generated by the compiler.

For example, we can specify that the state of package `Account` is initialized at package startup as follows:

```plaintext
package Account with
    Abstract_State => State,
    Initializes => State
is
    ...
end Account;
```

Then, unless `Account`'s implementation is not in SPARK, it should initialize the corresponding global variable `Total` either at declaration:

```plaintext
package body Account with
    Refined_State => (State => Total)
is
```
Total : Integer := 0;
...
end Account;

or in the package body statements:

```plaintext
package body Account with
  Refined_State => (State => Total)
is
  Total : Integer;
  ...
begin
  Total := 0;
end Account;
```

These initializations need not correspond to direct assignments, but may be performed in a call, for example here to procedure Init_Total as seen in State Abstraction and Dependencies. A mix of initializations at declaration and in package body statements is also possible.

Package initializations also serve as dependency contracts for global variables' initial values. That is, if the initial value of a global variable, state abstraction, or constant with variable inputs listed in a package initialization depends on the value of a variable defined outside the package, then this dependency must be listed in the package's initialization. For example, we can initialize Total by reading the value of an external variable:

```plaintext
package Account with
  Abstract_State => State,
  Initializes => (State => External_Variable)
is
  ...
end Account;

package body Account with
  Refined_State => (State => Total)
is
  Total : Integer := External_Variable;
  ...
end Account;
```

5.3.3 Package Initial Condition

[SPARK]

The package initial condition specifies the properties holding after package startup. Thus, package initial condition can be seen as the postcondition of the package elaboration procedure generated by the compiler. For example, we can specify that the value of Total defined in package Account's implementation is initially zero:

```plaintext
package Account with
  Abstract_State => State,
  Initial_Condition => Get_Total = 0
is
  function Get_Total return Integer;
  ...
end Account;
```

This is ensured either by initializing Total with value zero at declaration, or by assigning the value zero to Total in the package body statements, as seen in Package Initialization.
When the program is compiled with assertions (for example with switch -gnata in GNAT), the initial condition of a package is checked at run time after package startup. An exception is raised if the initial condition fails.

When a package is analyzed with GNATprove, it checks that the initial condition of a package cannot fail. GNATprove also analyzes the initial condition expression to ensure that it is free from run-time errors, like any other assertion.

5.3.4 Interfaces to the Physical World

[SPARK]

Volatile Variables

Most embedded programs interact with the physical world or other programs through so-called *volatile* variables, which are identified as volatile to protect them from the usual compiler optimizations. In SPARK, volatile variables are also analyzed specially, so that possible changes to their value from outside the program are taken into account, and so that changes to their value from inside the program are also interpreted correctly (in particular for checking flow dependencies).

For example, consider package *Volatile_Or_Not* which defines a volatile variable *V* and a non-volatile variable *N*, and procedure *Swap_Then_Zero* which starts by swapping the values of *V* and *N* before zeroing them out:

```plaintext
package Volatile_Or_Not with
   SPARK_Mode,
   Initializes => V
is
   V : Integer with Volatile;
   N : Integer;
   procedure Swap_Then_Zero with
      Global => (In_Out => (N, V)),
      Depends => (V => N, N => null, null => V);
end Volatile_Or_Not;

package body Volatile_Or_Not with
   SPARK_Mode
is
   procedure Swap_Then_Zero is
      Tmp : constant Integer := V;
      begin
         -- Swap values of V and N
         V := N;
         N := Tmp;
         -- Zero out values of V and N
         V := 0;
         N := 0;
      end Swap_Then_Zero;
end Volatile_Or_Not;
```

Compare the difference in contracts between volatile variable *V* and non-volatile variable *N*:

- The *Package Initialization* of package *Volatile_Or_Not* mentions *V* although this variable is not initialized at declaration or in the package body statements. This is because a volatile variable is assumed to be initialized.

- The *Flow Dependencies* of procedure *Swap_Then_Zero* are very different for *V* and *N*. If both variables were not volatile, the correct contract would state that both input values are not used with null => (V, N) and
that both output values depend on no inputs with \((V, N) \rightarrow \text{null}\). The difference lies with the special treatment of volatile variable \(V\): as its value may be read at any time, the intermediate value \(N\) assigned to \(V\) on line 8 of `volatile_or_not.adb` needs to be mentioned in the flow dependencies for output \(V\).

GNATprove checks that `Volatile_Or_Not` and `Swap_Then_Zero` implement their contract, and it issues a warning on the first assignment to \(N\):

```
volatile_or_not.adb:9:09: warning: unused assignment
volatile_or_not.ads:3:03: info: flow dependencies proved
volatile_or_not.ads:9:06: info: data dependencies proved
volatile_or_not.ads:10:06: info: flow dependencies proved
```

This warning points to a real issue, as the intermediate value of \(N\) is not used before \(N\) is zeroed out on line 12. But note that no warning is issued on the similar first assignment to \(V\), because the intermediate value of \(V\) may be read outside the program before \(V\) is zeroed out on line 11.

Note that in real code, the memory address of the volatile variable is set through aspect `Address` or the corresponding representation clause, so that it can be read or written outside the program.

**Properties of Volatile Variables**

Not all volatile variables are read and written outside the program, sometimes they are only read or only written outside the program. For example, the log introduced in `State Abstraction` could be implemented as an output port for the program logging the information, and as an input port for the program performing the logging. Two aspects are defined in SPARK to distinguish these different properties of volatile variables:

- **Aspect Async_Writers** indicates that the value of the variable may be changed at any time (asynchronously) by hardware or software outside the program.
- **Aspect Async_Readers** indicates that the value of the variable may be read at any time (asynchronously) by hardware or software outside the program.

Aspect `Async_Writers` has an effect on GNATprove’s proof: two successive reads of such a variable may return different results. Aspect `Async_Readers` has an effect on GNATprove’s flow analysis: an assignment to such a variable always has a potential effect, even if the value is never read in the program, since an external reader might actually read the value assigned.

These aspects are well suited to model respectively a sensor and a display, but not an input stream or an actuator, for which the act of reading or writing has an effect that should be reflected in the flow dependencies. Two more aspects are defined in SPARK to further refine the previous properties of volatile variables:

- **Aspect Effective_Reads** indicates that reading the value of the variable has an effect (for example, removing a value from an input stream). It can only be specified on a variable that also has `Async_Writers` set.
- **Aspect Effective_Writes** indicates that writing the value of the variable has an effect (for example, sending a command to an actuator). It can only be specified on a variable that also has `Async_Readers` set.

Both aspects `Effective_Reads` and `Effective_Writes` have an effect on GNATprove’s flow analysis: reading the former or writing the latter is modelled as having an effect on the value of the variable, which needs to be reflected in flow dependencies. Because reading a variable with `Effective_Reads` set has an effect on its value, such a variable cannot be only a subprogram input, it must be also an output.

For example, the program writing in a log each value passed as argument to procedure `Add_To_Total` may model the output port `Log_Out` as a volatile variable with `Async_Readers` and `Effective_Writes` set:

```
package Logging_Out with
  SPARK_Mode
is
```
Total : Integer;
Log_Out : Integer with Volatile, Async_Readers, Effective_Writes;

procedure Add_To_Total (Incr : in Integer) with
Global => (In_Out => Total, Output => Log_Out),
Depends => (Total =>+ Incr, Log_Out => Incr);
end Logging_Out;

package body Logging_Out with
SPARK_Mode
is
procedure Add_To_Total (Incr : in Integer) is
begin
  Total := Total + Incr;
  Log_Out := Incr;
end Add_To_Total;
end Logging_Out;

while the logging program may model the input port Log_In as a volatile variable with Async_Writers and Effective_Reads set:

package Logging_In with
SPARK_Mode
is
  Log_In : Integer with Volatile, Async_Writers, Effective_Reads;

type Integer_Array is array (Positive range 1 .. 100) of Integer;
Log : Integer_Array;
Log_Size : Natural;

procedure Get with
Global => (In_Out => (Log, Log_Size, Log_In)),
Depends => ((Log_Size, Log_In) =>+ null, Log =>+ (Log_Size, Log_In));
end Logging_In;

package body Logging_In with
SPARK_Mode
is
  procedure Get is
begin
  Log_Size := Log_Size + 1;
  Log (Log_Size) := Log_In;
end Get;
end Logging_In;

GNATprove checks the specified data and flow dependencies on both programs.

A volatile variable on which none of the four aspects Async_Writers, Async_Readers, Effective_Reads or Effective_Writes is set is assumed to have all four aspects set to True. A volatile variable on which some of the four aspects are set to True is assumed to have the remaining ones set to False. See SPARK RM 7.1.3 for details.
**External State Abstraction**

Volatile variables may be part of *State Abstraction*, in which case the volatility of the abstract name must be specified by using aspect `External` on the abstract name, as follows:

```haskell
package Account with
  Abstract_State => (State with External)
is
  ...
end Account;
```

An external state may represent both volatile variables and non-volatile ones, for example:

```haskell
package body Account with
  Refined_State => (State => (Total, Log, Log_Size))
is
  Total : Integer;
  Log : Integer_Array with Volatile;
  Log_Size : Natural with Volatile;
  ...
end Account;
```

The different *Properties of Volatile Variables* may also be specified in the state abstraction, which is then used by GNATprove to refine the analysis. For example, the program writing in a log seen in the previous section can be rewritten to abstract global variables as follows:

```haskell
package Logging_Out_Abstract with
  SPARK_Mode,
  Abstract_State => (State with External => (Async_Readers, Effective_Writes)),
  Initializes => State
is
  procedure Add_To_Total (Incr : in Integer) with
  Global => (In_Out => State),
  Depends => (State =>+ Incr);
end Logging_Out_Abstract;
```

```haskell
package body Logging_Out_Abstract with
  SPARK_Mode,
  Refined_State => (State => (Log_Out, Total))
is
  Total : Integer := 0;
  Log_Out : Integer := 0 with Volatile, Async_Readers, Effective_Writes;
  procedure Add_To_Total (Incr : in Integer) with
  Refined_Global => (In_Out => Total, Output => Log_Out),
  Refined_Depends => (Total =>+ Incr, Log_Out => Incr)
  is
    begin
      Total := Total + Incr;
      Log_Out := Incr;
    end Add_To_Total;
end Logging_Out_Abstract;
```

while the logging program seen in the previous section may be rewritten to abstract global variables as follows:
package Logging_In_Abstract with
  SPARK_Mode,
  Abstract_State => (State with External => (Async_Writers, Effective_Reads))
is
  procedure Get with
    Global => (In_Out => State),
    Depends => (State =>+ null);
end Logging_In_Abstract;

package body Logging_In_Abstract with
  SPARK_Mode,
  Refined_State => (State => (Log_In, Log, Log_Size))
is
  Log_In : Integer with Volatile, Async_Writers, Effective_Reads;
  type Integer_Array is array (Positive range 1 .. 100) of Integer;
  Log : Integer_Array := (others => 0);
  Log_Size : Natural := 0;
  procedure Get with
    Refined_Global => (In_Out => (Log, Log_Size, Log_In)),
    Refined_Depends => ((Log_Size, Log_In) =>+ null, Log =>+ (Log_Size, Log_In))
  is
    begin
      Log_Size := Log_Size + 1;
      Log (Log_Size) := Log_In;
    end Get;
end Logging_In_Abstract;

GNATprove checks the specified data and flow dependencies on both programs.

An external abstract state on which none of the four aspects Async_Writers, Async_Readers, Effective_Reads or Effective_Writes is set is assumed to have all four aspects set to True. An external abstract state on which some of the four aspects are set to True is assumed to have the remaining ones set to False. See SPARK RM 7.1.2 for details.

### 5.4 Type Contracts

SPARK contains various features to constrain the values of a given type:

- A **scalar range** may be specified on a scalar type or subtype to bound its values.
- A **record discriminant** may be specified on a record type to distinguish between variants of the same record.
- A **predicate** introduced by aspect Static_Predicate, Dynamic_Predicate or Predicate may be specified on a type or subtype to express a property verified by objects of the (sub)type.
- A **type invariant** introduced by aspect Type_Invariant or Invariant may be specified on the completion of a private type to express a property that is only guaranteed outside of the type scope.
- A **default initial condition** introduced by aspect Default_Initial_Condition on a private type specifies the initialization status and possibly properties of the default initialization for a type.

Note that SPARK does not yet support aspect Type_Invariant from Ada 2012.
5.4.1 Scalar Ranges

Scalar types (signed integer types, modulo types, fixed-point types, floating-point types) can be given a low bound and a high bound to specify that values of the type must remain within these bounds. For example, the global counter Total can never be negative, which can be expressed in its type:

```
Total : Integer range 0 .. Integer'Last;
```

Any attempt to assign a negative value to variable `Total` results in raising an exception at run time. During analysis, GNATprove checks that all values assigned to `Total` are positive or null. The anonymous subtype above can also be given an explicit name:

```
subtype Nat is Integer range 0 .. Integer'Last;
Total : Nat;
```

or we can use the equivalent standard subtype `Natural`:

```
Total : Natural;
```

or `Nat` can be defined as a derived type instead of a subtype:

```
type Nat is new Integer range 0 .. Integer'Last;
Total : Nat;
```

or as a new signed integer type:

```
type Nat is range 0 .. Integer'Last;
Total : Nat;
```

All the variants above result in the same range checks both at run-time and in GNATprove. GNATprove also uses the range information for proving properties about the program (for example, the absence of overflows in computations).

5.4.2 Record Discriminants

Record types can use discriminants to:

- define multiple variants and associate each component with a specific variant
- bound the size of array components

For example, the log introduced in *State Abstraction* could be implemented as a discriminated record with a discriminant `Kind` selecting between two variants of the record for logging either only the minimum and maximum entries or the last entries, and a discriminant `Capacity` specifying the maximum number of entries logged:

```
package Logging_Discr with SPARK_Mode is
  type Log_KIND is (Min_Max_Values, Last_Values);
  type Integer_Array is array (Positive range <>) of Integer;
  type Log_Type (Kind : Log_KIND; Capacity : Natural) is record
    case Kind is
      when Min_Max_Values =>
        Min_Entry : Integer;
```
Subtypes of Log_Type can specify fixed values for Kind and Capacity, like in Min_Max_Log and Ten_Values_Log. The discriminants Kind and Capacity are accessed like regular components, for example:

```plaintext
package body Logging_Discr with
  SPARK_Mode
is
  function Log_Size (Log : Log_Type) return Natural is
    begin
      case Log.Kind is
        when Min_Max_Values =>
          return 2;
        when Last_Values =>
          return Log.Log_Size;
      end case;
    end Log_Size;

  function Last_Entry (Log : Log_Type) return Integer is
    begin
      return Log.Log_Data (Log.Log_Size);
    end Last_Entry;
end Logging_Discr;
```

Any attempt to access a component not present in a variable (because it is of a different variant), or to access an array component outside its bounds, results in raising an exception at run time. During analysis, GNATprove checks that components accessed are present, and that array components are accessed within bounds:

```
logging_discr.adb:10:23: info: discriminant check proved
logging_discr.adb:16:17: info: discriminant check proved
logging_discr.adb:16:31: info: discriminant check proved
logging_discr.adb:16:31: info: index check proved
logging_discr.ads:13:13: info: range check proved
logging_discr.ads:18:37: info: range check proved
logging_discr.ads:18:53: info: range check proved
logging_discr.ads:19:40: info: range check proved
logging_discr.ads:19:53: info: range check proved
logging_discr.ads:24:48: info: discriminant check proved
```
5.4.3 Predicates

Predicates can be used on any subtype to express a property verified by objects of the subtype at all times. Aspects Static_Predicate and Dynamic_Predicate are defined in Ada 2012 to associate a predicate with a subtype. Aspect Dynamic_Predicate allows to express more general predicates than aspect Static_Predicate, at the cost of restricting the use of variables of the subtype. The following table summarizes the main similarities and differences between both aspects:

<table>
<thead>
<tr>
<th>Feature</th>
<th>Static_Predicate</th>
<th>Dynamic_Predicate</th>
</tr>
</thead>
<tbody>
<tr>
<td>Applicable to scalar subtype</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Applicable to array/record subtype</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Allows simple comparisons with static values</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Allows conjunctions/disjunctions</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Allows function calls</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Allows general Boolean properties</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Can be used in membership test</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Can be used as range in for-loop</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Can be used as choice in case-statement</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Can be used as prefix with attributes First, Last or Range</td>
<td>No</td>
<td>No</td>
</tr>
<tr>
<td>Can be used as index subtype in array</td>
<td>No</td>
<td>No</td>
</tr>
</tbody>
</table>

Aspect Predicate is specific to GNAT and can be used instead of Static_Predicate or Dynamic_Predicate. GNAT treats it as a Static_Predicate whenever possible and as a Dynamic_Predicate in the remaining cases, thus not restricting uses of variables of the subtype more than necessary.

Predicates are inherited by subtypes and derived types. If a subtype or a derived type inherits a predicate and defines its own predicate, both predicates are checked on values of the new (sub)type. Predicates are restricted in SPARK so that they cannot depend on variable input. In particular, a predicate cannot mention a global variable in SPARK, although it can mention a global constant.

GNATprove checks that all values assigned to a subtype with a predicate are allowed by its predicate (for all three forms of predicate: Predicate, Static_Predicate and Dynamic_Predicate). GNATprove generates a predicate check even in cases where there is no corresponding run-time check, for example when assigning to a component of a record with a predicate. GNATprove also uses the predicate information for proving properties about the program.

**Static Predicates**

A static predicate allows specifying which values are allowed or forbidden in a scalar subtype, when this specification cannot be expressed with Scalar Ranges (because it has holes). For example, we can express that the global counter Total cannot be equal to 10 or 100 with the following static predicate:

```ada
subtype Count is Integer with
  Static_Predicate => Count /= 10 and Count /= 100;
Total : Count;
```

or equivalently:

```ada
subtype Count is Integer with
  Static_Predicate => Count in Integer'First .. 9 | 11 .. 99 | 101 .. Integer'Last;
Total : Count;
```
Uses of the name of the subtype Count in the predicate refer to variables of this subtype. Scalar ranges and static predicates can also be combined, and static predicates can be specified on subtypes, derived types and new signed integer types. For example, we may define Count as follows:

```ada
type Count is new Natural with
  Static_Predicate => Count /= 10 and Count /= 100;
```

Any attempt to assign a forbidden value to variable Total results in raising an exception at run time. During analysis, GNATprove checks that all values assigned to Total are allowed.

Similarly, we can express that values of subtype Normal_Float are the normal 32-bits floating-point values (thus excluding subnormal values), assuming here that Float is the 32-bits floating-point type on the target:

```ada
subtype Normal_Float is Float with
  Static_Predicate => Normal_Float <= -2.0**(-126) or Normal_Float = 0.0 or Normal_→Float >= 2.0**(-126);
```

Any attempt to assign a subnormal value to a variable of subtype Normal_Float results in raising an exception at run time. During analysis, GNATprove checks that only normal values are assigned to such variables.

**Dynamic Predicates**

A dynamic predicate allows specifying properties of scalar subtypes that cannot be expressed as static predicates. For example, we can express that values of subtype Odd and Even are distributed according to their name as follows:

```ada
subtype Odd is Natural with
  Dynamic_Predicate => Odd mod 2 = 1;
```

```ada
subtype Even is Natural with
  Dynamic_Predicate => Even mod 2 = 0;
```

or that values of type Prime are prime numbers as follows:

```ada
type Prime is new Positive with
  Dynamic_Predicate => (for all Divisor in 2 .. Prime / 2 => Prime mod Divisor /= 0);
```

A dynamic predicate also allows specifying relations between components of a record. For example, we can express that the values paired together in a record are always distinct as follows:

```ada
type Distinct_Pair is record
  Val1, Val2 : Integer;
end record
  with Dynamic_Predicate => Distinct_Pair.Val1 /= Distinct_Pair.Val2;
```

or that a record stores pairs of values with their greatest common divisor as follows:

```ada
type Bundle_Values is record
  X, Y : Integer;
  GCD : Natural;
end record
  with Dynamic_Predicate => Bundle_Values.GCD = Get_GCD (Bundle_Values.X, Bundle_→.Values.Y);
```

or that the number of elements Count in a resizable table is always less than or equal to its maximal number of elements Max as follows:
type Resizable_Table (Max : Natural) is record
  Count : Natural;
  Data : Data_Array(1 .. Max);
end record
  with Dynamic_Predicate => Resizable_Table.Count <= Resizable_Table.Max;

A dynamic predicate also allows specifying global properties over the content of an array. For example, we can express that elements of an array are stored in increasing order as follows:

```ada
type Ordered_Array is array (Index) of Integer
  with Dynamic_Predicate =>
    (for all I in Index => (if I < Index'Last then Ordered_Array(I) < Ordered_Array(I+1)));
```
or that a special end marker is always present in the array as follows:

```ada
type Ended_Array is array (Index) of Integer
  with Dynamic_Predicate =>
    (for some I in Index => Ended_Array(I) = End_Marker);
```

Dynamic predicates are checked only at specific places at run time, as mandated by the Ada Reference Manual:

- when converting a value to the subtype with the predicate
- when returning from a call, for each in-out and out parameter passed by reference
- when declaring an object, except when there is no initialization expression and no subcomponent has a default expression

Thus, not all violations of the dynamic predicate are caught at run time. On the contrary, during analysis, GNATprove checks that initialized variables whose subtype has a predicate always contain a value allowed by the predicate.

### 5.4.4 Type Invariants

[Ada 2012]

In SPARK, type invariants can only be specified on completions of private types (and not directly on private type declarations). They express a property that is only guaranteed outside of the immediate scope of the type bearing the invariant. Aspect `Type_Invariant` is defined in Ada 2012 to associate an invariant with a type. Aspect `Invariant` is specific to GNAT and can be used instead of `Type_Invariant`.

GNATprove checks that, outside of the immediate scope of a type with an invariant, all values of this type are allowed by its invariant. In order to provide such a strong guarantee, GNATprove generates an invariant check even in cases where there is no corresponding run-time check, for example on global variables that are modified by a subprogram. GNATprove also uses the invariant information for proving properties about the program.

As an example, let us consider a stack, which can be queried for the maximum of the elements stored in it:

```ada
package P is
  type Stack is private;
  function Max (S : Stack) return Element;
private
```
In the implementation, an additional component is allocated for the maximum, which is kept up to date by the implementation of the stack. This information is a type invariant, which can be specified using a `Type_Invariant` aspect:

```plaintext
private

type Stack is record
    Content : Element_Array := (others => 0);
    Size    : My_Length := 0;
    Max     : Element := 0;
end record with
    Type_Invariant => Is_Valid (Stack);

function Is_Valid (S : Stack) return Boolean is
    ((for all I in 1 .. S.Size => S.Content (I) <= S.Max)
        and (if S.Max > 0 then
            (for some I in 1 .. S.Size => S.Content (I) = S.Max)));

function Max (S : Stack) return Element is (S.Max);
end P;
```

Like for subtype predicates, the name of the type can be used inside the invariant expression to refer to the current instance of the type. Here the subtype predicate of `Stack` expresses that the `Max` field of a valid stack is the maximum of the elements stored in the stack.

To make sure that the invariant holds for every value of type `Stack` outside of the package `P`, GNATprove introduces invariant checks in several places. First, at the type declaration, it will make sure that the invariant holds every time an object of type `Stack` is default initialized. Here, as the stack is empty by default and the default value of `Max` is 0, the check will succeed. It is also possible to forbid default initialization of objects of type `Stack` altogether by using a `Default_Initial_Condition` of `False`:

```plaintext
type Stack is private with Default_Initial_Condition => False;

type Stack is record
    Content : Element_Array;
    Size    : My_Length;
    Max     : Element;
end record with Type_Invariant => Is_Valid (Stack);
```

A check is also introduced to make sure the invariant holds for every global object declared in the scope of `Stack` after it has been initialized:

```plaintext
package body P is

    The_Stack : Stack := (Content => (others => 1),
        Size    => 5,
        Max     => 0);

begin

    The_Stack.Max := 1;

end P;
```

Here the global variable `The_Stack` is allowed to break its invariant during the elaboration of `P`. The invariant check will only be done at the end of the elaboration of `P`, and will succeed.

In the same way, variables and parameters of a subprogram are allowed to break their invariants in the subprogram
body. Verification conditions are generated to ensure that no invariant breaking value can leak outside of $P$. More precisely, invariant checks on subprogram parameters are performed:

- when calling a subprogram visible outside of $P$ from inside of $P$. Such a subprogram can be either declared in the visible part of $P$ or in another unit,

- when returning from a subprogram declared in the visible part of $P$.

For example, let us consider the implementation of a procedure $\text{Push}$ that pushes an element of top of a stack. It is declared in the visible part of the specification of $P$:

```plaintext
function Size (S : Stack) return My_Length;

procedure Push (S : in out Stack; E : Element) with
  Pre => Size (S) < My-Length'Last;

procedure Push_Zero (S : in out Stack) with
  Pre => Size (S) < My-Length'Last;
```

It is then implemented using an internal procedure $\text{Push_Internal}$ declared in the body of $P$:

```plaintext
procedure Push_Internal (S : in out Stack; E : Element) with
  Pre => S.Size < My-Length'Last,
  Post => S.Size = S.Size'Old + 1 and S.Content (S.Size) = E
  and S.Content (1 .. S.Size)'Old = S.Content (1 .. S.Size - 1)
  and S.Max = S.Max'Old
is
begin
  S.Size := S.Size + 1;
  S.Content (S.Size) := E;
end Push_Internal;

procedure Push (S : in out Stack; E : Element) is
begin
  Push_Internal (S, E);
  if S.Max < E then
    S.Max := E;
  end if;
end Push;

procedure Push_Zero (S : in out Stack) is
begin
  Push (S, 0);
end Push_Zero;
```

On exit of $\text{Push_Internal}$, the invariant of $\text{Stack}$ is broken. It is OK since $\text{Push_Internal}$ is not visible from outside of $P$. Invariant checks are performed when exiting $\text{Push}$ and when calling it from inside $\text{Push_Zero}$. They both succeed. Note that, because of invariant checks on parameters, it is not allowed in SPARK to call a function that is visible from outside $P$ in the invariant of $\text{Stack}$ otherwise this would lead to a recursive proof. In particular, it is not allowed to make $\text{Is_Valid}$ visible in the public declarations of $P$. In the same way, the function $\text{Size}$ cannot be used in the invariant of $\text{Stack}$. We also avoid using $\text{Size}$ in the contract of $\text{Push_Internal}$ as it would have enforced additional invariant checks on its parameter.

Checks are also performed for global variables accessed by subprograms inside $P$. Even if it is allowed to break the invariant of a global variable when inside the body of a subprogram declared in $P$, invariant checks are performed when calling and returning from every subprogram inside $P$. For example, if $\text{Push}$ and $\text{Push_Internal}$ are accessing directly the global stack $\text{The_Stack}$ instead of taking it as a parameter, there will be a failed invariant check on exit of $\text{Push_Internal}$:
procedure Push_Internal (E : Element) with
   Pre  => The_Stack.Size < My_Length'Last
is
begin
   The_Stack.Size := The_Stack.Size + 1;
   The_Stack.Content (The_Stack.Size) := E;
end Push_Internal;

procedure Push (E : Element) is
begin
   Push_Internal (E);
   if The_Stack.Max < E then
      The_Stack.Max := E;
   end if;
end Push;

In this way, users will never have to use contracts to ensure that the invariant holds on global variable The_Stack through local subprogram calls.

### 5.4.5 Default Initial Condition

[SPARK]

Private types in a package define an encapsulation mechanism that prevents client units from accessing the implementation of the type. That boundary may also be used to specify properties that hold for default initialized values of that type in client units. For example, the log introduced in State Abstraction could be implemented as a private type with a default initial condition specifying that the size of the log is initially zero, where uses of the name of the private type Log_Type in the argument refer to variables of this type:

```plaintext
package Logging_Priv with
   SPARK_Mode
is
   Max_Count : constant := 100;

   type Log_Type is private with
      Default_Initial_Condition => Log_Size (Log_Type) = 0;

   function Log_Size (Log : Log_Type) return Natural;

   procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
      Pre => Log_Size (Log) < Max_Count;

private

   type Integer_Array is array (1 .. Max_Count) of Integer;

   type Log_Type is record
      Log_Data : Integer_Array;
      Log_Size : Natural := 0;
   end record;

   function Log_Size (Log : Log_Type) return Natural is (Log.Log_Size);
end Logging_Priv;
```

This may be useful to analyze with GNATprove client code that defines a variable of type Log_Type with default initialization, and then proceeds to append values to this log, as procedure Append_To_Log’s precondition requires
that the log size is not maximal:

```plaintext
The_Log : Log_Type;
...
Append_To_Log (The_Log, X);
```

GNATprove’s flow analysis also uses the presence of a default initial condition as an indication that default initialized variables of that type are considered as fully initialized. So the code snippet above would pass flow analysis without messages being issued on the read of `The_Log`. If the full definition of the private type is in SPARK, GNATprove also checks that the type is indeed fully default initialized, and if not issues a message like here:

```plaintext
logging_priv.ads:18:04: medium: type "Log_Type" is not fully initialized
```

If partial default initialization of the type is intended, in general for efficiency like here, then the corresponding message can be justified with pragma `Annotate`, see section *Justifying Check Messages*.

Aspect `Default_Initial_Condition` can also be specified without argument to only indicate that default initialized variables of that type are considered as fully initialized. This is equivalent to `Default_Initial_Condition => True`:

```plaintext
type Log_Type is private with
  Default_Initial_Condition;
```

The argument can also be `null` to specify that default initialized variables of that type are *not* considered as fully initialized:

```plaintext
type Log_Type is private with
  Default_Initial_Condition => null;
```

This is different from an argument of `False` which can be used to indicate that variables of that type should always be explicitly initialized (otherwise GNATprove will not be able to prove the condition `False` on the default initialization and will issue a message during proof).

## 5.5 Specification Features

SPARK contains many features for specifying the intended behavior of programs. Some of these features come from Ada 2012 (*Attribute Old* and *Expression Functions* for example). Other features are specific to SPARK (*Attribute Loop_Entry* and *Ghost Code* for example). In this section, we describe these features and their impact on execution and formal verification.

### 5.5.1 Aspect Constant_After_Elaboration

Aspect `Constant_After_Elaboration` can be specified on a library level variable that has an initialization expression. When specified, the corresponding variable can only be changed during the elaboration of its enclosing package. SPARK ensures that users of the package do not change the variable. This feature can be particularly useful in tasking code since variables that are `Constant_After_Elaboration` are guaranteed to prevent unsynchronized modifications (see *Tasks and Data Races*).

```plaintext
package CAE is
  Var : Integer := 0 with
    Constant_After_Elaboration;

  -- The following is illegal because users of CAE could call Illegal
  -- and that would cause an update of Var after CAE has been
```
procedure Illegal with
  Global => (Output => Var);
end CAE;

package body CAE is
  procedure Illegal is
    begin
      Var := 10;
    end Illegal;

  -- The following subprogram is legal because it is declared inside
  -- the body of CAE and therefore it cannot be directly called
  -- from a user of CAE.
  procedure Legal is
    begin
      Var := Var + 2;
    end Legal;

begin
  -- The following statements are legal since they take place during
  -- the elaboration of CAE.
  Var := Var + 1;
  Legal;
end CAE;

5.5.2 Aspect No_Caching

Aspect No_Caching can be specified for a volatile variable to indicate that this variable can be analyzed as non-volatile by GNATprove. This is typically used to hold the value of local variables guarding the access to some critical section of the code. To defend against fault injection attacks, a common practice is to duplicate the test guarding the critical section, and the variable is marked as volatile to prevent the compiler from optimizing out the duplicate tests. For example:

Cond : Boolean with Volatile, No_Caching := Some_Computation;

if not Cond then
  return;
end if;

if not Cond then
  return;
end if;

if Cond then
  -- here do some critical work
end if;

Without No_Caching, the volatile variable is assumed to be used for Interfaces to the Physical World, GNATprove analyses it specially and one cannot declare it inside a subprogram.

5.5.3 Attribute Old

[Ada 2012]
In a Postcondition

Inside Postconditions, attribute Old refers to the values that expressions had at subprogram entry. For example, the postcondition of procedure Increment might specify that the value of parameter X upon returning from the procedure has been incremented:

```ada
procedure Increment (X : in out Integer) with
  Post => X = X'Old + 1;
```

At run time, a copy of the variable X is made when entering the subprogram. This copy is then read when evaluating the expression X'Old in the postcondition. Because it requires copying the value of X, the type of X cannot be limited.

Strictly speaking, attribute Old must apply to a name in Ada syntax, for example a variable, a component selection, a call, but not an addition like X + Y. For expressions that are not names, attribute Old can be applied to their qualified version, for example:

```ada
procedure Increment_One_Of (X, Y : in out Integer) with
  Post => X + Y = Integer'(X + Y)'Old + 1;
```

Because the compiler unconditionally creates a copy of the expression to which attribute Old is applied at subprogram entry, there is a risk that this feature might confuse users in more complex postconditions. Take the example of a procedure Extract, which copies the value of array A at index J into parameter V, and zeroes out this value in the array, but only if J is in the bounds of A:

```ada
procedure Extract (A : in out My_Array; J : Integer; V : out Value)
  with
  Post => (if J in A'Range then V = A(J)'Old) -- INCORRECT
```

Clearly, the value of A(J) at subprogram entry is only meaningful if J is in the bounds of A. If the code above was allowed, then a copy of A(J) would be made on entry to subprogram Extract, even when J is out of bounds, which would raise a run-time error. To avoid this common pitfall, use of attribute Old in expressions that are potentially unevaluated (like the then-part in an if-expression, or the right argument of a shortcut boolean expression - See Ada RM 6.1.1) is restricted to plain variables: A is allowed, but not A(J). The GNAT compiler issues the following error on the code above:

```
prefix of attribute "Old" that is potentially unevaluated must denote an entity
```

The correct way to specify the postcondition in the case above is to apply attribute Old to the entity prefix A:

```ada
procedure Extract (A : in out My_Array; J : Integer; V : out Value)
  with
  Post => (if J in A'Range then V = A'Old(J));
```

In Contract Cases

The rule for attribute Old inside Contract Cases is more permissive. Take for example the same contract as above for procedure Extract, expressed with contract cases:

```ada
procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
  Contract_Cases => ((J in A'Range) => V = A(J)'Old,
                      others => True);
```

Only the expressions used as prefixes of attribute Old in the currently enabled case are copied on entry to the subprogram. So if Extract is called with J out of the range of A, then the second case is enabled, so A(J) is not copied when entering procedure Extract. Hence, the above code is allowed.

It may still be the case that some contracts refer to the value of objects at subprogram entry inside potentially unevaluated expressions. For example, an incorrect variation of the above contract would be:
procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
  Contract_Cases => (J >= A’First => (if J <= A’Last then V = A(J)’Old), -- INCORRECT
                     others => True);

For the same reason that such uses are forbidden by Ada RM inside postconditions, the SPARK RM forbids these uses inside contract cases (see SPARK RM 6.1.3(2)). The GNAT compiler issues the following error on the code above:

prefix of attribute "Old" that is potentially unevaluated must denote an entity

The correct way to specify the consequence expression in the case above is to apply attribute Old to the entity prefix A:

procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
  Contract_Cases => (J >= A’First => (if J <= A’Last then V = A’Old(J)),
                      others => True);

In a Potentially Unevaluated Expression

In some cases, the compiler issues the error discussed above (on attribute Old applied to a non-entity in a potentially unevaluated context) on an expression that can safely be evaluated on subprogram entry, for example:

procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
  Post => (if J in A’Range then V = Get_If_In_Range(A,J)’Old); -- ERROR

where function Get_If_In_Range returns the value A(J) when J is in the bounds of A, and a default value otherwise.

In that case, the solution is either to rewrite the postcondition using nonshortcut boolean operators, so that the expression is not potentially evaluated anymore, for example:

procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
  Post => J not in A’Range or V = Get_If_In_Range(A,J)’Old;

or to rewrite the postcondition using an intermediate expression function, so that the expression is not potentially evaluated anymore, for example:

function Extract_Post (A : My_Array; J : Integer; V, Get_V : Value) return Boolean is
  (if J in A’Range then V = Get_V);

procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
  Post => Extract_Post (A, J, V, Get_If_In_Range(A,J)’Old);

or to use the GNAT pragma Unevaluated_Use_Of_Old to allow such uses of attribute Old in potentially unevaluated expressions:

pragma Unevaluated_Use_Of_Old (Allow);

procedure Extract (A : in out My_Array; J : Integer; V : out Value) with
  Post => (if J in A’Range then V = Get_If_In_Range(A,J)’Old);

GNAT does not issue an error on the code above, and always evaluates the call to Get_If_In_Range on entry to procedure Extract, even if this value may not be used when executing the postcondition. Note that the formal verification tool GNATprove correctly generates all required checks to prove that this evaluation on subprogram entry does not fail a run-time check or a contract (like the precondition of Get_If_In_Range if any).
Pragma Unevaluated_Use_Of_Old applies to uses of attribute Old both inside postconditions and inside contract cases. See GNAT RM for a detailed description of this pragma.

### 5.5.4 Attribute Result

[Ada 2012]

Inside *Postconditions* of functions, attribute Result refers to the value returned by the function. For example, the postcondition of function *Increment* might specify that it returns the value of parameter *X* plus one:

```ada
function Increment (X : Integer) return Integer with
  Post => Increment'Result = X + 1;
```

Contrary to *Attribute Old*, attribute Result does not require copying the value, hence it can be applied to functions that return a limited type. Attribute Result can also be used inside consequence expressions in *Contract Cases*.

### 5.5.5 Attribute Loop_Entry

[SPARK]

It is sometimes convenient to refer to the value of variables at loop entry. In many cases, the variable has not been modified between the subprogram entry and the start of the loop, so this value is the same as the value at subprogram entry. But *Attribute Old* cannot be used in that case. Instead, we can use attribute *Loop_Entry*. For example, we can express that after *J* iterations of the loop, the value of parameter array *X* at index *J* is equal to its value at loop entry plus one:

```ada
procedure Increment_Array (X : in out Integer_Array) is
  begin
    for J in X'Range loop
      X(J) := X(J) + 1;
      pragma Assert (X(J) = X'Loop_Entry(J) + 1);
    end loop
  end Increment_Array;
```

At run time, a copy of the variable *X* is made when entering the loop. This copy is then read when evaluating the expression *X'Loop_Entry*. No copy is made if the loop is never entered. Because it requires copying the value of *X*, the type of *X* cannot be limited.

Attribute *Loop_Entry* can only be used in top-level *Assertion Pragmas* inside a loop. It is mostly useful for expressing complex *Loop Invariants* which relate the value of a variable at a given iteration of the loop and its value at loop entry. For example, we can express that after *J* iterations of the loop, the value of parameter array *X* at all indexes already seen is equal to its value at loop entry plus one, and that its value at all indexes not yet seen is unchanged, using *Quantified Expressions*:

```ada
procedure Increment_Array (X : in out Integer_Array) is
  begin
    for J in X'Range loop
      X(J) := X(J) + 1;
      pragma Loop_Invariant (for all K in X'First .. J => X(K) = X'Loop_Entry(K) + 1);
      pragma Loop_Invariant (for all K in J + 1 .. X'Last => X(K) = X'Loop_Entry(K));
    end loop;
  end Increment_Array;
```

Attribute *Loop_Entry* may be indexed by the name of the loop to which it applies, which is useful to refer to the value of a variable on entry to an outer loop. When used without loop name, the attribute applies to the closest
enclosing loop. For example, \texttt{X'\text{Loop\_Entry}} is the same as \texttt{X'\text{Loop\_Entry(Inner)}} in the loop below, which is not the same as \texttt{X'\text{Loop\_Entry(Outer)}} (although all three assertions are true):

```plaintext
procedure Increment_Matrix (X : in out Integer_Matrix) is
begin
  Outer: for J in X'Range(1) loop
    Inner: for K in X'Range(2) loop
      X(J,K) := X(J,K) + 1;
      pragma Assert (X(J,K) = X'\text{Loop\_Entry(J,K)} + 1);
      pragma Assert (X(J,K) = X'\text{Loop\_Entry(Inner)(J,K)} + 1);
      pragma Assert (X(J,K) = X'\text{Loop\_Entry(Outer)(J,K)} + 1);
    end loop Inner;
  end loop Outer;
end Increment_Matrix;
```

By default, similar restrictions exist for the use of attribute \texttt{\text{Loop\_Entry}} and the use of attribute \texttt{\text{Old In a Potentially Unevaluated Expression}}. The same solutions apply here, in particular the use of GNAT pragma \texttt{Unevaluated\_Use\_Of\_Old}.

### 5.5.6 Attribute Update

[SPARK]

It is quite common in \textit{Postconditions} to relate the input and output values of parameters. While this can be as easy as \texttt{X = X'Old + 1} in the case of scalar parameters, it is more complex to express for array and record parameters. Attribute \texttt{Update} is useful in that case, to denote the updated value of a composite variable. For example, we can express more clearly that procedure \texttt{Zero\_Range} zeroes out the elements of its array parameter \texttt{X} between \texttt{From} and \texttt{To} by using attribute \texttt{Update}:

```plaintext
procedure Zero_Range (X : in out Integer_Array; From, To : Positive) with
  Post => X = X'Old'\text{Update(From} .. \text{To} \Rightarrow 0);
```

than with an equivalent postcondition using \textit{Quantified Expressions} and \textit{Conditional Expressions}:

```plaintext
procedure Zero_Range (X : in out Integer_Array; From, To : Positive) with
  Post => (for all J in X'Range =>
    if J in From .. To then X(J) = 0 else X(J) = X'Old(J)));
```

Attribute \texttt{Update} takes in argument a list of associations between indexes (for arrays) or components (for records) and values. Components can only be mentioned once, with the semantics that all values are evaluated before any update. Array indexes may be mentioned more than once, with the semantics that updates are applied in left-to-right order. For example, the postcondition of procedure \texttt{Swap} expresses that the values at indexes \texttt{J} and \texttt{K} in array \texttt{X} have been swapped:

```plaintext
procedure Swap (X : in out Integer_Array; J, K : Positive) with
  Post => X = X'Old'\text{Update(J} => X'Old(K), K => X'Old(J));
```

and the postcondition of procedure \texttt{Rotate\_Clockwise\_Z} expresses that the point \texttt{P} given in parameter has been rotated 90 degrees clockwise around the \texttt{Z} axis (thus component \texttt{Z} is preserved while components \texttt{X} and \texttt{Y} are modified):

```plaintext
procedure Rotate\_Clockwise\_Z (P : in out Point_3D) with
  Post => P = P'Old'\text{Update(X} => P.Y'Old, Y => - P.X'Old);
```

Similarly to its use in combination with attribute \texttt{Old} in postconditions, attribute \texttt{Update} is useful in combination with \textit{Attribute Loop\_Entry} inside \textit{Loop Invariants}. For example, we can express the property that, after iteration \texttt{J} in the main loop in procedure \texttt{Zero\_Range}, the value of parameter array \texttt{X} at all indexes already seen is equal to zero:
procedure Zero_Range (X : in out Integer_Array; From, To : Positive) is
begin
  for J in From .. To loop
    X(J) := 0;
    pragma Loop_Invariant (X = X'Loop_Entry'Update(From .. J => 0));
  end loop;
end Zero_Range;

Attribute Update can also be used outside of assertions. It is particularly useful in expression functions. For example, the functionality in procedure Rotate_Clockwise_Z could be expressed equivalently as an expression function:

function Rotate_Clockwise_Z (P : Point_3D) return Point_3D is
  (P'Update(X => P.Y, Y => - P.X));

Because it requires copying the value of P, the type of P cannot be limited.

5.5.7 Conditional Expressions

[Ada 2012]

A conditional expression is a way to express alternative possibilities in an expression. It is like the ternary conditional expression cond ? expr1 : expr2 in C or Java, except more powerful. There are two kinds of conditional expressions in Ada:

- if-expressions are the counterpart of if-statements in expressions
- case-expressions are the counterpart of case-statements in expressions

For example, consider the variant of procedure Add_To_Total seen in Contract Cases, which saturates at a given threshold. Its postcondition can be expressed with an if-expression as follows:

procedure Add_To_Total (Incr : in Integer) with
begin
  Post => (if Total'Old + Incr < Threshold then
            Total = Total'Old + Incr
          else
            Total = Threshold);
end Add_To_Total;

Each branch of an if-expression (there may be one, two or more branches when elsif is used) can be seen as a logical implication, which explains why the above postcondition can also be written:

procedure Add_To_Total (Incr : in Integer) with
begin
  Post => (if Total'Old + Incr < Threshold then Total = Total'Old + Incr and
            (if Total'Old + Incr >= Threshold then Total = Threshold else True));
end Add_To_Total;

or equivalently (as the absence of else branch above is implicitly the same as else True):

procedure Add_To_Total (Incr : in Integer) with
begin
  Post => (if Total'Old + Incr < Threshold then Total = Total'Old + Incr else True) and
          (if Total'Old + Incr >= Threshold then Total = Threshold else True);
end Add_To_Total;

If-expressions are not necessarily of boolean type, in which case they must have an else branch that gives the value of the expression for cases not covered in previous conditions (as there is no implicit else True in such a case). For example, here is a postcondition equivalent to the above, that uses an if-expression of Integer type:

procedure Add_To_Total (Incr : in Integer) with
begin
  Post => Total = (if Total'Old + Incr < Threshold then Total'Old + Incr else Threshold);
Although case-expressions can be used to cover cases of any scalar type, they are mostly used with enumerations, and the compiler checks that all cases are disjoint and that together they cover all possible cases. For example, consider a variant of procedure Add_To_Total which takes an additional Mode global input of enumeration value Single, Double, Negate or Ignore, with the intuitive corresponding leverage effect on the addition. The postcondition of this variant can be expressed using a case-expression as follows:

```ada
procedure Add_To_Total (Incr : in Integer) with
  Post => (case Mode is
    when Single => Total = Total'Old + Incr,
    when Double => Total = Total'Old + 2 * Incr,
    when Ignore => Total = Total'Old,
    when Negate => Total = Total'Old - Incr);
```

Like if-expressions, case-expressions are not necessarily of boolean type. For example, here is a postcondition equivalent to the above, that uses a case-expression of Integer type:

```ada
procedure Add_To_Total (Incr : in Integer) with
  Post => Total = Total'Old + (case Mode is
    when Single => Incr,
    when Double => 2 * Incr,
    when Ignore => 0,
    when Negate => - Incr);
```

A last case of others can be used to denote all cases not covered by previous conditions. If-expressions and case-expressions should always be parenthesized.

### 5.5.8 Quantified Expressions

[Ada 2012]

A quantified expression is a way to express a property over a collection, either an array or a container (see Formal Containers Library):

- a universally quantified expression using for all expresses a property that holds for all elements of a collection
- an existentially quantified expression using for some expresses a property that holds for at least one element of a collection

For example, consider the procedure Increment_Array that increments each element of its array parameter X by one. Its postcondition can be expressed using a universally quantified expression as follows:

```ada
procedure Increment_Array (X : in out Integer_Array) with
  Post => (for all J in X'Range => X(J) = X'Old(J) + 1);
```

The negation of a universal property being an existential property (the opposite is true too), the postcondition above can be expressed also using an existentially quantified expression as follows:

```ada
procedure Increment_Array (X : in out Integer_Array) with
  Post => not (for some J in X'Range => X(J) /= X'Old(J) + 1);
```

At run time, a quantified expression is executed like a loop, which exits as soon as the value of the expression is known: if the property does not hold (resp. holds) for a given element of a universally (resp. existentially) quantified expression, execution of the loop does not proceed with remaining elements and returns the value False (resp. True) for the expression.
When a quantified expression is analyzed with GNATprove, it uses the logical counterpart of the quantified expression. GNATprove also checks that the expression is free from run-time errors. For this checking, GNATprove checks that the enclosed expression is free from run-time errors over the *entire range* of the quantification, not only at points that would actually be reached at run time. As an example, consider the following expression:

\[
\text{for all } I \text{ in } 1 \ldots 10 \Rightarrow 1 / (I - 3) > 0
\]

This quantified expression cannot raise a run-time error, because the enclosed expression \(1 / (I - 3) > 0\) is false for the first value of the range \(I = 1\), so the execution of the loop exits immediately with the value \(\text{False}\) for the quantified expression. GNATprove is stricter and requires the enclosed expression \(1 / (I - 3) > 0\) to be free from run-time errors over the entire range \(I \text{ in } 1 \ldots 10\) (including \(I = 3\)) so it issues a check message for a possible division by zero in this case.

Quantified expressions should always be parenthesized.

### 5.5.9 Expression Functions

[Ada 2012]

An expression function is a function whose implementation is given by a single expression. For example, the function `Increment` can be defined as an expression function as follows:

```ada
function Increment (X : Integer) return Integer is (X + 1);
end Increment;
```

For compilation and execution, this definition is equivalent to:

```ada
function Increment (X : Integer) return Integer is
begin
  return X + 1;
end Increment;
```

For GNATprove, this definition as expression function is equivalent to the same function body as above, plus a post-condition:

```ada
function Increment (X : Integer) return Integer with
  Post => Increment'Result = X + 1
is
begin
  return X + 1;
end Increment;
```

Thus, a user does not need in general to add a postcondition to an expression function, as the implicit postcondition generated by GNATprove is the most precise one. If a user adds a postcondition to an expression function, GNATprove uses this postcondition to analyze the function’s callers as well as the most precise implicit postcondition.

On the contrary, it may be useful in general to add a precondition to an expression function, to constrain the contexts in which it can be called. For example, parameter \(X\) passed to function `Increment` should be less than the maximal integer value, otherwise an overflow would occur. We can specify this property in `Increment`'s precondition as follows:

```ada
function Increment (X : Integer) return Integer is (X + 1) with
  Pre => X < Integer'Last;
end Increment;
```

Note that the contract of an expression function follows its expression.

Expression functions can be defined in package declarations, hence they are well suited for factoring out common properties that are referred to in contracts. For example, consider the procedure `Increment_Array` that increments each element of its array parameter \(X\) by one. Its precondition can be expressed using expression functions as follows:
package Increment_Utils is

  function Not_Max (X : Integer) return Boolean is (X < Integer'Last);

  function None_Max (X : Integer_Array) return Boolean is
    (for all J in X'Range => Not_Max (X(J)));

  procedure Increment_Array (X : in out Integer_Array) with
    Pre => None_Max (X);

end Increment_Utils;

Expression functions can be defined over private types, and still be used in the contracts of publicly visible subprograms of the package, by declaring the function publicly and defining it in the private part. For example:

package Increment_Utils is

  type Integer_Array is private;

  function None_Max (X : Integer_Array) return Boolean;

  procedure Increment_Array (X : in out Integer_Array) with
    Pre => None_Max (X);

private

  type Integer_Array is array (Positive range <>) of Integer;

  function Not_Max (X : Integer) return Boolean is (X < Integer'Last);

  function None_Max (X : Integer_Array) return Boolean is
    (for all J in X'Range => Not_Max (X(J)));

end Increment_Utils;

If an expression function is defined in a unit spec, GNATprove can use its implicit postcondition at every call. If an expression function is defined in a unit body, GNATprove can use its implicit postcondition at every call in the same unit, but not at calls inside other units. This is true even if the expression function is declared in the unit spec and defined in the unit body.

### 5.5.10 Ghost Code

[SPARK]

Sometimes, the variables and functions that are present in a program are not sufficient to specify intended properties and to verify these properties with GNATprove. In such a case, it is possible in SPARK to insert in the program additional code useful for specification and verification, specially identified with the aspect `Ghost` so that it can be discarded during compilation. So-called `ghost code` in SPARK are these parts of the code that are only meant for specification and verification, and have no effect on the functional behavior of the program.

Various kinds of ghost code are useful in different situations:

- **Ghost functions** are typically used to express properties used in contracts.

- **Global ghost variables** are typically used to keep track of the current state of a program, or to maintain a log of past events of some type. This information can then be referred to in contracts.
• **Local ghost variables** are typically used to hold intermediate values during computation, which can then be referred to in assertion pragmas like loop invariants.

• **Ghost types** are those types only useful for defining ghost variables.

• **Ghost procedures** can be used to factor out common treatments on ghost variables. Ghost procedures should not have non-ghost outputs, either output parameters or global outputs.

• **Ghost packages** provide a means to encapsulate all types and operations for a specific kind of ghost code.

• **Imported ghost subprograms** are used to provide placeholders for properties that are defined in a logical language, when using manual proof.

When the program is compiled with assertions (for example with switch -gnata in GNAT), ghost code is executed like normal code. Ghost code can also be selectively enabled by setting pragma `Assertion_Policy` as follows:

```plaintext
pragma Assertion_Policy (Ghost => Check);
```

GNATprove checks that ghost code cannot have an effect on the behavior of the program. GNAT compiler also performs some of these checks, although not all of them. Apart from these checks, GNATprove treats ghost code like normal code during its analyses.

### Ghost Functions

Ghost functions are useful to express properties only used in contracts, and to factor out common expressions used in contracts. For example, function `Get_Total` introduced in *State Abstraction and Functional Contracts* to retrieve the value of variable `Total` in the contract of `Add_To_Total` could be marked as a ghost function as follows:

```plaintext
function Get_Total return Integer with Ghost;
```

and still be used exactly as seen in *State Abstraction and Functional Contracts*:

```plaintext
procedure Add_To_Total (Incr : in Integer) with
  Pre => Incr >= 0 and then Get_Total in 0 .. Integer'Last - Incr,
  Post => Get_Total = Get_Total'Old + Incr;
```

The definition of `Get_Total` would be also the same:

```plaintext
Total : Integer;
function Get_Total return Integer is (Total);
```

Although it is more common to define ghost functions as *Expression Functions*, a regular function might be used too:

```plaintext
function Get_Total return Integer is
begin
  return Total;
end Get_Total;
```

In that case, GNATprove uses only the contract of `Get_Total` (either user-specified or the default one) when analyzing its callers, like for a non-ghost regular function. (The same exception applies as for regular functions, when GNATprove can analyze a subprogram in the context of its callers, as described in *Contextual Analysis of Subprograms Without Contracts*.)

All functions which are only used in specification can be marked as ghost, but most don’t need to. However, there are cases where marking a specification-only function as ghost really brings something. First, as ghost entities are not allowed to interfere with normal code, marking a function as ghost avoids having to break state abstraction for the
purpose of specification. For example, marking `Get_Total` as ghost will prevent users of the package `Account` from accessing the value of `Total` from non-ghost code.

Then, in the usual context where ghost code is not kept in the final executable, the user is given more freedom to use in ghost code constructs that are less efficient than in normal code, which may be useful to express rich properties. For example, the ghost functions defined in the `Formal Containers Library` in GNAT typically copy the entire content of the argument container, which would not be acceptable for non-ghost functions.

**Ghost Variables**

Ghost variables are useful to keep track of local or global information during the computation, which can then be referred to in contracts or assertion pragmas.

**Case 1: Keeping Intermediate Values**

Local ghost variables are commonly used to keep intermediate values. For example, we can define a local ghost variable `Init_Total` to hold the initial value of variable `Total` in procedure `Add_To_Total`, which allows checking the relation between the initial and final values of `Total` in an assertion:

```plaintext
procedure Add_To_Total (Incr : in Integer) is
  Init_Total : Integer := Total with Ghost;
begin
  Total := Total + Incr;
  pragma Assert (Total = Init_Total + Incr);
end Add_To_Total;
```

**Case 2: Keeping Memory of Previous State**

Global ghost variables are commonly used to memorize the value of a previous state. For example, we can define a global ghost variable `Last_Incr` to hold the previous value passed in argument when calling procedure `Add_To_Total`, which allows checking in its precondition that the sequence of values passed in argument is non-decreasing:

```plaintext
Last_Incr : Integer := Integer'First with Ghost;

procedure Add_To_Total (Incr : in Integer) with
  Pre => Incr >= Last_Incr;

procedure Add_To_Total (Incr : in Integer) is
begin
  Total := Total + Incr;
  Last_Incr := Incr;
end Add_To_Total;
```

**Case 3: Logging Previous Events**

Going beyond the previous case, global ghost variables can be used to store a complete log of events. For example, we can define global ghost variables `Log` and `Log_Size` to hold the sequence of values passed in argument to procedure `Add_To_Total`, as in `State Abstraction`:
Log : Integer_Array with Ghost;
Log_Size : Natural with Ghost;

procedure Add_To_Total (Incr : in Integer) with
  Post => Log_Size = Log_Size'Old + 1 and Log = Log'Old'Update (Log_Size => Incr);

procedure Add_To_Total (Incr : in Integer) is
begin
  Total := Total + Incr;
  Log_Size := Log_Size + 1;
  Log (Log_Size) := Incr;
end Add_To_Total;

The postcondition of Add_To_Total above expresses that Log_Size is incremented by one at each call, and that the current value of parameter Incr is appended to Log at each call (using Attribute Old and Attribute Update).

**Case 4: Expressing Existentially Quantified Properties**

In SPARK, universal quantification is only allowed in restricted cases (over integer ranges and over the content of a container). To express the existence of a particular object, it is sometimes easier to simply provide it. This can be done using a global ghost variable. This can be used in particular to split the specification of a complex procedure into smaller parts:

X_Interm : T with Ghost;

procedure Do_Two_Thing (X : in out T) with
  Post => First_Thing_Done (X'Old, X_Interm) and then
           Second_Thing_Done (X_Interm, X)
is
begin
  X_Init : constant T := X with Ghost;
  Do_Something (X);
  pragma Assert (First_Thing_Done (X_Init, X));
  X_Interm := X;
  Do_Something_Else (X);
  pragma Assert (Second_Thing_Done (X_Interm, X));
end Do_Two_Things;

More complicated uses can also be envisioned, up to constructing ghost data structures reflecting complex properties. For example, we can express that two arrays are a permutation of each other by constructing a permutation from one to the other:

Perm : Permutation with Ghost;

procedure Permutation_Sort (A : Nat_Array) with
  Post => A = Apply_Perm (Perm, A'Old)
is
begin
  -- Initialize Perm with the identity
  Perm := Identity_Perms;

  for Current in A'First .. A'Last - 1 loop
    Smallest := Index_Of_Minimum_Value (A, Current, A'Last);
    if Smallest /= Current then
      Swap (A, Current, Smallest);
  end for;
end Permutation_Sort;
-- Update Perm each time we permute two elements in A
Permute (Perm, Current, Smallest);
end if;
end loop;
end Permutation_Sort;

Ghost Types

Ghost types can only be used to define ghost variables. For example, we can define ghost types Log_Type and Log_Size_Type that specialize the types Integer_Array and Natural for ghost variables:

```plaintext
subtype Log_Type is Integer_Array with Ghost;
subtype Log_Size_Type is Natural with Ghost;
Log : Log_Type with Ghost;
Log_Size : Log_Size_Type with Ghost;
```

Ghost Procedures

Ghost procedures are useful to factor out common treatments on ghost variables. For example, we can define a ghost procedure Append_To_Log to append a value to the log as seen previously.

```plaintext
procedure Append_To_Log (Incr : in Integer) with
  Ghost,
  Post => Log_Size = Log_Size'Old + 1 and Log = Log'Old'Update (Log_Size => Incr);
procedure Append_To_Log (Incr : in Integer) is
begin
  Log_Size := Log_Size + 1;
  Log (Log_Size) := Incr;
end Append_To_Log;
```

Then, this procedure can be called in Add_To_Total as follows:

```plaintext
procedure Add_To_Total (Incr : in Integer) is
begin
  Total := Total + Incr;
  Append_To_Log (Incr);
end Add_To_Total;
```

Ghost Packages

Ghost packages are useful to encapsulate all types and operations for a specific kind of ghost code. For example, we can define a ghost package Logging to deal with all logging operations on package Account:

```plaintext
package Logging with
  Ghost
is
  Log : Integer_Array;
```
Log_Size : Natural;

procedure Append_To_Log (Incr : in Integer) with
  Post => Log_Size = Log_Size'Old + 1 and Log = Log'Old'Update (Log_Size => Incr);
...
end Logging;

The implementation of package Logging is the same as if it was not a ghost package. In particular, a Ghost aspect is implicitly added to all declarations in Logging, so it is not necessary to specify it explicitly. Logging can be defined either as a local ghost package or as a separate unit. In the latter case, unit Account needs to reference unit Logging in a with-clause like for a non-ghost unit:

with Logging;

package Account is
  ...
end Account;

Imported Ghost Subprograms

When using manual proof (see GNATprove and Manual Proof), it may be more convenient to define some properties in the logical language of the prover rather than in SPARK. In that case, ghost functions might be marked as imported, so that no implementation is needed. For example, the ghost procedure Append_To_Log seen previously may be defined equivalently as a ghost imported function as follows:

function Append_To_Log (Log : Log_type; Incr : in Integer) return Log_Type with
  Ghost,
  Import;

where Log_Type is an Ada type used also as placeholder for a type in the logical language of the prover. To avoid any inconsistency between the interpretations of Log_Type in GNATprove and in the manual prover, it is preferable in such a case to mark the definition of Log_Type as not in SPARK, so that GNATprove does not make any assumptions on its content. This can be achieved by defining Log_Type as a private type and marking the private part of the enclosing package as not in SPARK:

package Logging with
  SPARK_Mode,
  Ghost
is
  type Log_Type is private;

  function Append_To_Log (Log : Log_type; Incr : in Integer) return Log_Type with
    Import;
...
private
  pragma SPARK_Mode (Off);

  type Log_Type is new Integer; -- Any definition is fine here
end Logging;

A ghost imported subprogram cannot be executed, so calls to Append_To_Log above should not be enabled during
compilation, otherwise a compilation error is issued. Note also that GNATprove will not attempt proving the contract of a ghost imported subprogram, as it does not have its body.

**Ghost Models**

When specifying a program, it is common to use a model, that is, an alternative, simpler view of a part of the program. As they are only used in annotations, models can be computed using ghost code.

**Models of Control Flow**

Global variables can be used to enforce properties over call chains in the program. For example, we may want to express that Total cannot be incremented twice in a row without registering the transaction in between. This can be done by introducing a ghost global variable Last_Transaction_Registered, used to encode whether Register_Transaction was called since the last call to Add_To_Total:

```ada
Last_Transaction_Registered : Boolean := True with Ghost;

procedure Add_To_Total (Incr : Integer) with
  Pre => Last_Transaction_Registered,
  Post => not Last_Transaction_Registered;

procedure Register_Transaction with
  Post => Last_Transaction_Registered;
```

The value of Last_Transaction_Registered should also be updated in the body of Add_To_Total and Register_Transaction to reflect their contracts:

```ada
procedure Add_To_Total (Incr : in Integer) is
begin
  Total := Total + Incr;
  Last_Transaction_Registered := False;
end Add_To_Total;
```

More generally, the expected control flow of a program can be modeled using an automaton. We can take as an example a mailbox containing only one message. The expected way Receive and Send should be interleaved can be expressed as a two state automaton. The mailbox can either be full, in which case Receive can be called but not Send, or it can be empty, in which case it is Send that can be called and not Receive. To express this property, we can define a ghost global variable of a ghost enumeration type to hold the state of the automaton:

```ada
type Mailbox_Status_Kind is (Empty, Full) with Ghost;
Mailbox_Status : Mailbox_Status_Kind := Empty with Ghost;

procedure Receive (X : out Message) with
  Pre => Mailbox_Status = Full,
  Post => Mailbox_Status = Empty;

procedure Send (X : Message) with
  Pre => Mailbox_Status = Empty,
  Post => Mailbox_Status = Full;
```

Like before, Receive and Send should update Mailbox_Status in their bodies. Note that all the transitions of the automaton need not be specified, only the part which are relevant to the properties we want to express.

If the program also has some regular state, an invariant can be used to link the value of this state to the value of the ghost state of the automaton. For example, in our mailbox, we may have a regular variable Message_Content
holding the content of the current message, which is only known to be valid after a call to Send. We can introduce a
ghost function linking the value of Message_Content to the value of Mailbox_Status, so that we can ensure
that Message_Content is always valid when accessed from Receive:

```plaintext
function Invariant return Boolean is
  (if Mailbox_Status = Full then Valid (Message_Content))
with Ghost;

procedure Receive (X : out Message) with
  Pre => Invariant and then Mailbox_Status = Full,
      Post => Invariant and then Mailbox_Status = Empty
            and then Valid (X)
is
  X := Message_Content;
end Receive;
```

Models of Data Structures

For specifying programs that use complex data structures (doubly-linked lists, maps...), it can be useful to supply
a model for the data structure. A model is an alternative, simpler view of the data-structure which allows to write
properties more easily. For example, a ring buffer, or a doubly-linked list, can be modeled using an array containing
the elements from the buffer or the list in the right order. Typically, though simpler to reason with, the model is less
efficient than the regular data structure. For example, inserting an element at the beginning of a doubly-linked list or at
the beginning of a ring buffer can be done in constant time whereas inserting an element at the beginning of an array
requires to slide all the elements to the right. As a result, models of data structures are usually supplied using ghost
code. As an example, the package Ring_Buffer offers an implementation of a single instance ring buffer. A ghost
variable Buffer_Model is used to write the specification of the Enqueue procedure:

```plaintext
package Ring_Buffer is
  function Get_Model return Nat_Array with Ghost;

  procedure Enqueue (E : Natural) with
    Post => Get_Model = E & Get_Model'Old (1 .. Max - 1);
private
  Buffer_Content : Nat_Array;
  Buffer_Top     : Natural;
  Buffer_Model   : Nat_Array with Ghost;

  function Get_Model return Nat_Array is (Buffer_Model);
end Ring_Buffer;
```

Then, just like for models of control flow, an invariant should be supplied to link the regular data structure to its model:

```plaintext
package Ring_Buffer is
  function Get_Model return Nat_Array with Ghost;
  function Invariant return Boolean with Ghost;

  procedure Enqueue (E : Natural) with
    Pre => Invariant,
    Post => Invariant and then Get_Model = E & Get_Model'Old (1 .. Max - 1);
private
  Buffer_Content : Nat_Array;
  Buffer_Top     : Natural;
  Buffer_Model   : Nat_Array with Ghost;

  function Get_Model return Nat_Array is (Buffer_Model);
end Ring_Buffer;
```
If a data structure type is defined, a ghost function can be provided to compute a model for objects of the data structure type, and the invariant can be stated as a postcondition of this function:

```ada
package Ring_Buffer is
type Buffer_Type is private;
subtype Model_Type is Nat_Array with Ghost;

function Invariant (X : Buffer_Type; M : Model_Type) return Boolean with Ghost;
function Get_Model (X : Buffer_Type) return Model_Type with Ghost,
    Post => Invariant (X, Get_Model'Result);
procedure Enqueue (X : in out Buffer_Type; E : Natural) with Post => Get_Model (X) = E & Get_Model (X)'Old (1 .. Max - 1);
private
    type Buffer_Type is record
        Content : Nat_Array;
        Top : Natural;
    end record;
end Ring_Buffer;
```

More complex examples of models of data structure can be found in the Formal Containers Library.

**Removal of Ghost Code**

By default, GNAT completely discards ghost code during compilation, so that no ghost code is present in the object code or the executable. This ensures that, even if parts of the ghost could have side-effects when executed (writing to variables, performing system calls, raising exceptions, etc.), by default the compiler ensures that it cannot have any effect on the behavior of the program.

This is also essential in domains submitted to certification where all instructions in the object code should be traceable to source code and requirements, and where testing should ensure coverage of the object code. As ghost code is not present in the object code, there is no additional cost for maintaining its traceability and ensuring its coverage by tests.

GNAT provides an easy means to check that no ignored ghost code is present in a given object code or executable, which relies on the property that, by definition, each ghost declaration or ghost statement mentions at least one ghost entity. GNAT prefixes all names of such ignored ghost entities in the object code with the string __ghost__(except for names of ghost compilation units). The initial triple underscore ensures that this substring cannot appear anywhere in the name of non-ghost entities or ghost entities that are not ignored. Thus, one only needs to check that the substring __ghost__ does not appear in the list of names from the object code or executable.

On Unix-like platforms, this can be done by checking that the following command does not output anything:

```
nm <object files or executable> | grep __ghost__
```

The same can be done to check that a ghost compilation unit called my_unit (whatever the capitalization) is not included at all (entities in that unit would have been detected by the previous check) in the object code or executable. For example on Unix-like platforms:

```
nm <object files or executable> | grep my_unit
```
5.6 Assertion Pragmas

SPARK contains features for directing formal verification with GNATprove. These features may also be used by other tools, in particular the GNAT compiler. Assertion pragmas are refinements of pragma `Assert` defined in Ada. For all assertion pragmas, an exception `Assertion_Error` is raised at run time when the property asserted does not hold, if the program was compiled with assertions. The real difference between assertion pragmas is how they are used by GNATprove during proof.

5.6.1 Pragma Assert

[Ada 2005]

Pragma `Assert` is the simplest assertion pragma. GNATprove checks that the property asserted holds, and uses the information that it holds for analyzing code that follows. For example, consider two assertions of the same property \( X > 0 \) in procedure `Assert_Twice`:

```ada
procedure Assert_Twice (X : Integer) with
begin
pragma Assert (X > 0);
pragma Assert (X > 0);
end Assert_Twice;
```

As expected, the first assertion on line 5 is not provable in absence of a suitable precondition for `Assert_Twice`, but GNATprove proves that it holds the second time the property is asserted on line 6:

```
assert_twice.adb:5:19: medium: assertion might fail, cannot prove X > 0 [possible explanation: subprogram at line 1 should mention X in a precondition]
assert_twice.adb:6:19: info: assertion proved
```

GNATprove considers that an execution of `Assert_Twice` with \( X \leq 0 \) stops at the first assertion that fails. Thus \( X > 0 \) when execution reaches the second assertion. This is true if assertions are executed at run time, but not if assertions are discarded during compilation. In the latter case, unproved assertions should be inspected carefully to ensure that the property asserted will indeed hold at run time. This is true of all assertion pragmas, which GNATprove analyzes like pragma `Assert` in that respect.

5.6.2 Pragma Assertion_Policy

[Ada 2005/Ada 2012]

Assertions can be enabled either globally or locally. Here, `assertions` denote either `Assertion Pragmas` of all kinds (among which `Pragma Assert`) or functional contracts of all kinds (among which `Preconditions` and `Postconditions`).

By default, assertions are ignored in compilation, and can be enabled globally by using the compilation switch `-gnata`. They can be enabled locally by using pragma `Assertion_Policy` in the program, or globally if the pragma is put in a configuration file. They can be enabled for all kinds of assertions or specific ones only by using the version of pragma `Assertion_Policy` that takes named associations which was introduced in Ada 2012.

When used with the standard policies `Check` (for enabling assertions) or `Ignore` (for ignoring assertions), pragma `Assertion_Policy` has no effect on GNATprove. GNATprove takes all assertions into account, whatever the assertion policy in effect at the point of the assertion. For example, consider a code with some assertions enabled and some ignored:
Although the postcondition and the second assertion are not executed at run time, GNATprove analyzes them and issues corresponding messages:

On the contrary, when used with the GNAT-specific policy Disable, pragma Assertion_Policy causes the corresponding assertions to be skipped both during execution and analysis with GNATprove. For example, consider the same code as above where policy Ignore is replaced with policy Disable:

On this program, GNATprove does not analyze the postcondition and the second assertion, and it does not issue corresponding messages:

The policy of Disable should thus be reserved for assertions that are not compilable, typically because a given build environment does not define the necessary entities.
5.6.3 Loop Invariants

Pragma *Loop_Invariant* is a special kind of assertion used in loops. GNATprove performs two checks that ensure that the property asserted holds at each iteration of the loop:

1. *loop invariant initialization*: GNATprove checks that the property asserted holds during the first iteration of the loop.

2. *loop invariant preservation*: GNATprove checks that the property asserted holds during an arbitrary iteration of the loop, assuming that it held in the previous iteration.

Each of these properties can be independently true or false. For example, in the following loop, the loop invariant is false during the first iteration and true in all remaining iterations:

```ada
6 Prop := False;
7 for J in 1 .. 10 loop
8   pragma Loop_Invariant (Prop);
9   Prop := True;
10 end loop;
```

Thus, GNATprove checks that property 2 holds but not property 1:

```
simple_loops.adb:8:30: info: loop invariant preservation proved
simple_loops.adb:8:30: medium: loop invariant might fail in first iteration, cannot prove Prop (e.g. when Prop = False)
```

Conversely, in the following loop, the loop invariant is true during the first iteration and false in all remaining iterations:

```ada
12 Prop := True;
13 for J in 1 .. 10 loop
14   pragma Loop_Invariant (Prop);
15   Prop := False;
16 end loop;
```

Thus, GNATprove checks that property 1 holds but not property 2:

```
simple_loops.adb:14:30: info: loop invariant initialization proved
simple_loops.adb:14:30: medium: loop invariant might fail after first iteration, cannot prove Prop (e.g. when Prop = False)
```

The following loop shows a case where the loop invariant holds both during the first iteration and all remaining iterations:

```ada
18 Prop := True;
19 for J in 1 .. 10 loop
20   pragma Loop_Invariant (Prop);
21   Prop := Prop;
22 end loop;
```

GNATprove checks here that both properties 1 and 2 hold:

```
simple_loops.adb:20:30: info: loop invariant initialization proved
simple_loops.adb:20:30: info: loop invariant preservation proved
```

In general, it is not sufficient that a loop invariant is true for GNATprove to prove it. The loop invariant should also be *inductive*: it should be precise enough that GNATprove can check loop invariant preservation by assuming *only*
that the loop invariant held during the last iteration. For example, the following loop is the same as the previous one, except the loop invariant is true but not inductive:

```plaintext
Prop := True;
for J in 1 .. 10 loop
  pragma Loop_Invariant (if J > 1 then Prop);
  Prop := Prop;
end loop;
```

GNATprove cannot check property 2 on that loop:

```plaintext
simple_loops.adb:26:30: info: loop invariant initialization proved
simple_loops.adb:26:44: medium: loop invariant might fail after first iteration,
  cannot prove Prop (e.g. when Prop = False)
```

Note that using CodePeer static analysis allows here to fully prove the loop invariant, which is possible because CodePeer generates its own sound approximation of loop invariants (see Using CodePeer Static Analysis for details):

```plaintext
simple_loops_cdp.adb:26:30: info: loop invariant proved
```

Note also that not using an assertion (Pragma Assert) instead of a loop invariant also allows here to fully prove the corresponding property, by relying on Automatic Unrolling of Simple For-Loops:

```plaintext
simple_loops_unroll.adb:26:22: info: assertion proved
```

Returning to the case where neither automatic loop unrolling nor CodePeer are used, the reasoning of GNATprove for checking property 2 in that case can be summarized as follows:

- Let’s take iteration K of the loop, where K > 1 (not the first iteration).
- Let’s assume that the loop invariant held during iteration K-1, so we know that if K-1 > 1 then Prop holds.
- The previous assumption can be rewritten: if K > 2 then Prop.
- But all we know is that K > 1, so we cannot deduce Prop.

See How to Write Loop Invariants for further guidelines.

Pragma Loop_Invariant may appear anywhere at the top level of a loop: it is usually added at the start of the loop, but it may be more convenient in some cases to add it at the end of the loop, or in the middle of the loop, in cases where this simplifies the asserted property. In all cases, GNATprove checks loop invariant preservation by reasoning on the virtual loop that starts and ends at the loop invariant.

It is possible to use multiple loop invariants, which should be grouped together without intervening statements or declarations. The resulting complete loop invariant is the conjunction of individual ones. The benefits of writing multiple loop invariants instead of a conjunction can be improved readability and better provability (because GNATprove checks each pragma Loop_Invariant separately).

Finally, Attribute Loop_Entry and Attribute Update can be very useful to express complex loop invariants.

**Note:** Users that are already familiar with the notion of loop invariant in other proof systems should be aware that loop invariants in SPARK are slightly different from the usual ones. In SPARK, a loop invariant must hold when execution reaches the corresponding pragma inside the loop. Hence, it needs not hold when the loop is never entered, or when exiting the loop.
5.6.4 Loop Variants

Pragma Loop_Variant is a special kind of assertion used in loops. GNATprove checks that the given scalar value decreases (or increases) at each iteration of the loop. Because a scalar value is always bounded by its type in Ada, it cannot decrease (or increase) at each iteration an infinite number of times, thus one of two outcomes is possible:

1. the loop exits, or
2. a run-time error occurs.

Therefore, it is possible to prove the termination of loops in SPARK programs by proving both a loop variant for each plain-loop or while-loop (for-loops always terminate in Ada) and the absence of run-time errors.

For example, the while-loops in procedure Terminating_Loops compute the value of $X - X \text{ mod } 3$ (or equivalently $X / 3 \times 3$) in variable $Y$:

```ada
procedure Terminating_Loops (X : Natural) with SPARK_Mode is
    Y : Natural;
begin
    Y := 0;
    while X - Y >= 3 loop
        Y := Y + 3;
        pragma Loop_Variant (Increases => Y);
    end loop;
    Y := 0;
    while X - Y >= 3 loop
        Y := Y + 3;
        pragma Loop_Variant (Decreases => X - Y);
    end loop;
end Terminating_Loops;
```

GNATprove is able to prove both loop variants, as well as absence of run-time errors in the subprogram, hence that loops terminate:

```
terminating_loops.adb:4:04: info: initialization of "Y" proved
terminating_loops.adb:7:12: info: overflow check proved
terminating_loops.adb:8:14: info: overflow check proved
terminating_loops.adb:9:07: info: loop variant proved
terminating_loops.adb:13:12: info: overflow check proved
terminating_loops.adb:14:14: info: overflow check proved
terminating_loops.adb:15:07: info: loop variant proved
terminating_loops.adb:15:43: info: overflow check proved
```

Pragma Loop_Variant may appear anywhere a loop invariant appears. It is also possible to use multiple loop variants, which should be grouped together with loop invariants. A loop variant may be more complex than a single decreasing (or increasing) value, and be given instead by a list of either decreasing or increasing values (possibly a mix of both). In that case, the order of the list defines the lexicographic order of progress. See SPARK RM 5.5.3 for details.

5.6.5 Pragma Assume

[SPARK]
Pragma Assume is a variant of Pragma Assert that does not require GNATprove to check that the property holds. This is used to convey trustworthy information to GNATprove, in particular properties about external objects that GNATprove has no control upon. GNATprove uses the information that the assumed property holds for analyzing code that follows. For example, consider an assumption of the property \( X > 0 \) in procedure Assume_Then_Assert, followed by an assertion of the same property:

```ada
procedure Assume_Then_Assert (X : Integer) with
  SPARK_Mode
is
begin
  pragma Assume (X > 0);
  pragma Assert (X > 0);
end Assume_Then_Assert;
```

As expected, GNATprove does not check the property on line 5, but used it to prove that the assertion holds on line 6:

```
assume_then_assert.adb:6:19: info: assertion proved
```

GNATprove considers that an execution of Assume_Then_Assert with \( X \leq 0 \) stops at the assumption on line 5, and it does not issue a message in that case because the user explicitly indicated that this case is not possible. Thus \( X > 0 \) when execution reaches the assertion on line 6. This is true if assertions (of which assumptions are a special kind) are executed at run time, but not if assertions are discarded during compilation. In the latter case, assumptions should be inspected carefully to ensure that the property assumed will indeed hold at run time. This inspection may be facilitated by passing a justification string as the second argument to pragma Assume.

### 5.6.6 Pragma Assert_And_Cut

[SPARK]

Pragma Assert_And_Cut is a variant of Pragma Assert that allows hiding some information to GNATprove. GNATprove checks that the property asserted holds, and uses only the information that it holds for analyzing code that follows. For example, consider two assertions of the same property \( X = 1 \) in procedure Forgetful_Assert, separated by a pragma Assert_And_Cut:

```ada
procedure Forgetful_Assert (X : out Integer) with
  SPARK_Mode
is
begin
  X := 1;
  pragma Assert (X = 1);
  pragma Assert_And_Cut (X > 0);
  pragma Assert (X > 0);
  pragma Assert (X = 1);
end Forgetful_Assert;
```

GNATprove proves that the assertion on line 7 holds, but it cannot prove that the same assertion on line 12 holds:

```
forgetful_assert.adb:1:29: info: initialization of "X" proved
forgetful_assert.adb:7:19: info: assertion proved
forgetful_assert.adb:9:27: info: assertion proved
forgetful_assert.adb:11:19: info: assertion proved
forgetful_assert.adb:12:19: medium: assertion might fail, cannot prove X = 1 (e.g. when X = 2)
```
GNATprove forgets the exact value of $X$ after line 9. All it knows is the information given in pragma `Assert_And_Cut`, here that $X > 0$. And indeed GNATprove proves that such an assertion holds on line 11. But it cannot prove the assertion on line 12, and the counterexample displayed mentions a possible value of 2 for $X$, showing indeed that GNATprove forgot its value of 1.

Pragma `Assert_And_Cut` may be useful in two cases:

1. When the automatic provers are overwhelmed with information from the context, pragma `Assert_And_Cut` may be used to simplify this context, thus leading to more automatic proofs.

2. When GNATprove is proving checks for each path through the subprogram (see switch `--proof` in `Running GNATprove from the Command Line`), and the number of paths is very large, pragma `Assert_And_Cut` may be used to reduce the number of paths, thus leading to faster automatic proofs.

For example, consider procedure $P$ below, where all that is needed to prove that the code using $X$ is free from run-time errors is that $X$ is positive. Let's assume that we are running GNATprove with switch `--proof=per_path` so that a formula is generated for each execution path. Without the pragma, GNATprove considers all execution paths through $P$, which may be many. With the pragma, GNATprove only considers the paths from the start of the procedure to the pragma, and the paths from the pragma to the end of the procedure, hence many fewer paths.

```plaintext
procedure P is
  X : Integer;
begin
  -- complex computation that sets X
  pragma Assert_And_Cut (X > 0);
  -- complex computation that uses X
end P;
```

## 5.7 Overflow Modes

Annotations such as preconditions, postconditions, assertions, loop invariants, are analyzed by GNATprove with the exact same meaning that they have during execution. In particular, evaluating the expressions in an annotation may raise a run-time error, in which case GNATprove will attempt to prove that this error cannot occur, and report a warning otherwise.

Integer overflows are a kind of run-time error that occurs when the result of an arithmetic computation does not fit in the bounds of the machine type used to hold the result. In some cases, it is convenient to express properties in annotations as they would be expressed in mathematics, where quantities are unbounded, for example:

```plaintext
function Add (X, Y : Integer) return Integer with
  Pre => X + Y in Integer,
  Post => Add'Result = X + Y;
```

The precondition of `Add` states that the result of adding its two parameters should fit in type `Integer`. In the default mode, evaluating this expression will fail an overflow check, because the result of $X + Y$ is stored in a temporary of type `Integer`. If the compilation switch `--gnato13` is used, then annotations are compiled specially, so that arithmetic operations use unbounded intermediate results. In this mode, GNATprove does not generate a check for the addition of $X$ and $Y$ in the precondition of `Add`, as there is no possible overflow here.

There are three overflow modes:

- Use base type for intermediate operations (STRICT): in this mode, all intermediate results for predefined arithmetic operators are computed using the base type, and the result must be in range of the base type.

- Most intermediate overflows avoided (MINIMIZED): in this mode, the compiler attempts to avoid intermediate overflows by using a larger integer type, typically `Long_Long_Integer`, as the type in which arithmetic is
performed for predefined arithmetic operators.

- All intermediate overflows avoided (ELIMINATED): in this mode, the compiler avoids all intermediate overflows by using arbitrary precision arithmetic as required.

The desired mode for handling intermediate overflow can be specified using either the Overflow_Mode pragma or an equivalent compiler switch. The pragma has the form:

```
pragma Overflow_Mode ([General =>] MODE [, [Assertions =>] MODE]);
```

where MODE is one of

- STRICT: intermediate overflows checked (using base type)
- MINIMIZED: minimize intermediate overflows
- ELIMINATED: eliminate intermediate overflows

For example:

```
pragma Overflow_Mode (General => Strict, Assertions => Eliminated);
```

specifies that general expressions outside assertions be evaluated in the usual strict mode, and expressions within assertions be evaluated in “eliminate intermediate overflows” mode. Currently, GNATprove only supports pragma Overflow_Mode being specified as a configuration pragma, either in a configuration pragma file or directly in a unit.

Additionally, a compiler switch `-gnato??` can be used to control the checking mode default. Here `?` is one of the digits 1 through 3:

1. use base type for intermediate operations (STRICT)
2. minimize intermediate overflows (MINIMIZED)
3. eliminate intermediate overflows (ELIMINATED)

The switch `-gnato13`, like the Overflow_Mode pragma above, specifies that general expressions outside assertions be evaluated in the usual strict mode, and expressions within assertions be evaluated in “eliminate intermediate overflows” mode.

Note that these modes apply only to the evaluation of predefined arithmetic, membership, and comparison operators for signed integer arithmetic.

For further details of the meaning of these modes, and for further information about the treatment of overflows for fixed-point and floating-point arithmetic please refer to the “Overflow Check Handling in GNAT” appendix in the GNAT User’s Guide.

5.8 Object Oriented Programming and Liskov Substitution Principle

SPARK supports safe Object Oriented Programming by checking behavioral subtyping between parent types and derived types, a.k.a. Liskov Substitution Principle: every overriding operation of the derived type should behave so that it can be substituted for the corresponding overridden operation of the parent type anywhere.

5.8.1 Class-Wide Subprogram Contracts

[Ada 2012]

Specific Subprogram Contracts are required on operations of tagged types, so that GNATprove can check Liskov Substitution Principle on every overriding operation:
• The **class-wide precondition** introduced by aspect Pre'Class is similar to the normal precondition.

• The **class-wide postcondition** introduced by aspect Post'Class is similar to the normal postcondition.

Although these contracts are defined in Ada 2012, they have a stricter meaning in SPARK for checking Liskov Substitution Principle:

• The class-wide precondition of an overriding operation should be weaker (more permissive) than the class-wide precondition of the corresponding overridden operation.

• The class-wide postcondition of an overriding operation should be stronger (more restrictive) than the class-wide postcondition of the corresponding overridden operation.

For example, suppose that the Logging unit introduced in *Ghost Packages* defines a tagged type Log_Type for logs, with corresponding operations:

```ada
package Logging with
  SPARK_Mode
is
  Max_Count : constant := 10_000;

  type Log_Count is range 0 .. Max_Count;

  type Log_Type is tagged private;

  function Log_Size (Log : Log_Type) return Log_Count;

  procedure Init_Log (Log : out Log_Type) with
    Post'Class => Log.Log_Size = 0;

  procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
    Pre'Class => Log.Log_Size < Max_Count,
    Post'Class => Log.Log_Size = Log.Log_Size'Old + 1;

private

  subtype Log_Index is Log_Count range 1 .. Max_Count;
  type Integer_Array is array (Log_Index) of Integer;

  type Log_Type is tagged record
    Log_Data : Integer_Array;
    Log_Size : Log_Count;
  end record;

  function Log_Size (Log : Log_Type) return Log_Count is (Log.Log_Size);

end Logging;
```

and that this type is derived in RangeLogging.Log_Type which additionally keeps track of the minimum and maximum values in the log, so that they can be accessed in constant time:

```ada
with Logging; use type Logging.Log_Count;

package Range_Logging with
  SPARK_Mode
is
  type Log_Type is new Logging.Log_Type with private;

  not overriding
  function Log_Min (Log : Log_Type) return Integer;
```
not overriding

function Log_Max (Log : Log_Type) return Integer;

overriding

procedure Init_Log (Log : out Log_Type) with
  Post'Class => Log.Log_Size = 0 and
  Log.Log_Min = Integer'Last and
  Log.Log_Max = Integer'First;

overriding

procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
  Pre'Class => Log.Log_Size < Logging.Max_Count,
  Post'Class => Log.Log_Size = Log.Log_Size'Old + 1 and
  Log.Log_Min = Integer'Min (Log.Log_Min'Old, Incr) and
  Log.Log_Max = Integer'Max (Log.Log_Max'Old, Incr);

private

type Log_Type is new Logging.Log_Type with record
  Min_Entry : Integer;
  Max_Entry : Integer;
end record;

function Log_Min (Log : Log_Type) return Integer is (Log.Min_Entry);
function Log_Max (Log : Log_Type) return Integer is (Log.Max_Entry);

end Range_Logging;

GNATprove proves that the contracts on Logging.Append_To_Log and its overriding Range_Logging.
Append_To_Log respect the Liskov Substitution Principle:

Units Logging and Range_Logging need not be implemented, or available, or in SPARK. It is sufficient that
the specification of Logging and Range_Logging are in SPARK for this checking. Here, the postcondition of
Range_Logging.Append_To_Log is strictly stronger than the postcondition of Logging.Append_To_Log,
as it also specifies the new expected value of the minimum and maximum values. The preconditions of both procedures
are exactly the same, which is the most common case, but in other cases it might be useful to be more permissive in
the overriding operation’s precondition. For example, Range_Logging.Append_To_Log could allocate dynam-
ically additional memory for storing an unbounded number of events, instead of being limited to Max_Count events
like Logging.Append_To_Log, in which case its precondition would be simply True (the default precondition).

A derived type may inherit both from a parent type and from one or more interfaces, which only provide abstract
operations and no components. GNATprove checks Liskov Substitution Principle on every overriding operation, both
when the overridden operation is inherited from the parent type and when it is inherited from an interface.

GNATprove separately checks that a subprogram implements its class-wide contract, like for a specific contract.

5.8.2 Mixing Class-Wide and Specific Subprogram Contracts

[Ada 2012]
It is possible to specify both a specific contract and a class-wide contract on a subprogram, in order to use a more precise contract (the specific one) for non-dispatching calls and a contract compatible with the Liskov Substitution Principle (the class-wide contract) for dispatching calls. In that case, GNATprove checks that:

- The specific precondition is weaker (more permissive) than the class-wide precondition.
- The specific postcondition is stronger (more restrictive) than the class-wide postcondition.

For example, Logging.Append_To_Log could set a boolean flag Special_Value_Logged when some Special_Value is appended to the log, and express this property in its specific postcondition so that it is available for analyzing non-dispatching calls to the procedure:

```ada
procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
  Pre'Class => Log.Log_Size < Max_Count,
  Post'Class => Log.Log_Size = Log.Log_Size'Old + 1,
  Post => Log.Log_Size = Log.Log_Size'Old + 1 and
    (if Incr = Special_Value then Special_Value_Logged = True);
```

This additional postcondition would play no role in dispatching calls, thus it is not involved in checking the Liskov Substitution Principle. Note that the absence of specific precondition on procedure Append_To_Log does not mean that the default precondition of True is used: as a class-wide precondition is specified on procedure Append_To_Log, it is also used as specific precondition. Similarly, if a procedure has a class-wide contract and a specific precondition, but no specific postcondition, then the class-wide postcondition is also used as specific postcondition.

When both a specific contract and a class-wide contract are specified on a subprogram, GNATprove only checks that the subprogram implements its specific (more precise) contract.

### 5.8.3 Dispatching Calls and Controlling Operands

[Ada 2012]

In a dispatching call, the controlling operand is the parameter of class-wide type whose dynamic type determinates the actual subprogram called. The dynamic type of this controlling operand may be any type derived from the specific type corresponding to the class-wide type of the parameter (the specific type is T when the class-wide type is T'Class). Thus, in general it is not possible to know in advance which subprograms may be called in a dispatching call, when separately analyzing a unit.

In SPARK, there is no need to know all possible subprograms called in order to analyze a dispatching call, which makes it possible for GNATprove to perform this analysis without knowledge of the whole program. As SPARK enforces Liskov Substitution Principle, the class-wide contract of an overriding operation is always less restrictive than the class-wide contract of the corresponding overridden operation. Thus, GNATprove uses the class-wide contract of the operation for the specific type of controlling operand to analyze a dispatching call.

For example, suppose a global variable The_Log of class-wide type defines the log that should be used in the program:

```ada
The_Log : Logging.Log_Type'Class := ...
```

The call to Append_To_Log in procedure Add_To_Total may dynamically call either Logging.Append_To_Log or Range_Logging.Append_To_Log:

```ada
procedure Add_To_Total (Incr : in Integer) is
begin
  Total := Total + Incr;
  The_Log.Append_To_Log (Incr);
end Add_To_Total;
```

Because GNATprove separately checks Liskov Substitution Principle for procedure Append_To_Log, it can use the class-wide contract of Logging.Append_To_Log for analyzing procedure Add_To_Total.
5.8.4 Dynamic Types and Invisible Components

The *Data Initialization Policy* in SPARK applies specially to objects of tagged type. In general, the dynamic type of an object of tagged type may be different from its static type, hence the object may have invisible components, that are only revealed when the object is converted to a class-wide type.

For objects of tagged type, modes on parameters and data dependency contracts have a different meaning depending on the object’s static type:

- For objects of a specific (not class-wide) tagged type, the constraints described in *Data Initialization Policy* apply to the visible components of the object only.
- For objects of a class-wide type, the constraints described in *Data Initialization Policy* apply to all components of the object, including invisible ones.

GNATprove checks during flow analysis that no uninitialized data is read in the program, and that the specified data dependencies and flow dependencies are respected in the implementation, based on the semantics above for objects of tagged type. For example, it detects no issues during flow analysis on procedure `Use_Logging` which initializes parameter `Log` and then updates it:

```plaintext
with Logging; use Logging;

procedure Use_Logging (Log : out Log_Type) with SPARK_Mode is
begin
  Log.Init_Log;
  Log.Append_To_Log (1);
end Use_Logging;
```

If parameter `Log` is of dynamic type `Logging.Log_Type`, then the call to `Init_Log` initializes all components of `Log` as expected, and the call to `Append_To_Log` can safely read those. If parameter `Log` is of dynamic type `Range_Logging.Log_Type`, then the call to `Init_Log` only initializes those components of `Log` that come from the parent type `Logging.Log_Type`, but since the call to `Append_To_Log` only read those, then there is no read of uninitialized data. This is in contrast with what occurs in procedure `Use_Logging_Classwide`:

```plaintext
with Logging; use Logging;

procedure Use_Logging_Classwide (Log : out Log_Type'Class) with SPARK_Mode is
begin
  Log_Type (Log).Init_Log;
  Log.Append_To_Log (2);
end Use_Logging_Classwide;
```

on which GNATprove issues an error during flow analysis:

```
use_logging_classwide.adb:8:04: high: extension of "Log" is not initialized
```

Indeed, the call to `Init_Log` (a non-dispatching call to `Logging.Init_Log` due to the conversion on its parameter) only initializes those components of `Log` that come from the parent type `Logging.Log_Type`, but the call to `Append_To_Log` may read other components from `Range_Logging.Log_Type` which may not be initialized.

A consequence of these rules for data initialization policy is that a parameter of a specific tagged type cannot be converted to a class-wide type, for example for a dispatching call. A special aspect *Extensions_Visible* is defined in SPARK to allow this case. When *Extensions_Visible* is specified on a subprogram, the data initialization
policy for the subprogram parameters of a specific tagged type requires that the constraints described in Data Initialization Policy apply to all components of the object, as if the parameter was of a class-wide type. This allows converting this object to a class-wide type.

5.9 Concurrency and Ravenscar Profile

Concurrency in SPARK requires enabling the Ravenscar profile (see Guide for the use of the Ada Ravenscar Profile in high integrity systems by Alan Burns, Brian Dobbing, and Tullio Vardanega). This profile defines a subset of the Ada concurrency features suitable for hard real-time/embedded systems requiring stringent analysis, such as certification and safety analyses. In particular, it is concerned with determinism, analyzability, and memory-boundedness.

In addition to the subset defined by the Ravenscar profile, concurrency in SPARK also requires that tasks do not start executing before the program has been completely elaborated, which is expressed by setting pragma Partition_Elaboration_Policy to the value Sequential. Together with the requirement to apply the Ravenscar profile, this means that a concurrent SPARK program should define the following configuration pragmas, either in a configuration pragma file (see Setting the Default SPARK_Mode for an example of defining a configuration pragma file in your project file) or at the start of files:

```ada
pragma Profile (Ravenscar);
pragma Partition_Elaboration_Policy (Sequential);
```

GNATprove also supports the GNAT Extended Ravenscar profile (see Section 4.5 “The Extended Ravenscar Profiles” in GNAT User’s Guide Supplement for GNAT Pro Safety-Critical and GNAT Pro High-Security). To use the GNAT Extended Ravenscar profile simply replace Ravenscar with GNAT_Extended_Ravenscar in the pragma Profile in the above code. The extended profile is intended for hard real-time/embedded systems that may require schedulability analysis but not the most stringent analyses required for other domains.

In particular, to increase expressive power the GNAT Extended Ravenscar profile relaxes certain restrictions defined by the standard Ravenscar profile. Notably, these relaxed constraints allow multiple protected entries per protected object, multiple queued callers per entry, and more expressive protected entry barrier expressions. The profile also allows the use of relative delay statements in addition to the absolute delay statements allowed by Ravenscar. The two forms of delay statement are processed by GNATprove based on the type of their expression, as follows (absolute and relative delays, respectively):

- If the expression is of the type Ada.Real_Time.Time then for the purposes of determining global inputs and outputs the absolute delay statement is considered just like the relative delay statement, i.e., to reference the state abstraction Ada.Real_Time.Clock_Time as an input (see SPARK RM 9(17) for details).
- If the expression is of the type Ada.Calendar.Time then it is considered to reference the state abstraction Ada.Calendar.Clock_Time, which is defined similarly to Ada.Real_Time.Clock_Time but represents a different time base.

5.9.1 Tasks and Data Races

Parallel Ada programs are made of several tasks, that is, separate threads of control which share the same address space. In Ravenscar, only library-level, nonterminating tasks are allowed.

Task Types and Task Objects

Like ordinary objects, tasks have a type in Ada and can be stored in composite objects such as arrays and records. The definition of a task type looks like the definition of a subprogram. It is made of two parts: a declaration, usually empty as Ravenscar does not allow tasks to have entries (for task rendezvous), and a body containing the list of statements
to be executed by objects of the task type. The body of nonterminating tasks (the only ones allowed in Ravenscar)
usually takes the form of an infinite loop. For task objects of a given type to be parameterized, task types can have
discriminants. As an example, a task type `Account_Management` can be declared as follows:

```plaintext
package Account is
    Num_Accounts : Natural := 0;
    task type Account_Management;
end Account;

package body Account is
    task body Account_Management is
        begin
            loop
                Get_Next_Account_Created;
                Num_Accounts := Num_Accounts + 1;
            end loop;
        end Account_Management;
end Account;
```

Then, tasks of type `Account_Management` can be created at library level, either as complete objects or as compo-
nents of other objects:

```plaintext
package Bank is
    Special_Accounts : Account_Management;
    type Account_Type is (Regular, Premium, Selective);
    type Account_Array is array (Account_Type) of Account_Management;
    All_Accounts : Account_Array;
end Bank;
```

If only one object of a given task type is needed, then the task object can be declared directly giving a declaration and
a body. An anonymous task type is then defined implicitly for the declared type object. For example, if we only need
one task `Account_Management` then we can write:

```plaintext
package Account is
    Num_Accounts : Natural := 0;
    task Account_Management;
end Account;

package body Account is
    task body Account_Management is
        begin
            loop
                Get_Next_Account_Created;
                Num_Accounts := Num_Accounts + 1;
            end loop;
        end Account_Management;
end Account;
```
Preventing Data Races

In Ravenscar, communication between tasks can only be done through shared objects (tasks cannot communicate through rendezvous as task entries are not allowed in Ravenscar). In SPARK, the language is further restricted to avoid the possibility of erroneous concurrent access to shared data (a.k.a. data races). More precisely, tasks can only share synchronized objects, that is, objects that are protected against concurrent accesses. These include atomic objects, protected objects (see Protected Objects and Deadlocks), and suspension objects (see Suspension Objects). As an example, our previous definition of the Account_Management task type was not in SPARK. Indeed, data races could occur when accessing the global variable Num_Accounts, as detected by GNATprove:

```plaintext
bank1.ads:5:04: high: possible data race when accessing variable "account1.num_accounts"
bank1.ads:5:04: high: with task "bank1.all_accounts"
bank1.ads:5:04: high: with task "bank1.special_accounts"
```

To avoid this problem, shared variable Num_Account can be declared atomic:

```plaintext
class Account is
    Num_Accounts : Natural := 0 with Atomic;
    task type Account_Management;
extend Account;
end Account;
```

With this modification, GNATprove now alerts us that the increment of Num_Account is not legal, as a volatile variable (which is the case of atomic variables) cannot be read as a subexpression of a larger expression in SPARK:

```plaintext
account2.adb:15:26: volatile object cannot appear in this context (SPARK RM 7.1.3(12))
```

This can be fixed by copying the current value of Num_Account in a temporary before the increment:

```plaintext
declare
    Tmp : constant Natural := Num_Accounts;
begin
    Num_Accounts := Tmp + 1;
end;
```

But note that even with that fix, there is no guarantee that Num_Accounts is incremented by one each time an account is created. Indeed, two tasks may read the same value of Num_Accounts and store the same value in Tmp before both updating it to Tmp + 1. In such a case, two accounts have been created but Num_Accounts has been increased by 1 only. There is no data race in this program, which is confirmed by running GNATprove with no error, but there is by design a race condition on shared data that causes the program to malfunction. The correct way to fix this in SPARK is to use Protected Types and Protected Objects.

As they cannot cause data races, constants and variables that are constant after elaboration (see Aspect Constant_After_Elaboration) are considered as synchronized and can be accessed by multiple tasks. For example, we can declare a global constant Max_Accounts and use it inside Account_Management without risking data races:

```plaintext
class Account is
    Num_Accounts : Natural := 0 with Atomic;
    Max_Accounts : constant Natural := 100;
    task type Account_Management;
extend Account;
end Account;
```

package body Account is
```
```
It is possible for a task to access an unsynchronized global variable only if this variable is declared in the same package as the task and if there is a single task accessing this variable. To allow this property to be statically verified, only tasks of an anonymous task type are allowed to access unsynchronized variables and the variables accessed should be declared to belong to the task using aspect Part_Of. Global variables declared to belong to a task are handled just like local variables of the task, that is, they can only be referenced from inside the task body. As an example, we can state that Num_Accounts is only accessed by the task object Account_Management in the following way:

```clojure
package Account is
  task Account_Management;
      Num_Accounts : Natural := 0 with Part_Of => Account_Management;
end Account;
```

### 5.9.2 Task Contracts

[SPARK]

Dependency contracts can be specified on tasks. As tasks should not terminate in SPARK, such contracts specify the dependencies between outputs and inputs of the task *updated while the task runs*:

- The **data dependencies** introduced by aspect Global specify the global data read and written by the task.
- The **flow dependencies** introduced by aspect Depends specify how task outputs depend on task inputs.

This is a difference between tasks and subprograms, for which such contracts describe the dependencies between outputs and inputs *when the subprogram returns*.

**Data Dependencies**

Data dependencies on tasks follow the same syntax as the ones on subprograms (see `Data Dependencies`). For example, data dependencies can be specified for task (type or object) Account_Management as follows:

```clojure
package Account is
  task type Account_Management with
      Global => (In_Out => Num_Accounts);
end Account;
```
Flow Dependencies

Flow dependencies on tasks follow the same syntax as the ones on subprograms (see *Flow Dependencies*). For example, flow dependencies can be specified for task (type or object) `Account_Management` as follows:

```ada
package Account is
    Num_Accounts : Natural := 0 with Atomic;

    task type Account_Management with
        Depends => (Account_Management => Account_Management,
                     Num_Accounts => Num_Accounts);
end Account;
```

Notice that the task unit itself is both an input and an output of the task:

- It is an input because task discriminants (if any) and task attributes may be read in the task body.
- It is an output so that the task unit may be passed as in out parameter in a subprogram call. But note that the task object cannot be modified once created.

The dependency of the task on itself can be left implicit as well, as follows:

```ada
package Account is
    Num_Accounts : Natural := 0 with Atomic;

    task type Account_Management with
        Depends => (Num_Accounts => Num_Accounts);
end Account;
```

5.9.3 Protected Objects and Deadlocks

[Ravenscar]

In Ada, protected objects are used to encapsulate shared data and protect it against data races (low-level unprotected concurrent access to data) and race conditions (lack of proper synchronization between reads and writes of shared data). They coordinate access to the protected data guaranteeing that read-write accesses are always exclusive while allowing concurrent read-only accesses. In Ravenscar, only library-level protected objects are allowed.

**Protected Types and Protected Objects**

Definitions of protected types resemble package definitions. They are made of two parts, a declaration (divided into a public part and a private part) and a body. The public part of a protected type’s declaration contains the declarations of the subprograms that can be used to access the data declared in its private part. The body of these subprograms are located in the protected type’s body. In Ravenscar, protected objects should be declared at library level, either as complete objects or as components of other objects. As an example, here is how a protected type can be used to coordinate concurrent accesses to the global variable `Num_Accounts`:

```ada
package Account is

    protected type Protected_Natural is
        procedure Incr;
        function Get return Natural;
    private
        The_Data : Natural := 0;
    end Protected_Natural;
```
Contrary to the previous version using an atomic global variable (see Preventing Data Races), this version prevents also any race condition when incrementing the value of Num_Accounts. But note that there is still a possible race condition between the time the value of Num_Accounts is read and checked to be less than Max_Accounts and the time it is incremented. So this version does not guarantee that Num_Accounts stays below Max_Accounts.

The correct way to fix this in SPARK is to use protected entries (see Protected Subprograms).

Note that, in SPARK, to avoid initialization issues on protected objects, both private variables and variables belonging to a protected object must be initialized at declaration (either explicitly or through default initialization).

Just like for tasks, it is possible to directly declare a protected object if it is the only one of its type. In this case, an anonymous protected type is implicitly declared for it. For example, if Num_Account is the only Protected_Natural we need, we can directly declare:
The access mode granted by protected subprograms depends on their kind:

- Protected procedures provide exclusive read-write access to the private data of a protected object.
- Protected functions offer concurrent read-only access to the private data of a protected object.
- Protected entries are conceptually procedures with a barrier. When an entry is called, the caller waits until the condition of the barrier is true to be able to access the protected object.

So that scheduling is deterministic, Ravenscar requires that at most one entry is specified in a protected unit and at most one task is waiting on a given entry at every time. To ensure this, GNATprove checks that no two tasks can call the same protected object’s entry. As an example, we could replace the procedure `Incr` of `Protected_Natural` to wait until `The_Data` is smaller than `Max_Accounts` before incrementing it. As only simple Boolean variables are allowed as entry barriers in Ravenscar, we add such a Boolean flag `Not_Full` as a component of the protected object:

```plaintext
package Account is

protected type Protected_Natural is
  entry Incr;
  function Get return Natural is (The_Data);
private
  The_Data : Natural := 0;
  Not_Full : Boolean := True;
end Protected_Natural;

Num_Accounts : Protected_Natural;
Max_Accounts : constant Natural := 100;

task type Account_Management;
end Account;

package body Account is

protected body Protected_Natural is
  entry Incr when Not_Full is
    begin
      The_Data := The_Data + 1;
      if The_Data = Max_Accounts then
        Not_Full := False;
      end if;
    end Incr;

  function Get return Natural is (The_Data);
end Protected_Natural;

task body Account_Management is
```
This version fixes the remaining race condition on this example, thus ensuring that every new account created bumps the value of **Num_Accounts** by 1, and that **Num_Accounts** stays below **Max_Accounts**.

To avoid data races, protected subprograms should not access unsynchronized objects (see *Tasks and Data Races*). Like for tasks, it is still possible for subprograms of a protected object of an anonymous protected type to access an unsynchronized object declared in the same package as long as it is not accessed by any task or subprogram from other protected objects. In this case, the unsynchronized object should have a **Part_Of** aspect referring to the protected object. It is then handled as if it was a private variable of the protected object. This is typically done so that the address in memory of the variable can be specified, using either aspect **Address** or a corresponding representation clause. Here is how this could be done with **Num_Account**:

```ada
package Account is
  protected Protected_Num_Accounts is
    procedure Incr;
    function Get return Natural;
  end Protected_Num_Accounts;

  Num_Accounts : Natural := 0 with
    Part_Of => Protected_Num_Accounts,
    Address => ...
end Account;
```

As it can prevent access to a protected object for an unbounded amount of time, a task should not be blocked or delayed while inside a protected subprogram. Actions that can block a task are said to be **potentially blocking**. For example, calling a protected entry, explicitly waiting using a `delay_until` statement (note that `delay` statements are forbidden in Ravenscar), or suspending on a suspension object (see *Suspension Objects*) are potentially blocking actions. In Ada, it is an error to do a potentially blocking action while inside a protected subprogram. Note that a call to a function or a procedure on another protected object is not considered to be potentially blocking. Indeed, such a call cannot block a task in the absence of deadlocks (which is enforced in Ravenscar using the priority ceiling protocol, see *Avoiding Deadlocks and Priority Ceiling Protocol*).

GNATprove verifies that no potentially blocking action is performed from inside a protected subprogram in a modular way on a per subprogram basis. Thus, if a subprogram can perform a potentially blocking operation, every call to this subprogram from inside a protected subprogram will be flagged as a potential error. As an example, the procedure **Incr_Num_Accounts** is potentially blocking and thus should not be called, directly or indirectly, from a protected subprogram:

```ada
package Account is
  protected type Protected_Natural is
    entry Incr;
  private
    The_Data : Natural := 0;
  end Protected_Natural;

  Num_Accounts : Protected_Natural;

  procedure Incr_Num_Accounts;
end Account;
```
end Account;

package body Account is

   procedure Incr_Num_Accounts is
      begin
         Num_Accounts.Incr;
      end Incr_Num_Accounts;

end Account;

Avoiding Deadlocks and Priority Ceiling Protocol

To ensure exclusivity of read-write accesses, when a procedure or an entry of a protected object is called, the protected object is locked so that no other task can access it, be it in a read-write or a read-only mode. In the same way, when a protected function is called, no other task can access the protected object in read-write mode. A deadlock happens when two or more tasks are unable to run because each of them is trying to access a protected object that is currently locked by another task.

To ensure absence of deadlocks on a single core, Ravenscar requires the use of the Priority Ceiling Protocol. This protocol ensures that no task can be blocked trying to access a protected object locked by another task. It relies on task’s priorities. The priority of a task is a number encoding its urgency. On a single core, scheduling ensures that the current running task can only be preempted by another task if it has a higher priority. Using this property, the Priority Ceiling Protocol works by increasing the priorities of tasks accessing a protected object to a priority that is at least as high as the priorities of other tasks accessing this object. This ensures that, while holding a lock, the currently running task cannot be preempted by a task which could later be blocked by this lock.

To enforce this protocol, every task is associated with a base priority, either given at declaration using the Priority aspect or defaulted. This base priority is static and cannot be modified after the task’s declaration. A task also has an active priority which is initially the task’s base priority but will be increased when the task enters a protected action. For example, we can set the base priority of Account_Management to 5 at declaration:

package Account is
   task type Account_Management with Priority => 5;
end Account;

Likewise, each protected object is associated at declaration with a ceiling priority which should be equal or higher than the active priority of any task accessing it. The ceiling priority of a protected object does not need to be static, it can be set using a discriminant for example. Still, like for tasks, Ravenscar requires that it is set once and for all at the object’s declaration and cannot be changed afterwards. As an example, let us attach a ceiling priority to the protected object Num_Accounts. As Num_Accounts will be used by Account_Management, its ceiling priority should be no lower than 5:

package Account is

   protected Num_Accounts with Priority => 7 is
      procedure Incr;
      function Get return Natural;
   private
      The_Data : Natural := 0;
   end Num_Accounts;

   task type Account_Management with Priority => 5;

end Account;
5.9.4 Suspension Objects

[Ravenscar]

The language-defined package Ada.Synchronous_Task_Control provides a type for semaphores called suspension objects. They allow lighter synchronization mechanisms than protected objects (see Protected Objects and Deadlocks). More precisely, a suspension object has a Boolean state which can be set atomically to True using the Set_True procedure. When a task suspends on a suspension object calling the Suspend_Until_True procedure, it is blocked until the state of the suspension object is True. At that point, the state of the suspension object is set back to False and the task is unblocked. Note that Suspend_Until_True is potentially blocking and therefore should not be called directly or indirectly from within Protected Subprograms. In the following example, the suspension object Semaphore is used to make sure T1 has initialized the shared data by the time T2 begins processing it:

```ada
Semaphore : Suspension_Object;
task T1;
task T2;

task body T1 is
begin
    Initialize_Shared_Data;
    Set_True (Semaphore);
    loop
        ...
    end loop;
end T1;

task body T2 is
begin
    Suspend_Until_True (Semaphore);
    loop
        ...
    end loop;
end T2;
```

In Ada, an exception is raised if a task tries to suspend on a suspension object on which another task is already waiting on that same suspension object. Like for verifying that no two tasks can be queued on a protected entry, this verification is done by GNATprove by checking that no two tasks ever suspend on the same suspension object. In the following example, the suspension objects Semaphore1 and Semaphore2 are used to ensure that T1 and T2 never call Enter_Protected.Region at the same time. GNATprove will successfully verify that only one task can suspend on each suspension object:

```ada
Semaphore1, Semaphore2 : Suspension_Object;
task T1;
task T2;

task body T1 is
begin
    loop
        Suspend_Until_True (Semaphore1);
        Enter_Protected.Region;
        Set_True (Semaphore2);
    end loop;
end T1;
```
Task body T2 is
begin
  loop
    Suspend_Until_True (Semaphore2);
    Enter_Protected_Region;
    Set_True (Semaphore1);
  end loop;
end T2;

5.9.5 State Abstraction and Concurrency

[SPARK]
Protected objects, as well as suspension objects, are effectively volatile which means that their value as seen from a given task may change at any time due to some other task accessing the protected object or suspension object. If they are part of a state abstraction, the volatility of the abstract state must be specified by using the External aspect (see External State Abstraction). Note that task objects, though they can be part of a package’s hidden state, are not effectively volatile and can therefore be components of normal state abstractions. For example, the package Synchronous_Abstractions defines two abstract states, one for external objects, containing the atomic variable V, the suspension object S, and the protected object P, and one for normal objects, containing the task T:

```
package Synchronous_Abstractions with
  Abstract_State => (Normal_State, (Synchronous_State with External))
is
  end Synchronous_Abstractions;
end Synchronous_Abstractions;
```

To avoid data races, task bodies, as well as protected subprograms, should only access synchronized objects (see Preventing Data Races). State abstractions containing only synchronized objects can be specified to be synchronized using the Synchronous aspect. Only synchronized state abstractions can be accessed from task bodies and protected subprograms. For example, if we want the procedure Do_Something to be callable from the task Use_Synchronized_State, then the state abstraction Synchronous_State must be annotated using the Synchronous aspect:
package Synchronous_Abstractions with
  Abstract_State => (Normal_State,
      (Synchronous_State with Synchronous, External))
is
  procedure Do_Something with Global => (In_Out => Synchronous_State);
end Synchronous_Abstractions;

task body Use_Synchronized_State is
begin
  loop
    Synchronous_Abstractions.Do_Something;
  end loop;
end Use_Synchronized_State;

5.9.6 Project-wide Tasking Analysis

Tasking-related analysis, as currently implemented in GNATprove, is subject to two limitations:

First, the analysis is always done when processing a source file with task objects or with a subprogram that can be used as a main subprogram of a partition (i.e. is at library level, has no parameters, and is either a procedure or a function returning an integer type).

In effect, you might get spurious checks when:

- a subprogram satisfies conditions for being used as a main subprogram of a partition but is not really used that way, i.e. it is not specified in the Main attribute of the GNAT project file you use to build executables, and
- it “withs” or is “withed” (directly or indirectly) from a library-level package that declares some task object, and
- both the fake “main” subprogram and the task object access the same resource in a way that violates tasking-related rules (e.g. suspends on the same suspension object).

As a workaround, either wrap the fake “main” subprogram in a library-level package or give it a dummy parameter.

Second, the analysis is only done in the context of all the units “withed” (directly and indirectly) by the currently analyzed source file.

In effect, you might miss checks when:

- building a library that declares tasks objects in unrelated source files, i.e. files that are never “withed” (directly or indirectly) from the same file, and those tasks objects access the same resource in a way that violates tasking-related rules, or
- using a library that internally declares some tasks objects, they access some tasking-sensitive resource, and your main subprogram also accesses this resource.

As a workaround, when building library projects add a dummy main subprogram that “withs” all the library-level packages of your project.

5.9.7 Interrupt Handlers

SPARK puts no restrictions on the Ada interrupt handling and GNATprove merely checks that interrupt handlers will be safely executed. In Ada interrupts handlers are defined by annotating protected procedures, for example:


protected P is
Currently GNATprove emits a check for each handler declaration saying that the corresponding interrupt might be already reserved. In particular, it might be reserved by either the system or the Ada runtime; see GNAT pragmas Interrupt_State and Unreserve_All_Interrupts for details. Once examined, those checks can be suppressed with pragma Annotate.

If pragma Priority or Interrupt_Priority is explicitly specified for a protected type, then GNATprove will check that its value is in the range of the System.Any_Priority or System.Interrupt_Priority, respectively; see Ada RM D.3(6.1/3).

For interrupt handlers whose bodies are annotated with SPARK_Mode => On, GNATprove will additionally check that:

- the interrupt handler does not call (directly or indirectly) the Ada.Task_Identification.Current_Task routine, which might cause a Program_Error runtime exception; see Ada RM C.7.1(17/3);
- all global objects read (either as an Input or a Proof_In) by the interrupt handler are initialized at elaboration;
- there are no unsynchronized objects accessed both by the interrupt handler and by some task (or by some other interrupt handler);
- there are no protected objects locked both by the interrupt handler and by some task (or by some other interrupt handler).

5.10 SPARK Libraries

5.10.1 Functional Containers Library

To model complex data structures, one often needs simpler, mathematical like containers. The mathematical containers provided in the SPARK library are unbounded and may contain indefinite elements. Furthermore, to be usable in every context, they are neither controlled nor limited. So that these containers can be used safely, we have made them functional, that is, no primitives are provided which would allow modifying an existing container. Instead, their API features functions creating new containers from existing ones. As an example, functional containers provide no Insert procedure but rather a function Add which creates a new container with one more element than its parameter:

```ada
function Add (C : Container; E : Element_Type) return Container;
```

As a consequence, these containers are highly inefficient. They are also memory consuming as the allocated memory is not reclaimed when the container is no longer referenced. Thus, they should in general be used in ghost code and annotations so that they can be removed from the final executable.

There are 3 functional containers, which are part of the GNAT standard library:

- Ada.Containers.Functional_Maps
- Ada.Containers.Functional_Sets
- Ada.Containers.Functional_Vectors

Sequences defined in Functional_Vectors are no more than ordered collections of elements. In an Ada like manner, the user can choose the range used to index the elements:

```ada
function Length (S : Sequence) return Count_Type;
function Get (S : Sequence; N : Index_Type) return Element_Type;
```

Functional sets offer standard mathematical set functionalities such as inclusion, union, and intersection. They are neither ordered nor hashed:
Functional maps offer a dictionary between any two types of elements:

```ada
function Contains (S : Set; E : Element_Type) return Boolean;
function "<=" (Left : Set; Right : Set) return Boolean;
```

Functional containers offer a dictionary between any two types of elements:

```ada
function Has_Key (M : Map; K : Key_Type) return Boolean;
function Get (M : Map; K : Key_Type) return Element_Type;
```

Each functional container type supports iteration as appropriate, so that its elements can easily be quantified over.

These containers can easily be used to model user defined data structures. They were used to this end to annotate and verify a package of allocators (see allocators example in the Examples in the Toolset Distribution). In this example, an allocator featuring a free list implemented in an array is modeled by a record containing a set of allocated resources and a sequence of available resources:

```ada
type Status is (Available, Allocated);
type Cell is record
  Stat : Status;
  Next : Resource;
end record;
type Allocator is array (Valid_Resource) of Cell;
type Model is record
  Available : Sequence;
  Allocated : Set;
end record;
```

**Note:** Functional sets and maps represent elements modulo equivalence. For proof, the range of quantification over their content includes all elements that are equivalent to elements included in the container. On the other hand, for execution, the iteration is only done on elements which have actually been included in the container. This difference may make interaction between test and proof tricky when the equivalence relation is not the equality.

**Note:** Functional containers do not comply with the ownership policy of SPARK if element or key types are ownership types. Care should be taken to do the required copies when storing these elements/keys inside the container or retrieving them.

### 5.10.2 Formal Containers Library

Containers are generic data structures offering a high-level view of collections of objects, while guaranteeing fast access to their content to retrieve or modify it. The most common containers are lists, vectors, sets and maps, which are defined as generic units in the Ada Standard Library. In critical software where verification objectives severely restrict the use of pointers, containers offer an attractive alternative to pointer-intensive data structures.

The Ada Standard Library defines two kinds of containers:

- The controlled containers using dynamic allocation, for example Ada.Containers.Vectors. They define containers as controlled tagged types, so that memory for the container is automatically reallocated during assignment and automatically freed when the container object’s scope ends.

- The bounded containers not using dynamic allocation, for example Ada.Containers.Bounded_Vectors. They define containers as discriminated tagged types, so that the memory for the container can be reserved at initialization.
Although bounded containers are better suited to critical software development, neither controlled containers nor bounded containers can be used in SPARK, because their API does not lend itself to adding suitable contracts (in particular preconditions) ensuring correct usage in client code.

The formal containers are a variation of the bounded containers with API changes that allow adding suitable contracts, so that GNATprove can prove that client code manipulates containers correctly. There are 7 formal containers, which are part of the GNAT standard library:

- Ada.Containers.Formal_Vectors
- Ada.Containers.Formal_Indefinite_Vectors
- Ada.Containers.Formal_Doubly_Linked_Lists
- Ada.Containers.Formal_Hashed_Sets
- Ada.Containers.Formal_Ordered_Sets
- Ada.Containers.Formal_Hashed_Maps

Lists, sets and maps can only be used with definite objects (objects for which the compiler can compute the size in memory, hence not String nor T'Class). Vectors come in two flavors for definite objects (Formal_Vectors) and indefinite objects (Formal_Indefinite_Vectors).

Lists, sets, maps, and definite vectors are always bounded. Indefinite vectors can be bounded or unbounded depending on the value of the formal parameter Bounded when instantiating the generic unit. Bounded containers do not use dynamic allocation. Unbounded vectors use dynamic allocation to expand their internal block of memory.

### Modified API of Formal Containers

The visible specification of formal containers is in SPARK, with suitable contracts on subprograms to ensure correct usage, while their private part and implementation is not in SPARK. Hence, GNATprove can be used to prove correct usage of formal containers in client code, but not to prove that formal containers implement their specification.

Procedures Update_Element or Query_Element that iterate over a container are not defined on formal containers. Specification and analysis of such procedures that take an access-to-procedure in parameter is beyond the capabilities of SPARK and GNATprove. See Excluded Ada Features.

Procedures and functions that query the content of a container take the container in parameter. For example, function Has_Element that queries if a container has an element at a given position is declared as follows:

```plaintext
function Has_Element (Container : T; Position : Cursor) return Boolean;
```

This is different from the API of controlled containers and bounded containers, where it is sufficient to pass a cursor to these subprograms, as the cursor holds a reference to the underlying container:

```plaintext
function Has_Element (Position : Cursor) return Boolean;
```

Cursors of formal containers do not hold a reference to a specific container, as this would otherwise introduce aliasing between container and cursor variables, which is not supported in SPARK. See Absence of Interferences. As a result, the same cursor can be applied to multiple container objects.

For each container type, the library provides model functions that are used to annotate subprograms from the API. The different models supply different levels of abstraction of the container’s functionalities. These model functions are grouped in Ghost Packages named Formal_Model.

The higher level view of a container is usually the mathematical structure of element it represents. We use a sequence for ordered containers such as lists and vectors and a mathematical map for imperative maps. This allows us to specify the effects of a subprogram in a very high level way, not having to consider cursors nor order of elements in a map:
procedure Increment_All (L : in out List) with
  Post =>
    (for all N in 1 .. Length (L) =>
      Element (Model (L), N) = Element (Model (L)'Old, N) + 1);

procedure Increment_All (S : in out Map) with
  Post =>
    (for all K of Model (S)'Old => Has_Key (Model (S), K))
    and
    (for all K of Model (S) =>
      Get (Model (S), K) = Get (Model (S)'Old, K) + 1);

For sets and maps, there is a lower level model representing the underlying order used for iteration in the container, as well as the actual values of elements/keys. It is a sequence of elements/keys. We can use it if we want to specify in Increment_All on maps that the order and actual values of keys are preserved:

procedure Increment_All (S : in out Map) with
  Post =>
    Keys (S) = Keys (S)'Old
    and
    (for all K of Model (S) =>
      Get (Model (S), K) = Get (Model (S)'Old, K) + 1);

Finally, cursors are modeled using a functional map linking them to their position in the container. For example, we can state that the positions of cursors in a list are not modified by a call to Increment_All:

procedure Increment_All (L : in out List) with
  Post =>
    Positions (L) = Positions (L)'Old
    and
    (for all N in 1 .. Length (L) =>
      Element (Model (L), N) = Element (Model (L)'Old, N) + 1);

Switching between the different levels of model functions allows to express precise considerations when needed without polluting upper level specifications. For example, consider a variant of the List.Find function defined in the API of formal containers, which returns a cursor holding the value searched if there is one, and the special cursor No_Element otherwise:

with Element_Lists; use Element_Lists; use Element_Lists.Lists;

function My_Find (L : List; E : Element_Type) return Cursor with
  SPARK_Mode,
  Contract_Cases =>
    (Contains (L, E) => Has_Element (L, My_Find'Result) and then
      Element (L, My_Find'Result) = E,
    not Contains (L, E) => My_Find'Result = No_Element);

The ghost functions mentioned above are specially useful in \textit{Loop Invariants} to refer to cursors, and positions of elements in the containers. For example, here, ghost function Positions is used in the loop invariant to query the position of the current cursor in the list, and Model is used to specify that the value searched is not contained in the part of the container already traversed (otherwise the loop would have exited):

function My_Find (L : List; E : Element_Type) return Cursor with
  SPARK_Mode
is

1 with Element_Lists; use Element_Lists; use Element_Lists.Lists;
3
4 function My_Find (L : List; E : Element_Type) return Cursor with
5   SPARK_Mode,
6   Contract_Cases =>
7     (Contains (L, E) => Has_Element (L, My_Find'Result) and then
8       Element (L, My_Find'Result) = E,
9     not Contains (L, E) => My_Find'Result = No_Element);
10
11 The ghost functions mentioned above are specially useful in \textit{Loop Invariants} to refer to cursors, and positions of elements in the containers. For example, here, ghost function Positions is used in the loop invariant to query the position of the current cursor in the list, and Model is used to specify that the value searched is not contained in the part of the container already traversed (otherwise the loop would have exited):
Cu : Cursor := First (L);

begin
  while Has_Element (L, Cu) loop
    pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
      Element (Model (L), I) /= E);

    if Element (L, Cu) = E then
      return Cu;
    end if;

    Next (L, Cu);
  end loop;

  return No_Element;
end My_Find;

GNATprove proves that function My_Find implements its specification:

my_find.adb:8:30: info: loop invariant initialization proved
my_find.adb:8:30: info: loop invariant preservation proved
my_find.adb:8:49: info: precondition proved
my_find.adb:9:33: info: precondition proved
my_find.adb:11:10: info: precondition proved
my_find.adb:15:07: info: precondition proved
my_find.ads:6:03: info: complete contract cases proved
my_find.ads:6:03: info: disjoint contract cases proved
my_find.ads:7:26: info: contract case proved
my_find.ads:8:29: info: precondition proved
my_find.ads:9:26: info: contract case proved

Note: Just like functional containers, the formal containers do not comply with the ownership policy of SPARK if element or key types are ownership types. Care should be taken to do the required copies when storing these elements/keys inside the container or retrieving them.

Quantification over Formal Containers

Quantified Expressions can be used over the content of a formal container to express that a property holds for all elements of a container (using for all) or that a property holds for at least one element of a container (using for some).

For example, we can express that all elements of a formal list of integers are prime as follows:

(for all Cu in My_List => Is_Prime (Element (My_List, Cu)))

On this expression, the GNAT compiler generates code that iterates over My_List using the functions First, Has_Element and Next given in the Iterable aspect applying to the type of formal lists, so the quantified expression above is equivalent to:

declare
  Cu : Cursor_Type := First (My_List);
  Result : Boolean := True;
begin
  while Result and then Has_Element (My_List, Cu) loop

Result := Is_Prime (Element (My_List, Cu));
Cu := Next (My_List, Cu);
end loop;
end;

where Result is the value of the quantified expression. See GNAT Reference Manual for details on aspect Iterable.

### 5.10.3 SPARK Lemma Library

As part of the SPARK product, a library of lemmas is available through the project file `<spark-install>/lib/gnat/spark_lemmas.gpr`. To use this library in a program, you need to add a corresponding dependency in your project file, for example:

```plaintext
with "spark_lemmas";
project My_Project is ...
end My_Project;
```

You may need to update the environment variable `GPR_PROJECT_PATH` for the lemma library project to be found by GNAT compiler, as described in *Installation of GNATprove*.

You also need to set the environment variable `SPARK_LEMMAS_OBJECT_DIR` to the absolute path of the object directory where you want compilation and verification artefacts for the lemma library to be created. This should be an absolute path (not a relative one) otherwise these artefacts will be created inside your SPARK install.

Finally, if you instantiate in your code a generic from the lemma library, you also need to pass `-gnateDSPARK_BODY_MODE=Off` as a compilation switch for these generic units.

This library consists in a set of ghost null procedures with contracts (called *lemmas*). Here is an example of such a lemma:

```plaintext
procedure Lemma_Div_Is_Monotonic
  (Val1 : Int;
   Val2 : Int;
   Denom : Pos)
with
  Global => null,
  Pre => Val1 <= Val2,
  Post => Val1 / Denom <= Val2 / Denom;
```

whose body is simply a null procedure:

```plaintext
procedure Lemma_Div_Is_Monotonic
  (Val1 : Int;
   Val2 : Int;
   Denom : Pos)
is null;
```

This procedure is ghost (as part of a ghost package), which means that the procedure body and all calls to the procedure are compiled away when producing the final executable without assertions (when switch `-gnata` is not set). On the contrary, when compiling with assertions for testing (when switch `-gnata` is set) the precondition of the procedure is executed, possibly detecting invalid uses of the lemma. However, the main purpose of such a lemma is to facilitate automatic proof, by providing the prover specific properties expressed in the postcondition. In the case of `Lemma_Div_Is_Monotonic`, the postcondition expresses an inequality between two expressions. You may use this lemma in your program by calling it on specific expressions, for example:
R1 := X1 / Y;
R2 := X2 / Y;
 Lemma_Div_Is_Monotonic (X1, X2, Y);
-- at this program point, the prover knows that R1 <= R2
-- the following assertion is proved automatically:
pragma Assert (R1 <= R2);

Note that the lemma may have a precondition, stating in which contexts the lemma holds, which you will need to prove when calling it. For example, a precondition check is generated in the code above to show that X1 <= X2. Similarly, the types of parameters in the lemma may restrict the contexts in which the lemma holds. For example, the type Pos for parameter Denom of Lemma_Div_Is_Monotonic is the type of positive integers. Hence, a range check may be generated in the code above to show that Y is positive.

All the lemmas provided in the SPARK lemma library have been proved either automatically or using Coq interactive prover. The Why3 session file recording all proofs, as well as the individual Coq proof scripts, are available as part of the SPARK product under directory <spark-install>/lib/gnat/proof. For example, the proof of lemma Lemma_Div_Is_Monotonic is a Coq proof of the mathematical property (in Coq syntax):

```
subgoals
  h1 : in_range val1
  h2 : in_range val2
  h3 : in_range1 denom
  h4 : (val1 <= val2) % Z
  (val1 + denom <= val2 + denom) % Z
```

Currently, the SPARK lemma library provides the following lemmas:

- Lemmas on signed integer arithmetic in file spark-arithmetic_lemmas.ads, that are instantiated for 32 bits signed integers (Integer) in file spark-integer_arithmetic_lemmas.ads and for 64 bits signed integers (Long_Integer) in file spark-long_integer_arithmetic_lemmas.ads.

- Lemmas on modular integer arithmetic in file spark-mod_arithmetic_lemmas.ads, that are instantiated for 32 bits modular integers (Interfaces.Unsigned_32) in file spark-mod32_arithmetic_lemmas.ads and for 64 bits modular integers (Interfaces.Unsigned_64) in file spark-mod64_arithmetic_lemmas.ads.

- GNAT-specific lemmas on fixed-point arithmetic in file spark-fixed_point_arithmetic_lemmas.ads, that need to be instantiated by the user for her specific fixed-point type.

- Lemmas on floating point arithmetic in file spark-floating_point_arithmetic_lemmas.ads, that are instantiated for single-precision floats (Float) in file spark-float_arithmetic_lemmas.ads and for double-precision floats (Long_Float) in file spark-long_float_arithmetic_lemmas.ads.

- Lemmas on unconstrained arrays in file spark-unconstrained_array_lemmas.ads, that need to be instantiated by the user for her specific type of index and element, and specific ordering function between elements.

To apply lemmas to signed or modular integers of different types than the ones used in the instances provided in the library, just convert the expressions passed in arguments, as follows:

R1 := X1 / Y;
R2 := X2 / Y;
Lemma_Div_Is_Monotonic (Integer(X1), Integer(X2), Integer(Y));
-- at this program point, the prover knows that R1 <= R2
-- the following assertion is proved automatically:
pragma Assert (R1 <= R2);
5.10.4 Higher Order Function Library

The SPARK product also includes a library of higher order functions for unconstrained arrays. It is available using the same project file as the SPARK Lemma Library.

This library consists in a set of generic entities defining usual operations on arrays. As an example, here is a generic function for the map higher-level function on arrays. It applies a given function F to each element of an array, returning an array of results in the same order.

```spark
generic
  type Index_Type is range <>;
  type Element_In is private;
  type Array_In is array (Index_Type range <>) of Element_In;

  type Element_Out is private;
  type Array_Out is array (Index_Type range <>) of Element_Out;

with function Init_Prop (A : Element_In) return Boolean;
  -- Potential additional constraint on values of the array to allow Map

with function F (X : Element_In) return Element_Out;
  -- Function that should be applied to elements of Array_In

function Map (A : Array_In) return Array_Out with
  Pre => (for all I in A'Range => Init_Prop (A (I))),
  Post => Map'Result'First = A'First
  and then Map'Result'Last = A'Last
  and then (for all I in A'Range => Map'Result (I) = F (A (I))));
```

This function can be instantiated by providing two unconstrained array types ranging over the same index type and a function F mapping a component of the first array type to a component of the second array type. Additionally, a constraint Init_Prop can be supplied for the components of the first array to be allowed to apply F. If no such constraint is needed, Init_Prop can be instantiated with an always True function.

```spark
type Nat_Array is array (Positive range <>) of Natural;

function Small_Enough (X : Natural) return Boolean is
  (X < Integer'Last);

function Increment_One (X : Integer) return Integer is (X + 1) with
  Pre => X < Integer'Last;

function Increment_All is new SPARK.Higher_Order.Map
  (Index_Type => Positive,
   Element_In => Natural,
   Array_In => Nat_Array,
   Element_Out => Natural,
   Array_Out => Nat_Array,
   Init_Prop => Small_Enough,
   F => Increment_One);
```

The Increment_All function above will take as an argument an array of natural numbers small enough to be incremented and will return an array containing the result of incrementing each number by one:

```spark
function Increment_All (A : Nat_Array) return Nat_Array with
  Pre => (for all I in A'Range => Small_Enough (A (I))),
  Post => Increment_All'Result'First = A'First
```
and then Increment_All'Result'Last = A'Last
and then (for all I in A'Range =>
  Increment_All'Result (I) = Increment_One (A (I)));

Currently, the higher-order function library provides the following functions:

- Map functions over unconstrained one-dimensional arrays in file spark-higher_order.ads. These include both in place and functional map subprograms, with and without an additional position parameter.
- Fold functions over unconstrained one-dimensional and two-dimensional arrays in file spark-higher_order-fold.ads. Both left to right and right to left fold functions are available for one-dimensional arrays. For two-dimensional arrays, fold functions go on a line by line, left to right, top-to-bottom way. For ease of use, these functions have been instantiated for the most common cases. Sum and Sum_2 respectively compute the sum of all the elements of a one-dimensional or two-dimensional array, and Count and Count_2 the number of elements with a given Choose property.

**Note:** Unlike the SPARK Lemma Library, these generic functions are not verified once and for all as their correction depends on the functions provided at each instance. As a result, each instance should be verified by running the SPARK tools.

### 5.10.5 SPARK Heap Library

To annotate subprograms that allocate and deallocate memory with explicit Global and Depends contract, a library is available through the project file <spark-install>/lib/gnat/spark_heap.gpr. To use this library in a program, you need to add a corresponding dependency in your project file, for example:

```plaintext
with "spark_heap";
project My_Project is
  ...
end My_Project;
```

You may need to update GPR_PROJECT_PATH and set SPARK_HEAP_OBJECT_DIR environment variables, just like for the SPARK Lemma Library.

This library declares an abstract state, that is implicitly referenced by every occurrence of an allocator and by every call to an instance of the Ada.Unchecked_Deallocation procedure:

```plaintext
package SPARK.Heap with
  SPARK_Mode,
  Abstract_State => (Dynamic_Memory with External => Async_Writers) is ...
```

For example:

```plaintext
with SPARK.Heap;

function New_Integer with
  Global => SPARK.Heap.Dynamic_Memory,
  Volatile_Function
is
  Result : T := new Integer'(0);
begin
  return Result;
end;
```
5.10.6 Input-Output Libraries


The effect of functions and procedures of input-output units is partially modelled. This means in particular:

- that SPARK functions cannot directly call procedures that do input-output. The solution is either to transform them into procedures, or to hide the effect from GNATprove (if not relevant for analysis) by wrapping the standard input-output procedures in procedures with an explicit Global => null and body with SPARK_Mode => Off.

```ada
with Ada.Text_IO;

function Foo return Integer is
   procedure Put_Line (Item : String) with
      Global => null;
   procedure Put_Line (Item : String) with
      SPARK_Mode => Off
   is
      begin
         Ada.Text_IO.Put_Line (Item);
   end Put_Line;

   begin
      Put_Line ("Hello, world!");
      return 0;
   end Foo;
```

- SPARK procedures that call input-output subprograms need to reflect these effects in their Global/Depends contract if they have one.

```ada
with Ada.Text_IO;

procedure Foo with
   Global => (Input => Var,
              In_Out => Ada.Text_IO.File_System)
is
   begin
      Ada.Text_IO.Put_Line (Var);
   end Foo;

procedure Bar is
   begin
      Ada.Text_IO.Put_Line (Var);
   end Bar;
```

In the examples above, procedure Foo and Bar have the same body, but their declarations are different. Global contracts have to be complete or not present at all. In the case of Foo, it has an Input contract on Var and an In_Out contract on File_System, an abstract state from Ada.Text_IO. Without the latter contract, a high message would be raised when running GNATprove. Global contracts will be automatically generated for Bar by flow analysis if this is user code. Both declarations are accepted by SPARK.
State Abstraction and Global Contracts

The abstract state File_System is used to model the memory on the system and the file handles (Line_Length, Col, etc.). This is explained by the fact that almost every procedure in Text_IO that actually modifies attributes of the File_Type parameter has in File_Type as a parameter and not in out. This would be inconsistent with SPARK rules without the abstract state.

All functions and procedures are annotated with Global, and Pre, Post if necessary. The Global contracts are most of the time In_Out for File_System, even in Put or Get procedures that update the current column and/or line. Functions have an Input global contract. The only functions with Global => null are the functions Get and Put in the generic packages that have a similar behaviour as sprintf and sscanf.

Functions and Procedures Removed in SPARK

Some functions and procedures are removed from SPARK usage because they are not consistent with SPARK rules:

1. Aliasing

   The functions Current_Input, Current_Output, Current_Error, Standard_Input, Standard_Output and Standard_Error are turned off in SPARK_Mode because they create aliasing, by returning the corresponding file.

   Set_Input, Set_Output and Set_Error are turned off because they also create aliasing, by assigning a File_Type variable to Current_Input or the other two.

   It is still possible to use Set_Input and the 3 others to make the code clearer. This is doable by calling Set_Input in a different subprogram whose body has SPARK_Mode => Off. However, it is necessary to check that the file is open and the mode is correct, because there are no checks made on procedures that do not take a file as a parameter (i.e. implicit, so it will write to/read from the current output/input).

2. Get_Line function

   The function Get_Line is disabled in SPARK because it is a function with side effects. Even with the Volatile_Function attribute, it is not possible to model its action on the files and global variables in SPARK. The function is very convenient because it returns an unconstrained string, but a workaround is possible by constructing the string with a buffer:

```
with Ada.Text_IO;

procedure Echo is
    Unb_Str : Unbounded_String := Null_Unbounded_String;
    Buffer : String (1 .. 1024);
    Last   : Natural := 1024;
begin
    while Last = 1024 loop
        Ada.Text_IO.Get_Line (Buffer, Last);
        exit when Last > Natural'Last - Length (Unb_Str);
        Unb_Str := Unb_Str & Buffer (1 .. Last);
    end loop;

    declare
        Str : String := To_String (Unb_Str);
    begin
        Ada.Text_IO.Put_Line (Str);
    end;
end Echo;
```
Errors Handling

Status_Error (due to a file already open/not open) and Mode_Error are fully handled.

Except for Layout_Error, which is a special case of a partially handled error and explained in a few lines below, all other errors are not handled:

- Use_Error is related to the external environment.
- Name_Error would require to check availability on disk beforehand.
- End_Error is raised when a file terminator is read while running the procedure.

For an Out_File, it is possible to set a Line_Length and Page_Length. When writing in this file, the procedures will add Line markers and Page markers each Line_Length characters or Page_Length lines respectively. Layout_Error occurs when trying to set the current column or line to a value that is greater than Line_Length or Page_Length respectively. This error is handled when using Set_Col or Set_Line procedures.

However, this error is not handled when no Line_Length or Page_Length has been specified, e.g., if the lines are unbounded, it is possible to have a Col greater than Count’Last and therefore have a Layout_Error raised when calling Col.

Not only the handling is partial, but it is also impossible to prove preconditions when working with two files or more. Since Line_Length etc. attributes are stored in the File_System, it is not possible to prove that the Line_Length of File_2 has not been modified when running any procedure that do input-output on File_1.
This chapter describes a simple use of the SPARK toolset on a program written completely in SPARK, within the GNAT Studio integrated development environment. All the tools may also be run from the command-line, see Command Line Invocation.

Note: If you’re using SPARK Discovery instead of SPARK Pro, some of the proofs in this tutorial may not be obtained automatically. See the section on Alternative Provers to install additional provers that are not present in SPARK Discovery.

6.1 Writing SPARK Programs

As a running example, we consider a naive searching algorithm for an unordered collection of elements. The algorithm returns whether the collection contains the desired value, and if so, at which index. The collection is implemented here as an array. We deliberately start with an incorrect program for package Search, in order to explain how the SPARK toolset can help correct these errors. The final version of the linear_search example is part of the Examples in the Toolset Distribution.

We start with creating a GNAT project file in search.gpr:

```gpr
project Search is
  for Source_Dirs use (".");

  package Compiler is
    for Default_Switches ("Ada") use ("-gnatwa");
  end Compiler;
end Search;
```

It specifies that the source code to inspect is in the current directory, and that the code should be compiled at maximum warning level (switch --gnatwa). GNAT projects are used by most tools in the GNAT toolsuite; for in-depth documentation of this technology, consult the GNAT User’s Guide. Documentation and examples for the SPARK language and tools are also available via the Help → SPARK menu in GNAT Studio.

The obvious specification of Linear_Search is given in file linear_search.ads, where we specify that the spec is in SPARK by using aspect SPARK_Mode.

```gpr
package Linear_Search
  with SPARK_Mode is
  type Index is range 1 .. 10;
  type Element is new Integer;
```
type Arr is array (Index) of Element;

function Search
(A : Arr;
Val : Element;
At_Index : out Index) return Boolean;
-- Returns True if A contains value Val, in which case it also returns
-- in At_Index the first index with value Val. Returns False otherwise.
end Linear_Search;

The implementation of Linear_Search is given in file linear_search.adb, where we specify that the body
is in SPARK by using aspect SPARK_Mode. It is as obvious as its specification, using a loop to go through the array
parameter A and looking for the first index at which Val is found, if there is such an index.

package body Linear_Search
with SPARK_Mode
is

function Search
(A : Arr;
Val : Element;
At_Index : out Index) return Boolean
is
Pos : Index := A'First;
begins
while Pos < A'Last loop
if A(Pos) = Val then
At_Index := Pos;
return True;
end if;
Pos := Pos + 1;
end loop;
return False;
end Search;
end Linear_Search;

We can check that the above code is valid Ada by using the Build > Check Semantic menu, which completes
without any errors or warnings:
6.1.1 Checking SPARK Legality Rules

Now, let us run GNATprove on this unit, using the SPARK → Examine File menu, so that it issues errors on SPARK code that violates SPARK rules:
It detects here that function `Search` is not in SPARK, because it has an `out` parameter:

The permission in Ada 2012 to have `out` parameters to functions is not allowed in SPARK, because it causes calls to have side-effects (assigning to their `out` parameters), which means that various calls in the same expression may be
conflicting, yielding different results depending on the order of evaluation of the expression.

We correct this problem by defining a record type `Search_Result` in `linear_search.ads` holding both the Boolean result and the index for cases when the value is found, and making `Search` return this type:

```
package Linear_Search
  with SPARK_Mode
is
  type Index is range 1 .. 10;
  type Element is new Integer;
  type Arr is array (Index) of Element;
  type Search_Result is record
    Found  : Boolean;
    At_Index : Index;
  end record;

  function Search
    (A : Arr;
     Val : Element) return Search_Result;
end Linear_Search;
```

The implementation of `Search` in `linear_search.adb` is modified to use this type:

```
package body Linear_Search
  with SPARK_Mode
is
  function Search
    (A : Arr;
     Val : Element) return Search_Result
  is
    Pos : Index := A'First;
    Res : Search_Result;
  begin
    while Pos < A'Last loop
      if A(Pos) = Val then
        Res.At_Index := Pos;
        Res.Found := True;
        return Res;
      end if;
      Pos := Pos + 1;
    end loop;
    Res.Found := False;
    return Res;
  end Search;
end Linear_Search;
```
6.1.2 Checking SPARK Initialization Policy

Re-running GNATprove on this unit, still using the SPARK → Examine File menu, now reports a different kind of error. This time it is the static analysis pass of GNATprove called flow analysis that detects an attempt of the program to return variable Res while it is not fully initialized, thus violating the initialization policy of SPARK:

```
Inside the GNAT Studio editor, we can click on the icon, either on the left of the message, or on line 23 in file linear_search.adb, to show the path on which Res.At._Index is not initialized:
```

![Image of GNAT Studio editor showing the path of the error message]
Another click on the icon makes the path disappear.

This shows that, when the value is not found, the component At_Index of the value returned is indeed not initialized. Although that is allowed in Ada, SPARK requires that all inputs and outputs of subprograms are completely initialized (and the value returned by a function is such an output). As a solution, we could give a dummy value to component At_Index when the search fails, but we choose here to turn the type Search_Result in linear_search.ads into a discriminant record, so that the component At_Index is only usable when the search succeeds:

```
type Search_Result (Found : Boolean := False) is record
  case Found is
  when True =>
    At_Index : Index;
  when False =>
    null;
  end case;
end record;
```

Then, in the implementation of Search in linear_search.adb, we change the value of the discriminant depending on the success of the search:

```
function Search
  (A : Arr;
   Val : Element) return Search_Result
is
  Pos : Index := A'First;
  Res : Search_Result;
begin
  while Pos < A'Last loop
  when True =>
    if A(Pos) = Val then
      Res := (Found => True,
              At_Index => Pos);
      return Res;
    end if;
    Pos := Pos + 1;
  end loop;
  return Res;
end Search;
```
function Search
   (A : Arr;
   Val : Element) return Search_Result
with
   Pre  => Val >= 0,
   Post  => (if Search'Result.Found then
               A (Search'Result.At_Index) = Val),
end Search;

function Value_Found_In_Range
   (A : Arr;
   Val : Element;
   Low, Up : Index) return Boolean
is
   for some J in Low .. Up => A(J) = Val);
end function Value_Found_In_Range;

function Search

Now re-running GNATprove on this unit, using the SPARK → Examine File menu, shows that there are no reads of uninitialized data.

6.1.3 Writing Functional Contracts

We now have a valid SPARK program. It is not yet very interesting SPARK code though, as it does not contain any contracts, which are necessary to be able to apply formal verification modularly on each subprogram, independently of the implementation of other subprograms. The precondition constrains the value of input parameters, while the postcondition states desired properties of the result of the function. See Preconditions and Postconditions for more details. Here, we can require in the precondition of Search in linear_search.ads that callers of Search always pass a non-negative value for parameter Val, and we can state that, when the search succeeds, the index returned points to the desired value in the array:

Notice the use of an if-expression in the postcondition to express an implication: if the search succeeds it implies that the value at the returned index is the value that was being searched for. Note also the use of Search'Result to denote the value returned by the function.

This contract is still not very strong. Many faulty implementations of the search would pass this contract, for example one that always fails (thus returning with Search'Result.Found = False). We could reinforce the postcondition, but we choose here to do it through a contract by cases, which adds further constraints to the usual contract by precondition and postcondition. We want to consider here three cases:

- the desired value is found at the first index (1)
- the desired value is found at other indexes (2 to 10)
- the desired value is not found in the range 1 to 10

In the first case, we want to state that the index returned is 1. In the second case, we want to state that the search succeeds. In the third case, we want to state that the search fails. We use a helper function Value_Found_In_Range in linear_search.ads to express that a value Val is found in an array A within given bounds Low and Up:

function Value_Found_In_Range
   (A : Arr;
   Val : Element;
   Low, Up : Index) return Boolean
is
   (for some J in Low .. Up => A(J) = Val);
end function Value_Found_In_Range;
(A : Arr; Val : Element) return Search_Result
with Pre => Val >= 0, Post => (if Search'Result.Found then A (Search'Result.At_Index) = Val),
Contract_Cases => (A(1) = Val => Search'Result.At_Index = 1,
Value_Found_In_Range (A, Val, 2, 10) => Search'Result.Found,
(for all J in Arr'Range => A(J) /= Val) => not Search'Result.Found);

Note that we express Value_Found_In_Range as an expression function, a function whose body consists of a single expression, which can be given in a specification file.

Note also the use of quantified expressions to express properties over collections: for some in Value_Found_In_Range expresses an existential property (there exists an index in this range such that ...), for all in the third contract case expresses a universal property (all indexes in this range are such that ...).

Each contract case consists of a guard (on the left of the arrow symbol) evaluated on subprogram entry, and a consequence (on the right of the arrow symbol) evaluated on subprogram exit. The special expression Search'Result may be used in consequence expressions. The three guards here should cover all possible cases, and be disjoint. When a contract case is activated (meaning its guard holds on entry), its consequence should hold on exit.

The program obtained so far is a valid SPARK program, which GNAT analyzes semantically without errors or warnings.

### 6.2 Testing SPARK Programs

We can compile the above program, and test it on a set of selected inputs. The following test program in file test_search.adb exercises the case where the searched value is present in the array and the case where it is not:

```ada
with Linear_Search; use Linear_Search;
with Ada.Text_IO; use Ada.Text_IO;

procedure Test_Search is
  A : constant Arr := (1, 5, 3, 8, 8, 2, 0, 1, 0, 4);
  Res : Search_Result;
begin
  Res := Search (A, 1);
  if Res.Found then
    if Res.At_Index = 1 then
      Put_Line ("OK: Found existing value at first index");
    else
      Put_Line ("not OK: Found existing value at other index");
    end if;
  else
    Put_Line ("not OK: Did not find existing value");
  end if;
  Res := Search (A, 6);
  if not Res.Found then
```
We can check that the implementation of `Linear_Search` passes this test by compiling and running the test program:

```
$ gnatmake test_search.adb
$ test_search
> OK: Found existing value at first index
> OK: Did not find non-existing value
```

**Note:** We use above the command-line interface to compile and run the test program `test_search.adb`. You can do the same inside GNAT Studio by selecting the menu `Project → Properties` and inside the panel `Main` of folder `Sources`, add `test_search.adb` as a main file. Then, click `OK`. To generate the `test_search` executable, you can now select the menu `Build → Project → test_search.adb` and to run the `test_search` executable, you can select the menu `Build → Run → test_search`.

But only part of the program was really tested, as the contract was not checked during execution. To check the contract at run time, we recompile with the switch `-gnata` (a for assertions, plus switch `-f` to force recompilation of sources that have not changed):

- a check is inserted that the precondition holds on subprogram entry
- a check is inserted that the postcondition holds on subprogram exit
- a check is inserted that the guards of contract cases are disjoint on subprogram entry (no two cases are activated at the same time)
- a check is inserted that the guards of contract cases are complete on subprogram entry (one case must be activated)
- a check is inserted that the consequence of the activated contract case holds on subprogram exit

Note that the evaluation of the above assertions may also trigger other run-time check failures, like an index out of bounds. With these additional run-time checks, an error is reported when running the test program:

```
$ gnatmake -gnata -f test_search.adb
$ test_search
> raised SYSTEMASSERTIONSASSERT_FAILURE : contract cases overlap for subprogram
```

**Note:** We use above the command-line interface to add compilation switch `-gnata` and force recompilation with switch `-f`. You can do the same inside GNAT Studio by selecting the menu `Project → Properties` and inside the panel `Ada` of the subfolder `Switches` of folder `Build`, select the checkbox `Enable assertions`. Then, click `OK`. To force recompilation with the new switch, you can now select the menu `Build → Clean → Clean All` followed by recompilation with `Build → Project → test_search.adb`. Then run the `test_search` executable with `Build → Run → test_search`.

It appears that two contract cases for `Search` are activated at the same time! More information can be generated at run time if the code is compiled with the switch `-gnateE`:
It shows here that the guards of the first and second contract cases hold at the same time. This failure in annotations can be debugged with gdb like a failure in the code (provided the program was compiled with appropriate switches, like `–g –O0`). The stack trace inside GNAT Studio shows that the error occurs on the first call to Search in the test program:

Indeed, the value 1 is present twice in the array, at indexes 1 and 8, which makes the two guards $A(1) = Val$ and $Value\_Found\_In\_Range\ (A, Val, 2, 10)$ evaluate to True. We correct the contract of Search in `linear_search.ads` by strengthening the guard of the second contract case, so that it only applies when the value is not found at index 1:

With this updated contract, the test passes again, but this time with assertions checked at run time:
The program obtained so far passes successfully a test campaign (of one test!) that achieves 100% coverage for all the common coverage criteria, once impossible paths have been ruled out: statement coverage, condition coverage, the MC/DC coverage used in avionics, and even the full static path coverage.

### 6.3 Proving SPARK Programs

Formal verification of SPARK programs is a two-step process:

1. the first step checks that flows through the program correctly implement the specified flows (if any), and that all values read are initialized.
2. the second step checks that the program correctly implement its specified contracts (if any), and that no run-time error can be raised.

Step 1 is implemented as a static analysis pass in the tool GNATprove, in flow mode. We have seen this flow analysis at work earlier (see Checking SPARK Initialization Policy). Step 2 is implemented as a deductive verification (a.k.a. proof) pass in the tool GNATprove, in the default all mode.

The difference between these two steps should be emphasized. Flow analysis in step 1 is a terminating algorithm, which typically takes 2 to 10 times as long as compilation to complete. Proof in step 2 is based on the generation of logical formulas for each check to prove, which are then passed on to automatic provers to decide whether the logical formula holds or not. The generation of logical formulas is a translation phase, which typically takes 10 times as long as compilation to complete. The automatic proof of logical formulas may take a very long time, or never terminate, hence the use of a timeout (1s at proof level 0) for each call to the automatic provers. It is this last step which takes the most time when calling GNATprove on a program, but it is also a step which can be completely parallelized (using switch \(-j\) to specify the number of parallel processes): each logical formula can be proved independently, so the more cores are available the faster it completes.

**Note:** The proof results presented in this tutorial may slightly vary from the results you obtain on your machine, as automatic provers may take more or less time to complete a proof depending on the platform and machine used.

Let us continue with our running example. This time we will see how step 2 works to prove contracts and absence of run-time errors, using the main mode all of GNATprove reached through the SPARK → Prove File menu.
Note: The proof panels presented in this tutorial correspond to an advanced user profile. A simpler proof panel is displayed when the basic user profile is selected (the default). You can switch to the advanced user profile in menu Edit → Preferences → SPARK, by changing the value of User profile from Basic to Advanced. See Running GNATprove from GNAT Studio for details.

We use the default settings and click on Execute. It completes in a few seconds, with a message stating that some checks could not be proved:
Note that there is no such message on the postcondition of Search, which means that it was proved. Likewise, there are no such messages on the body of Search, which means that no run-time errors can be raised when executing the function.

These messages correspond to checks done when exiting from Search. It is expected that not much can be proved at this point, given that the body of Search has a loop but no loop invariant, so the formulas generated for these checks assume the worst about locations modified in the loop. A loop invariant is a special pragma Loop_Invariant stating an assertion in a loop, which can be both executed at run-time like a regular pragma Assert, and used by GNATprove to summarize the effect of successive iterations of the loop. We need to add a loop invariant in linear_search.adb stating enough properties about the cumulative effect of loop iterations, so that the contract cases of Search become provable. Here, it should state that the value searched was not previously found:

```
pragma Loop_Invariant
(not Value_Found_In_Range (A, Val, A'First, Pos));
```

As stated above, this invariant holds exactly between the two statements in the loop in linear_search.adb (after the if-statement, before the increment of the index). Thus, it should be inserted at this place. With this loop invariant, two checks previously not proved are now proved, and a check previously proved becomes unproved:
The new unproved checks may seem odd, since all we did was add information in the form of a loop invariant. The reason is that we also removed information at the same time. By adding a loop invariant, we require GNATprove to prove iterations around the (virtual) loop formed by the following steps:

1. Take any context satisfying the loop invariant, which summarizes all previous iterations of the loop.
2. Execute the end of a source loop iteration (just the increment here).
3. Test whether the loop exits, and continue with values which do not exit.
4. Execute the start of a source loop iteration (just the if-statement here).
5. Check that the loop invariant still holds.

Around this virtual loop, nothing guarantees that the index \( \text{Pos} \) is below the maximal index at step 2 (the increment), so the range check cannot be proved. It was previously proved because, in the absence of a loop invariant, GNATprove proves iterations around the source loop, and then we get the information that, since the loop did not exit, its test \( \text{Pos} < \text{A'Last} \) is false, so the range check can be proved.

We solve this issue by setting the type of \( \text{Pos} \) in \text{linear_search.adb} to the base type of Index, which ranges past the last value of Index. (This may not be the simplest solution, but we use it here for the dynamics of this tutorial.)

\[
\text{Pos} : \text{Index'} \text{Base} := \text{A'First};
\]

And we add the range information for \( \text{Pos} \) to the loop invariant in \text{linear_search.adb}:

\[
\text{pragma Loop_Invariant}
\begin{align*}
\text{(Pos in A'Range} & \text{ and then)} \\
& \text{not Value_Found_In_Range (A, Val, A'First, Pos));}
\end{align*}
\]

This allows GNATprove to prove the range check, but not the contract:
This is actually progress! Indeed, the loop invariant should be strong enough to:

1. prove the absence of run-time errors in the loop and after the loop
2. prove that it is preserved from iteration to iteration
3. prove the postcondition and contract cases of the subprogram

So we have just achieved goal 1 above!

As we have modified the code and annotations, it is a good time to compile and run our test program, before doing any more formal verification work. This helps catch bugs early, and it’s easy to do! In particular, the loop invariant will be dynamically checked at each iteration through the loop. Here, testing does not show any problems:

```plaintext
$ gnatmake -gnata test_search.adb
$ test_search
> OK: Found existing value at first index
> OK: Did not find non-existing value
```

The next easy thing to do is to increase the timeout of automatic provers. Its default of 1s is deliberately low, to facilitate interaction with GNATprove during the development of annotations, but it is not sufficient to prove the more complex checks. Let’s increase it to 10s (or equivalently set the Proof level to 2 in the proof panel corresponding to a basic user profile), and rerun GNATprove:
The unproven check remains in the contract cases of Linear_Search. The next step is to use the SPARK → Prove Line contextual menu available on line 35:

We select the Progressively split value for choice Proof strategy in the window raised in order to
maximize proof precision (or equivalently set the Proof level to 3 in the proof panel corresponding to a basic user profile), and click on \textbf{Execute}:

This runs GNATprove only on the checks that originate from line 35, in a special mode which considers separately individual execution paths if needed. The check is still not proved, but GNAT Studio now displays an icon, either on the left of the message, or on line 35 in file \texttt{linear_search.ads}, to show the path on which the contract case is not proved:
This corresponds to a case where the implementation of Search does not find the searched value, but the guard of the second contract case holds, meaning that the value is present in the range 2 to 10. Looking more closely at the path highlighted, we can see that the loop exits when Pos = A'Last, so the value 10 is never considered! We correct this bug by changing the loop test in linear_search.adb from a strict to a non-strict comparison operation:

```
while Pos <= A'Last loop
```

On this modified code, we rerun GNATprove on line 35, checking the box Report checks proved to get information even when a check is proved. The reassuring green color (and the accompanying info message) show that the check was proved this time:
As usual after code changes, we rerun the test program, which shows no errors. Rerunning GNATprove on the complete file shows no more unproved checks. The Linear_Search unit has been fully proved. To see all the checks that were proved, we can rerun the tool with box `Report checks proved checked`, which displays the results previously computed:
Note that one thing that was not proved is that `Search` terminates. As it contains a while-loop, it could loop forever. To prove that it is not the case, we add a loop variant, which specifies a quantity varying monotonically with each iteration. Since this quantity is bounded by its type, and we have proved absence of run-time errors in `Search`, proving this monotonicity property also shows that there cannot be an infinite number of iterations of the loop. The natural loop variant for `Search` is the index `Pos`, which increases at each loop iteration:

```
pragma Loop_Variant (Increases => Pos);
```

With this line inserted after the loop invariant in `linear_search.adb`, the test program still runs without errors (it checks dynamically that the loop variant is respected), and the program is still fully proved. Here is the final version of `Linear_Search`, with the complete annotations:

```
package Linear_Search
with SPARK_Mode
is
  type Index is range 1 .. 10;
  type Element is new Integer;
  type Arr is array (Index) of Element;
  type Search_Result (Found : Boolean := False) is record
    case Found is
      when True =>
        At_Index : Index;
      when False =>
        null;
    end case;
  end record;
```

The final version of the `linear_search` example is part of the *Examples in the Toolset Distribution*. This concludes...
our tutorial on the SPARK toolset.
The GNATprove tool is packaged as an executable called `gnatprove`. Like other tools in GNAT toolsuite, GNATprove is based on the structure of GNAT projects, defined in `.gpr` files.

A crucial feature of GNATprove is that it interprets annotations exactly like they are interpreted at run time during tests. In particular, their executable semantics includes the verification of run-time checks, which can be verified statically with GNATprove. GNATprove also performs additional verifications on the specification of the expected behavior itself, and its correspondence to the code.

### 7.1 How to Run GNATprove

#### 7.1.1 Setting Up a Project File

**Basic Project Set Up**

If not already done, create a GNAT project file (`.gpr`), as documented in the GNAT User’s Guide, section *GNAT Project Manager*. See also *Project Attributes* for optional project attributes to specify the proof directory and other GNATprove switches in the project file directly.

Note that you can use the project wizard from GNAT Studio to create a project file interactively, via the menu *File → New Project*…. In the dialog, see in particular the default option (*Single Project*).

If you want to get started quickly, and assuming a standard naming scheme using `.ads/.adb` lower case files and a single source directory, then your project file will look like:

```plaintext
project My_Project is
  for Source_Dirs use ".";
end My_Project;
```

saved in a file called `my_project.gpr`.

**Having Different Switches for Compilation and Verification**

In some cases, you may want to pass different compilation-level switches to GNAT and GNATprove, for example use warning switches only for compilation, in the same project file. In that case, you can use a scenario variable to specify different switches for compilation and verification. We recommend to use the predefined `GPR_TOOL` variable for this purpose:

```plaintext
project My_Project is
  Mode := External ("GPR_TOOL");
```
package Compiler is
  case Mode is
    when "gnatprove" =>
      for Switches ("Ada") use ...
    when others =>
      for Switches ("Ada") use ...
  end case;
end Compiler;
end My_Project;

With the above project, compilation will be automatically done in the “normal” mode (the “others” branch above):

gprbuild -P my_project.gpr

while GNATprove automatically sets the GPR_TOOL variable to the gnatprove value:

gnatprove -P my_project.gpr

Other tools set the value of this variable to other values. See the documentation of other AdaCore tools to know more about this.

Note that before SPARK Pro 20, the GPR_TOOL was not set automatically by the tool. You can set it manually in this case:

gnatprove -P my_project.gpr -XGPR_TOOL=gnatprove

7.1.2 Running GNATprove from the Command Line

GNATprove can be run from the command line as follows:

gnatprove -P <project-file.gpr>

In the appendix, section Command Line Invocation, you can find an exhaustive list of switches; here we only give an overview over the most common uses. Note that GNATprove cannot be run without a project file.

There are essentially three common ways you can select the files which will be analyzed by GNATprove:

- Analyze everything:

  gnatprove -P <project-file.gpr> -U

  With switch \texttt{-U}, all units of all projects in the project tree are analyzed. This includes units that are not used yet. This is usually what you want to use for an overnight analysis of a complex project.

- Analyze this project:

  gnatprove -P <project-file.gpr>

  All main units in the project and all units they (recursively) depend on are analyzed. If there are no main units specified, analyze all files in the project.

  This is what you want to use for the analysis of a particular executable only, or if you want to analyze different executables within a complex project with different options.

- Analyze files:
gnatprove -P <project-file.gpr> [-u] FILES...

If -u is specified, we only analyze the given files. If -u is not specified, we also analyze all units these files (recursively) depend on.

This is intended for the day-to-day command-line or IDE use of GNATprove when implementing a project.

GNATprove consists of two distinct analyses: flow analysis and proof. Flow analysis checks the correctness of aspects related to data flow (Global, Depends, Abstract_State, Initializes, and refinement versions of these), and verifies the initialization of variables. Proof verifies the absence of run-time errors and the correctness of assertions such as Pre and Post aspects. Using the switch --mode=<mode>, whose possible values are check, check_all, flow, prove all, stone, bronze, silver and gold, you can choose which analysis is performed:

- In mode check, GNATprove partially checks that the program does not violate SPARK restrictions. The benefit of using this mode prior to mode check_all is that it is much faster, as it does not require the results of flow analysis.

- In mode check_all (stone is a synonym for this mode), GNATprove fully checks that the program does not violate SPARK restrictions, including checks not performed in mode check like the absence of side-effects in functions. Mode check_all includes mode check.

- In mode flow (bronze is a synonym for this mode), GNATprove checks that no uninitialized data are read in the program, and that the specified data dependencies and flow dependencies are respected in the implementation. Mode flow includes mode check_all. This phase is called flow analysis.

- In mode prove , GNATprove checks that the program is free from run-time errors, and that the specified functional contracts are respected in the implementation. Mode prove includes mode check_all, as well as the part of mode flow that checks that no uninitialized data are read, to guarantee soundness of the proof results. This phase is called proof.

- In the default mode all, GNATprove does both flow analysis and proof. The silver and gold modes are synonyms for this mode.

Using the option --limit-line= one can limit proofs to a particular file and line of an Ada file. For example, if you want to prove only line 12 of file example.adb, you can add the option --limit-line=example.adb:12 to the call to GNATprove. Using the option --limit-subp= one can limit proofs to a subprogram declared in a particular file at a particular line. Using --limit-region= one can limit proofs to a range of lines in a particular file. For example, --limit-region=example.adb:12:14 will limit analysis to lines 12 to 14 in example.adb.

A number of options exist to influence the behavior for proof. Internally, the prover(s) specified with option --prover is/are called repeatedly for each check or assertion. Using the options --timeout and --memlimit, one can change the maximal time and memory that is allocated to each prover to prove each check or assertion. Using the option --steps (default: 100), one can set the maximum number of reasoning steps that the prover is allowed to perform before giving up. The steps option should be used when predictable results are required, because the results with a timeout and memory limit may differ depending on the computing power, current load or platform of the machine. The option -j activates parallel compilation and parallel proofs. With -jnnn, at most nnn cores can be used in parallel. With the special value -j0, at most N cores can be used in parallel, when N is the number of cores on the machine.

Note: When the project has a main file, or a file is passed as starting point to gnatprove, and the dependencies in the project are very linear (unit A depends only on unit B, which depends only on unit C, etc), then even when the -j switch is used, gnatprove may only consider one file at a time. This problem can be avoided by additionally using the -U switch.
Note: The –memlimit switch is currently ineffective on the Mac OS X operating system, due to limitations of the underlying system call on that system.

The way checks are passed to the prover can also be influenced using the option --proof. By default, the prover is invoked a single time for each check or assertion (mode per_check). This can be changed using mode per_path to invoke the prover for each path that leads to the check. This option usually takes much longer, because the prover is invoked much more often, but may give better proof results. Finally, in mode progressive, invoking the prover a single time on the entire check is tried, and only if the check is not proved, then other techniques that progressively consider each path in isolation are tried.

The proof mode set with --proof can be extended with a qualifier all or lazy, so that the entire switch may for example look like this: --proof=progressive:all. With this qualifier, one can select if proof should stop at the first unproved formula (to save time) for a check or should continue attempting to prove the other formulas related to the same check (typically to identify more precisely which formulas are left unproved, which can be then be handled with manual proof). The former is most suited for fully automatic proof, it is the default value, and can be explicitly selected with lazy. The latter is most suited for combination of automatic and manual proof and can be selected with all.

Instead of setting individually switches that influence the speed and power of proof, one may use the switch --level, which corresponds to predefined proof levels, from the faster level 0 to the more powerful level 4. More precisely, each value of --level is equivalent to directly setting a collection of other switches discussed above:

- --level=0 is equivalent to --prover=cvc4 --timeout=1 --memlimit=1000 --steps=0
- --level=1 is equivalent to --prover=cvc4,z3,altergo --timeout=1 --memlimit=1000 --steps=0
- --level=2 is equivalent to --prover=cvc4,z3,altergo --timeout=5 --memlimit=1000 --steps=0
- --level=3 is equivalent to --prover=cvc4,z3,altergo --timeout=20 --memlimit=2000 --steps=0
- --level=4 is equivalent to --prover=cvc4,z3,altergo --timeout=60 --memlimit=2000 --steps=0

If both --level is set and an underlying switch is set (--prover, --timeout, or --proof), the value of the latter takes precedence over the value set through --level.

Note that using --level does not provide results that are reproducible across different machines. For nightly builds or shared repositories, consider using the --steps or --replay switches instead. The number of steps required to proved an example can be accessed by running GNATprove with the option --report=statistics.

GNATprove also supports using the static analysis tool CodePeer as an additional source for the proof of checks, by specifying the command line option --codepeer=on (see Using CodePeer Static Analysis).

By default, GNATprove avoids reanalyzing unchanged files, on a per-unit basis. This mechanism can be disabled with the option -f.

When GNATprove proves a check, it stores this result in a session file, along with the required time and steps for this check to be proved. This information can be used to replay the proofs, to check that they are indeed correct. If such session files are present, and when GNATprove is invoked using the --replay option, it will attempt such a replay, using the same prover that was able to prove the check last time, with some slightly higher time and step limit. In this mode, the user-provided steps and time limits are ignored. If the --prover option is not provided, GNATprove will attempt to replay all checks, otherwise it will replay only the proofs proved by one of the specified provers. If all replays succeeded, GNATprove output will be exactly the same as a normal run of GNATprove. If a replay failed, the corresponding check will be reported as not proved. If a replay has not been attempted because the corresponding prover is not available (a third-party prover that is not configured, or the user has selected other provers using the
--prover option), a warning will be issued that the proof could not be replayed, but the check will still be marked as proved.

By default, GNATprove stops at the first unit where it detect errors (violations of Ada or SPARK legality rules). The option --k can be used to get GNATprove to issue errors of the same kind for multiple units. If there are any violations of Ada legality rules, GNATprove does not attempt any analysis. If there are violations of SPARK legality rules, GNATprove stops after the checking phase and does not attempt flow analysis or proof.

GNATprove returns with a non-zero exit status when an error is detected. This includes cases where GNATprove issues unproved check messages when switch --checks-as-errors is used, as well as cases where GNATprove issues warnings when switch --warnings=error is used. In such cases, GNATprove also issues a message about termination in error. Otherwise, GNATprove returns with an exit status of zero, even when unproved check messages and warnings are issued.

7.1.3 Using the GNAT Target Runtime Directory

If you are using GNAT as your target compiler and explicitly specify a runtime and target to use in your project, for instance:

```plaintext
for Target use "arm-eabi";
for Runtime ("Ada") use "ravenscar-sfp-stm32f4";
```

GNATprove will take such setting into account and will use the GNAT runtime directory, as long as your target compiler is found in your PATH environment variable. Note that you will need to use a matching version of GNAT and SPARK (e.g. GNAT 18.2 and SPARK 18.2).

The handling of runtimes of GNATprove is in fact unified with that of the GNAT compiler. For details, see “GNAT User’s Guide Supplement for Cross Platforms”, Section 3. If you specify a target, note that GNATprove requires additional configuration, see the section Specifying the Target Architecture and Implementation-Defined Behavior.

If you’re using GNAT Common Code Generator to generate C code from SPARK, you can specify the target and runtime as follows:

```plaintext
for Target use "c";
for Runtime ("Ada") use "ccg";
```

7.1.4 Specifying the Target Architecture and Implementation-Defined Behavior

A SPARK program is guaranteed to be unambiguous, so that formal verification of properties is possible. However, some behaviors (for example some representation attribute values like the Size attribute) may depend on the compiler used. By default, GNATprove adopts the same choices as the GNAT compiler. GNATprove also supports other compilers by providing special switches:

- --gnateT for specifying the target configuration
- --pedantic for warnings about possible implementation-defined behavior

Note that, even with switch --pedantic, GNATprove only detects some implementation-defined behaviors. For more details, see the dedicated section on how to Ensure Portability of Programs.

Note that GNATprove will always choose the smallest multiple of 8 bits for the base type, which is a safe and conservative choice for any Ada compiler.
Target Parameterization

If you specify the Target and Runtime attributes in your project file or via the --target and --RTS switches, GNATprove attempts to configure automatically the target dependent values such as endianness or sizes and alignments of standard types. If this automatic configuration fails, GNATprove outputs a warning and assumes that the compilation target is the same as the host on which it is run.

You can however configure the target dependent values manually. In addition to specifying the target and runtime via the project file or the commandline, you need to add the following to your project file, under a scenario variable as seen in Having Different Switches for Compilation and Verification:

```ada
project My_Project is
[...]
package Builder is
case Mode is
  when "Compile" =>
    ...
  when "Analyze" =>
    for Global_Compilation_Switches ("Ada") use ("-gnateT=" & My_Project ↪ 'Project_Dir & "/target.atp");
  end case;
end Builder;
end My_Project;
```

where target.atp is a file stored here in the same directory as the project file my_project.gpr, which contains the target parametrization. The format of this file is described in the GNAT User’s Guide as part of the -gnateT switch description.

Target parameterization can be used:

- to specify a target different than the host on which GNATprove is run, when cross-compilation is used. If GNAT is the cross compiler and the automatic configuration fails, the configuration file can be generated by calling the compiler for your target with the switch -gnatet=target.atp. Otherwise, the target file should be generated manually.
- to specify the parameters for a different compiler than GNAT, even when the host and target are the same. In that case, the target file should be generated manually.

Here is an example of a configuration file for a bare board PowerPC 750 processor configured as big-endian:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bits_BE</td>
<td>1</td>
</tr>
<tr>
<td>Bits_Per_Unit</td>
<td>8</td>
</tr>
<tr>
<td>Bits_Per_Word</td>
<td>32</td>
</tr>
<tr>
<td>Bytes_BE</td>
<td>1</td>
</tr>
<tr>
<td>Char_Size</td>
<td>8</td>
</tr>
<tr>
<td>Double_Float_Alignment</td>
<td>0</td>
</tr>
<tr>
<td>Double_Scalar_Alignment</td>
<td>0</td>
</tr>
<tr>
<td>Double_Size</td>
<td>64</td>
</tr>
<tr>
<td>Float_Size</td>
<td>32</td>
</tr>
<tr>
<td>Float_Words_BE</td>
<td>1</td>
</tr>
<tr>
<td>Int_Size</td>
<td>32</td>
</tr>
<tr>
<td>Long_Double_Size</td>
<td>64</td>
</tr>
<tr>
<td>Long_Long_Size</td>
<td>64</td>
</tr>
<tr>
<td>Long_Size</td>
<td>32</td>
</tr>
<tr>
<td>Maximum_Alignment</td>
<td>16</td>
</tr>
<tr>
<td>Max_Unaligned_Field</td>
<td>64</td>
</tr>
<tr>
<td>Pointer_Size</td>
<td>32</td>
</tr>
<tr>
<td>ShortEnums</td>
<td>0</td>
</tr>
<tr>
<td>Short_Size</td>
<td>16</td>
</tr>
</tbody>
</table>
7.1.5 Using CodePeer Static Analysis

Note: CodePeer is only available in SPARK Pro. It is not available in the following SPARK releases:

- the Community release
- SPARK Discovery
- on the MacOS X operating system

CodePeer is a static analysis tool developed and commercialized by AdaCore (see http://www.adacore.com/codepeer). GNATprove supports using CodePeer as an additional source for the proof of checks, by specifying the command line option `--codepeer=on`. CodePeer will be run before automatic provers. If it proves a check, GNATprove will not attempt to run another prover on this check.

When run by GNATprove, CodePeer does not attempt to generate preconditions, and relies instead on user-provided preconditions for its analysis. CodePeer analysis inside GNATprove is sound, in that it does not allow to prove a check that could fail. CodePeer analysis may allow to prove more properties than the strict contract-based reasoning performed in SPARK allow in general:

1. CodePeer generates a sound approximation of data dependencies for subprograms based on the implementation of subprograms and the call-graph relating subprograms. Hence CodePeer may be able to prove properties which cannot be deduced otherwise based on too coarse user-provided data dependencies.

2. CodePeer generates a sound approximation of loop invariants for loops. Hence CodePeer may be able to prove properties which cannot be deduced otherwise based on imprecise loop invariants, or in absence of a loop invariant.

3. CodePeer ignores the `SPARK_Mode` pragma and aspects; in particular it uses information that is hidden from SPARK using `pragma SPARK_Mode(Off)` or the equivalent aspect.

In addition, CodePeer is using the same choice as GNAT compiler for the rounding of fixed-point multiplication and division. This makes it more precise for the analysis of code compiled with GNAT. If some code using fixed-point arithmetic is compiled with another compiler than GNAT, and the code uses fixed-point multiplication or division, the choice of rounding made in CodePeer may not be suitable, in which case `--codepeer=on` should not be used.

CodePeer analysis is particularly interesting when analyzing code using floating-point computations, as CodePeer is both fast and precise for proving bounds of floating-point operations.

7.1.6 Running GNATprove from GNAT Studio

GNATprove can be run from GNAT Studio. When GNATprove is installed and found on your PATH, a SPARK menu is available with the following entries:
<table>
<thead>
<tr>
<th>Submenu</th>
<th>Action</th>
</tr>
</thead>
<tbody>
<tr>
<td>Examine All</td>
<td>This runs GNATprove in flow analysis mode on all mains and the units they depend on in the project.</td>
</tr>
<tr>
<td>Examine All Sources</td>
<td>This runs GNATprove in flow analysis mode on all files in the project.</td>
</tr>
<tr>
<td>Examine File</td>
<td>This runs GNATprove in flow analysis mode on the current unit, its body and any subunits.</td>
</tr>
<tr>
<td>Prove All</td>
<td>This runs GNATprove on all mains and the units they depend on in the project.</td>
</tr>
<tr>
<td>Prove All Sources</td>
<td>This runs GNATprove on all files in the project.</td>
</tr>
<tr>
<td>Prove File</td>
<td>This runs GNATprove on the current unit, its body and any subunits.</td>
</tr>
<tr>
<td>Show Report</td>
<td>This displays the report file generated by GNATprove.</td>
</tr>
<tr>
<td>Clean Proofs</td>
<td>This removes all files generated by GNATprove.</td>
</tr>
</tbody>
</table>

The three “Prove...” entries run GNATprove in the mode given by the project file, or in the default mode “all” if no mode is specified.

The menus SPARK → Examine/Prove All run GNATprove on all main files in the project, and all files they depend on (recursively). Both main files in the root project and in projects that are included in the root project are considered. The menus SPARK → Examine/Prove All Sources run GNATprove on all files in all projects. On a project that has neither main files nor includes other projects, menus SPARK → Examine/Prove All and SPARK → Examine/Prove All Sources are equivalent.

Keyboard shortcuts for these menu items can be set using the Edit → Preferences dialog in GNAT Studio, and opening the General → Key Shortcuts section.

**Note:** The changes made by users in the panels raised by these submenus are persistent from one session to the other. Be sure to check that the selected checkboxes and additional switches that were previously added are still appropriate.

When editing an Ada file, GNATprove can also be run from a SPARK contextual menu, which can be obtained by a right click:

<table>
<thead>
<tr>
<th>Submenu</th>
<th>Action</th>
</tr>
</thead>
<tbody>
<tr>
<td>Examine File</td>
<td>This runs GNATprove in flow analysis mode on the current unit, its body and any subunits.</td>
</tr>
<tr>
<td>Examine Subprogram</td>
<td>This runs GNATprove in flow analysis mode on the current subprogram.</td>
</tr>
<tr>
<td>Prove File</td>
<td>This runs GNATprove on the current unit, its body and any subunits.</td>
</tr>
<tr>
<td>Prove Subprogram</td>
<td>This runs GNATprove on the current subprogram.</td>
</tr>
<tr>
<td>Prove Line</td>
<td>This runs GNATprove on the current line.</td>
</tr>
<tr>
<td>Prove Selected Region</td>
<td>This runs GNATprove on the currently selected region.</td>
</tr>
<tr>
<td>Prove Check</td>
<td>This runs GNATprove on the current failing condition. GNATprove must have been run at least once for this option to be available in order to know which conditions are failing.</td>
</tr>
</tbody>
</table>

Except from Examine File and Prove File, all other submenus are also applicable to code inside generic units, in which case the corresponding action is applied to all instances of the generic unit in the project. For example, if a generic unit is instantiated twice, selecting Prove Subprogram on a subprogram inside the generic unit will apply proof to the two corresponding subprograms in instances of the generic unit.

The menus SPARK → Examine ... open a panel which allows setting various switches for GNATprove’s analysis. The main choice offered in this panel is to select the mode of analysis, among modes check, check_all and flow (the default).

The menus SPARK → Prove ... open a panel which allows setting various switches for GNATprove’s analysis. By default, this panel offers a few simple choices, like the proof level (see description of switch --level in Running
GNATprove from the Command Line). If the user changes its User profile for SPARK (in the SPARK section of the Preferences dialog - menu Edit → Preferences) from Basic to Advanced, then a more complex panel is displayed for proof, with more detailed switches.

GNATprove project switches can be edited from the panel GNATprove (menu Edit → Project Properties, in the Build → Switches section of the dialog).

When proving a check fails on a specific path through a subprogram (for both checks verified in flow analysis and in proof), GNATprove may generate path information for the user to see. The user can display this path in GNAT Studio by clicking on the icon to the left of the failed proof message, or to the left of the corresponding line in the editor. The path is hidden again when re-clicking on the same icon.

For checks verified in proof, GNATprove may also generate counterexample information for the user to see (see Understanding Counterexamples). The user can display this counterexample in GNAT Studio by clicking on the icon to the left of the failed proof message, or to the left of the corresponding line in the editor. The counterexample is hidden again when re-clicking on the same icon.

A monospace font with ligature like Fira Code (https://github.com/tonsky/FiraCode) or Hasklig (https://github.com/i-tu/Hasklig) can be separately installed and selected to make contracts more readable inside GNAT Studio or GNATbench. See the following screenshot which shows how symbols like => (arrow) or >= (greater than or equal) are displayed in such a font:

```
10  function LCP (A : Text; X, Y : Integer) return Natural with
11  SPARK_Mode,
12  Pre ⇒ X in A'Range and then Y in A'Range,
13  Post ⇒
14      (for all K in 0 .. LCP'Result - 1 ⇒ A (X + K) = A (Y + K))
15      and then (X + LCP'Result = A'Last + 1
16      or else Y + LCP'Result = A'Last + 1
17      or else A (X + LCP'Result) /= A (Y + LCP'Result)),
18      Contract_Cases ⇒
19      (A (X) /= A (Y) ⇒ LCP'Result = 0,
20      X = Y ⇒ LCP'Result = A'Last - X + 1,
21      others ⇒ LCP'Result ≥ 0);
```

7.1.7 Running GNATprove from GNATbench

GNATprove can be run from GNATbench. When GNATprove is installed and found on your PATH, a SPARK menu is available with the following entries:

<table>
<thead>
<tr>
<th>Submenu</th>
<th>Action</th>
</tr>
</thead>
<tbody>
<tr>
<td>Examine All</td>
<td>This runs GNATprove in flow analysis mode on all mains and the units they depend on in the project.</td>
</tr>
<tr>
<td>Examine All Sources</td>
<td>This runs GNATprove in flow analysis mode on all files in the project.</td>
</tr>
<tr>
<td>Examine File</td>
<td>This runs GNATprove in flow analysis mode on the current unit, its body and any subunits.</td>
</tr>
<tr>
<td>Prove All</td>
<td>This runs GNATprove on all mains and the units they depend on in the project.</td>
</tr>
<tr>
<td>Prove All Sources</td>
<td>This runs GNATprove on all files in the project.</td>
</tr>
<tr>
<td>Prove File</td>
<td>This runs GNATprove on the current unit, its body and any subunits.</td>
</tr>
<tr>
<td>Show Report</td>
<td>This displays the report file generated by GNATprove.</td>
</tr>
<tr>
<td>Clean Proofs</td>
<td>This removes all files generated by GNATprove.</td>
</tr>
</tbody>
</table>

The three “Prove...” entries run GNATprove in the mode given by the project file, or in the default mode “all” if no mode is specified.
The menus SPARK → Examine/Prove All run GNATprove on all main files in the project, and all files they depend on (recursively). Both main files in the root project and in projects that are included in the root project are considered. The menus SPARK → Examine/Prove All Sources run GNATprove on all files in all projects. On a project that has neither main files nor includes other projects, menus SPARK → Examine/Prove All and SPARK → Examine/Prove All Sources are equivalent.

**Note:** The changes made by users in the panels raised by these submenus are persistent from one session to the other. Be sure to check that the selected checkboxes and additional switches that were previously added are still appropriate.

When editing an Ada file, GNATprove can also be run from a SPARK contextual menu, which can be obtained by a right click:

<table>
<thead>
<tr>
<th>Submenu</th>
<th>Action</th>
</tr>
</thead>
<tbody>
<tr>
<td>Examine File</td>
<td>This runs GNATprove in flow analysis mode on the current unit, its body and any subunits.</td>
</tr>
<tr>
<td>Examine Subprogram</td>
<td>This runs GNATprove in flow analysis mode on the current subprogram.</td>
</tr>
<tr>
<td>Prove File</td>
<td>This runs GNATprove on the current unit, its body and any subunits.</td>
</tr>
<tr>
<td>Prove Subprogram</td>
<td>This runs GNATprove on the current subprogram.</td>
</tr>
<tr>
<td>Prove Line</td>
<td>This runs GNATprove on the current line.</td>
</tr>
</tbody>
</table>

### 7.1.8 GNATprove and Manual Proof

When automated provers fail to prove some condition that is valid, the validity may be proved using manual proof inside GNAT Studio or an external interactive prover.

In the appendix, section *Alternative Provers*, is explained how to use different provers than the one GNATprove uses as default.

**Calling an Interactive Prover From the Command Line**

When the prover used by GNATprove is configured as interactive, for each analysed condition, either:

- It is the first time the prover is used on the condition then a file (containing the condition as input to the specified prover) is created in the project’s proof directory (see *Project Attributes*). GNATprove outputs a message concerning this condition indicating the file that was created. The created file should be edited by the user in order to prove the condition.
- The prover has already been used on this condition and the editable file exists. The prover is run on the file and the success or failure of the proof is reported in the same way it is done with the default prover.

**Note:** Once a manual proof file is created and has been edited by the user, in order to run the prover on the file, the same prover must be once again specified to GNATprove. Once the condition is proved, the result will be saved in the why3 session so GNATprove won’t need to be specified the prover again to know that the condition is valid.

Analysis with GNATprove can be limited to a single condition with the **--limit-line** option:

```
gnatprove -P <project-file.gpr> --prover=<prover> --limit-line=<file>:<line>:<column>:<check-kind>
```

Please use the output of gnatprove **--list-categories** to determine the **check-kind** to be provided in this command.
Calling an Interactive Prover From GNAT Studio

After running GNATprove with proof mode, the menu "SPARK → Prove Check" is available by right-clicking on a check message in the location tab or by right-clicking on a line that fails because of a single condition (i.e. there is only one check in the output of GNATprove concerning this line).

In the dialog box, the field “Alternate prover” can be filled to use another prover than Alt-Ergo. If the alternative prover is configured as “interactive”, after the execution of "SPARK → Prove Check", GNAT Studio opens the manual proof file with the editor corresponding to the prover under the condition that an editor is specified in the configuration of the alternative prover.

Once the editor is closed, GNAT Studio re-executes "SPARK → Prove Check". The user should verify the same alternative prover as before is still specified. After execution, GNAT Studio will offer to re-edit the file if the proof fails.

Manual Proof Within GNAT Studio

A manual proof system is integrated into GNAT Studio. It allows the user to directly visualize the verification condition, apply simple proof steps on it, and call provers to discharge it. The proof system is available after running GNATprove via one of the "Prove ..." menus. By right-clicking on a check message in the location tab, and selecting the menu "SPARK → Start Manual Proof" the proof system starts. It consists of the Manual Proof console, the Proof Tree and the current Verification Condition being dealt with.

The user interacts with the system mainly using the manual proof console. Three types of commands can be entered:

- Some helper commands such as help, list-provers and list-transforms are available.
- When a prover name (type list-provers to see a list of the available provers) is entered, the corresponding prover is run on the verification condition that is selected in the proof tree.
- A transformation (see list-transforms and the below table for the available transformations) can modify the proof tree. A transformation applies to a verification condition or goal and may produce several new subgoals. For example, the transformation assert allows the user to assert an auxiliary fact. This transformation will create two subgoals, one to prove the assertion, and the other to prove that the assertion implies the previous goal.

The Manual proof system can be quit by selecting "SPARK → Exit Manual Proof" in the menu. A pop-up window asks if the user wants to save the session. It is recommended to close it using the menu because it makes sure to close everything related to manual proof. A tutorial to the proof system can be found in Manual Proof Using GNAT Studio.

List of Useful Transformations and Commands for Manual Proof

The transformations all contain a specific documentation through the list-transforms command and help transform_name command. The most useful transformations/commands are the following:

- apply: apply an hypothesis to the current goal. For example: H : x > 0 -> not x = 0 can be applied on the goal G : not x = 0. After the application you will be left to prove a new goal x > 0.
- assert: adds a new lemma you can use for proving the current Verification Condition. For example: assert x = 0 will generate two new subgoals. In the first one you have to prove that x is indeed equal to 0. In the second one, you can use this hypothesis.
- case: takes a formula and perform an analysis by case on its boolean value. You will have to prove your Verification Condition once with this formula asserted to true and once asserted to false.
- clean: removes unsuccessful proof attempts below proved goals.
• **clear_but**: removes all hypotheses except the one provided by the user as argument. Removing unused context helps the provers. For example, `clear_but H,H2,h` will remove everything but hypotheses H, H2, and h.

• **compute_in_goal**: performs possible computations in goal.

• **destruct**: destruct the head constructor of a formula (∨, ∧, or →). With H: A ∨ B, applying `destruct H` make two new hypotheses (H: A and H1: B). With H: A ∧ B, applying `destruct H` duplicates the goal which has to be proved with H: A and H: B independently. With H: A → B, `destruct H` creates a new subgoal for A and simplify to H: B in the current one.

• **eliminate_epsilon**: sometimes the goal appears as epsilon [...]. This transforms epsilons into adapted logic.

• **exists**: allows the user to provide a term that instantiates a goal starting with an existential.

• **help**: with no arguments, return basic commands that can be used. If a transformation is given as argument, it displays a small description of the transformation.

• **induction**: performs an induction on the unbounded integer specified.

• **instantiate**: instantiates a forall quantification at the head of an hypothesis with a term given by the user (a list of terms can be provided).

• **intros**: introduces a list of constants/hypotheses. This transformation should not be necessary but it can be used to rename constants/hypotheses.

• **left**: in a goal, transforms A ∨ B into A.

• **list-provers**: gives a list of the provers available on your machine. You should have at least altergo.

• **list-transforms**: list transformations.

• **pose**: defines a new constant equal to a given term.

• **print**: prints the definition of a name.

• **remove**: removes a list of hypotheses.

• **replace**: replace a term by another and create a subgoal asking the user to show that they are equivalent.

• **rewrite**: rewrites an equality in a goal or hypothesis. For example, with H: x = 0 and goal y = x, `rewrite H` transforms the goal into y = 0.

• **right**: in a goal, transforms A ∨ B into B.

• **search**: search all occurrences of a name in the context.

• **split_**: a set of transformations that split the goals/hypotheses. For example, `split_goal_wp` transforms the goal A ∨ B into two new subgoals A and B.

• **subst**: try to find an equality that could be used for a given constant and replace each occurrence of this constant by the other side of the equality. It then removes said constant.

• **subst_all**: do all possible substitutions.

• **unfold**: unfolds the definition of a function in an hypothesis or a goal.

**Recommendations and Tips for Manual Proof**

• As for proofs with an external interactive prover, the user should set the attribute `Proof_Dir` so that proofs can be saved under version control.
• The Proof_Dir is recommended to be under a version control system (git or svn for example). The proofs can be tedious to rewrite so it is better not to lose them.

• There is currently no way to adapt proofs made on a given version of the code when the code is changed. The update will have to be done manually but we hope to automate the process in the future.

• This feature is experimental and we currently recommend to keep the proof as short as possible.

• If the goal contains epsilons, they can be removed by using eliminate_epsilon.

• Manual provers can be launched during the edition of the proof like other provers. The user can select a goal node and type coq for example.

• The command line remembers what is typed. Arrow keys can be used to get the last queried commands.

7.1.9 How to Speed Up a Run of GNATprove

GNATprove can take some time on large programs with difficult checks to prove. This section describes how one can improve the running time of the GNATprove tool. Note that some of the suggested settings will decrease the number of proved checks or decrease usability of the tool, because spending more time often results in more successful proofs. You may still want to try some of the suggestions here to see if the time spent by GNATprove is really useful in your context.

These settings will speed up GNATprove:

• Use the -j switch to use more than one core on your machine. GNATprove can make efficient usage of multi-processing. If your machine has more than one processor or core, we strongly suggest to enable multi-processing, using the -j switch. This switch should not have an impact on proof results, only on running time.

• Use --no-loop-unrolling to deactivate loop unrolling. Loop unrolling can often avoid the use of a loop invariant, but it almost always will be more costly to analyze than a loop with a loop invariant. See also Automatic Unrolling of Simple For-Loops.

• Use --no-inlining to deactivate contextual analysis of local subprograms without contracts. This feature can often avoid the use of subprogram contracts, but it will be more costly to analyze such subprograms in their calling context than analyzing them separately. See also Contextual Analysis of Subprograms Without Contracts.

• Use --no-counterexample to deactivate counterexamples. Counter-examples are very useful to understand the reason for a failed proof attempt. You can disable this feature if you are not working on a failed proof attempt.

• Use the --level switch to use a lower level and faster presets. Generally, a lower level is faster than higher levels. See also Running GNATprove from the Command Line.

• More fine-grained than the --level switch, you can directly set the --prover, --timeout and --steps options. Using only one prover with a small timeout or a small steps limit will result in much faster execution.

7.1.10 GNATprove and Network File Systems or Shared Folders

On Linux and Mac-OS, GNATprove needs to create a Unix domain socket file. This might be a problem if GNATprove attempts to create such a file in a directory that is a shared folder or on a network file system like NFS, which does not support such folders. To minimize changes for this to occur, GNATprove determines the folder to create that special file as follows:

• if the environment variable TMPDIR is set, and the corresponding directory exists and is writable, use that; otherwise,

• if /tmp exists and is writable, use that; otherwise,
• use the `gnatprove` subfolder of the object directory of the root project.

7.2 How to View GNATprove Output

GNATprove produces two kinds of outputs: the one which is echoed to standard output or displayed in your IDE (GNAT Studio or GNATbench), and a textual summary of the analysis results.

7.2.1 The Analysis Report Panel

GNAT Studio can display an interactive view reporting the results of the analysis, with a count of issues per file, subprogram and severity, as well as filters to selectively view a subset of the issues only. This interactive view is displayed using the menu `SPARK → Show Report`. This menu becomes available after the checkbox `Display analysis report` is checked in the SPARK section of the Preferences dialog - menu `Edit → Preferences`, and only if GNATprove was run so that there are results to display.

[Image of the Analysis Report Panel]

Here is an example of this view:

7.2.2 The Analysis Results Summary File

GNATprove generates global project statistics in file `gnatprove.out`, which can be displayed in GNAT Studio using the menu `SPARK → Show Log`. The file `gnatprove.out` is generated in the `gnatprove` subdirectory of the object directory of the project.

When switch `--output-header` is used, this file starts with a header containing extra information about the run including:

• The date and time of GNATprove run
• The GNATprove version that has generated this report
• The host for which GNATprove is configured (e.g. Windows 32 bits)
• The full command-line of the GNATprove invocation, including project file
• The GNATprove switches specified in the project file

A summary table at the start of file `gnatprove.out` provides an overview of the verification results for all checks in the project. The table may look like this:

<table>
<thead>
<tr>
<th>SPARK Analysis results</th>
<th>Total</th>
<th>Flow</th>
<th>Interval</th>
<th>CodePeer</th>
</tr>
</thead>
<tbody>
<tr>
<td>Provers</td>
<td>Justified</td>
<td>Unproved</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Data Dependencies</td>
<td>281</td>
<td>281</td>
<td>.</td>
<td>.</td>
</tr>
<tr>
<td>Flow Dependencies</td>
<td>228</td>
<td>228</td>
<td>.</td>
<td>.</td>
</tr>
<tr>
<td>Initialization</td>
<td>693</td>
<td>692</td>
<td>.</td>
<td>1</td>
</tr>
<tr>
<td>Non-Aliasing</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>.</td>
</tr>
<tr>
<td>Run-time Checks</td>
<td>474</td>
<td>.</td>
<td>.</td>
<td>.</td>
</tr>
<tr>
<td>Assertions</td>
<td>45</td>
<td>.</td>
<td>.</td>
<td>45 (CVC4 95%, Trivial 5%)</td>
</tr>
<tr>
<td>Functional Contracts</td>
<td>304</td>
<td>.</td>
<td>.</td>
<td>302 (CVC4 82%, Trivial 18%)</td>
</tr>
<tr>
<td>LSP Verification</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>.</td>
</tr>
<tr>
<td>Termination</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>.</td>
</tr>
<tr>
<td>Concurrency</td>
<td>.</td>
<td>.</td>
<td>.</td>
<td>.</td>
</tr>
<tr>
<td>Total</td>
<td>2025</td>
<td>1201 (59%)</td>
<td>.</td>
<td>19 (1%)</td>
</tr>
</tbody>
</table>

The following table explains the lines of the summary table:

<table>
<thead>
<tr>
<th>Line Description</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Data Dependencies</td>
<td>Verification of Data Dependencies and parameter modes</td>
</tr>
<tr>
<td>Flow Dependencies</td>
<td>Verification of Flow Dependencies</td>
</tr>
<tr>
<td>Initialization</td>
<td>Verification of Data Initialization Policy</td>
</tr>
<tr>
<td>Non-Aliasing</td>
<td>Verification of Absence of Interferences</td>
</tr>
<tr>
<td>Run-time Checks</td>
<td>Verification of absence of run-time errors (AoRTE) (except those raising Storage_Error)</td>
</tr>
<tr>
<td>Assertions</td>
<td>Verification of Assertion Pragmas</td>
</tr>
<tr>
<td>Functional Contracts</td>
<td>Verification of functional contracts (includes Subprogram Contracts, Package Contracts and Type Contracts)</td>
</tr>
<tr>
<td>LSP Verification</td>
<td>Verification related to Object Oriented Programming and Liskov Substitution Principle</td>
</tr>
<tr>
<td>Termination</td>
<td>Verification related to Loop Variants and Subprogram Termination</td>
</tr>
<tr>
<td>Concurrency</td>
<td>Verification related to Concurrency and Ravenscar Profile</td>
</tr>
</tbody>
</table>

We now explain the columns of the table.
• The **Total** column describes the total number of checks in this category.

• The **Flow** column describes the number of checks proved by flow analysis.

• The **Interval** column describes the number of checks (overflow and range checks) proved by a simple static analysis of bounds for floating-point expressions based on type bounds of sub-expressions.

• The **CodePeer** column describes the number of checks proved by calling CodePeer when *Using CodePeer Static Analysis*. 

• The **Provers** column describes the number of checks proved by automatic or manual provers. The column also gives information on the provers used, and the percentage of checks proved by each prover. Note that sometimes a check is proved by a combination of provers, hence the use of percentage instead of an absolute count. Also note that generally the prover which is run first (as determined by the `--prover` command line switch) proves the most checks, because each prover is called only on those checks that were not previously proved. The prover percentages are provided in alphabetical order. The special name **Trivial** is used to refer to an internal simplication that discards checks that are trivially true.

• The **Justified** column contains the number of checks for which the user has provided a *Direct Justification with Pragma Annotate*.

• Finally, the column **Unproved** counts the checks which have neither been proved nor justified.

After the summary table, a line states the maximal steps that were consumed by automated provers. The line may look like this:

```
max steps used for successful proof: 1234
```

The use of this line is to help with reproducability of a run of GNATprove that proved all checks and properties. If the user provides the given number via the `--steps` option to GNATprove, and disables the time and memory limits, (if enabled directly or indirectly such as via the `--level` switch), then GNATprove will again prove all checks and properties. For example, if a user has proved all checks in a project using an invocation of GNATprove as follows:

```
gnatprove -P <projectfile> --level=2
```

then the following command will also prove all checks:

```
gnatprove -P <projectfile> --level=2 --timeout=0 --memlimit=0 --steps=1234
```

The next contents in the file are statistics describing:

• which units were analyzed (with flow analysis, proof, or both)

• which subprograms in these units were analyzed (with flow analysis, proof, or both)

• the results of this analysis

### 7.2.3 Categories of Messages

GNATprove issues four different kinds of messages: errors, warnings, check messages and information messages.

• **Errors** are issued for SPARK violations or other language legality problems, or any other problem which does not allow to proceed to analysis. Errors cannot be suppressed and must be fixed to proceed with analysis.

• **Warnings** are issued for any suspicious situation like unused values of variables, useless assignments, etc. Warnings are prefixed with the text "warning: " and can be suppressed with *pragma Warnings*, see section * Suppressing Warnings*. 

• **Check messages** are issued for any potential problem in the code which could affect the correctness of the program, such as missing initialization, possible failing run-time checks or unproved assertions. Checks come
with a severity, and depending on the severity the message text is prefixed with "low: ", "medium: " or "high: ". Check messages cannot be suppressed like warnings, but they can be individually justified with pragma Annotate, see section Justifying Check Messages.

- Information messages are issued to notify the user of limitations of GNATprove on some constructs, or to prevent possible confusion in understanding the output of GNATprove. They are also issued to report proved checks in some modes of GNATprove.

### 7.2.4 Effect of Mode on Output

GNATprove can be run in four different modes, as selected with the switch --mode=<mode>, whose possible values are check, check_all, flow, prove and all (see Running GNATprove from the Command Line). The output depends on the selected mode.

In modes check and check_all, GNATprove prints on the standard output a list of error messages for violations of SPARK restrictions on all the code for which SPARK_Mode is On.

In modes flow and prove, this checking is done as a first phase.

In mode flow, GNATprove prints on the standard output messages for possible reads of uninitialized data, mismatches between the specified data dependencies and flow dependencies and the implementation, and suspicious situations such as unused assignments and missing return statements. These messages are all based on flow analysis.

In mode prove, GNATprove prints on the standard output messages for possible reads of uninitialized data (using flow analysis), possible run-time errors and mismatches between the specified functional contracts and the implementation (using proof).

In mode all, GNATprove prints on the standard output both messages for mode flow and for mode prove.

If switch --report=all, --report=provers or --report=statistics is specified, GNATprove additionally prints on the standard output information messages for proved checks.

### 7.2.5 Description of Messages

This section lists the different messages which GNATprove may output. Each message points to a very specific place in the source code. For example, if a source file file.adb contains a division as follows:

```ada
if X / Y > Z then ...
```

GNATprove may output a message such as:

```
file.adb:12:37: medium: divide by zero might fail
```

where the division sign / is precisely on line 12, column 37. Looking at the explanation in the first table below, which states that a division check verifies that the divisor is different from zero, it is clear that the message is about $Y$, and that GNATprove was unable to prove that $Y$ cannot be zero. The explanations in the table below should be read with the context that is given by the source location.

When switch --cwe is used, a corresponding CWE id is included in the message when relevant. For example, on the example above, GNATprove will output a message such as:

```
file.adb:12:37: medium: divide by zero might fail [CWE 369]
```

Note that CWE ids are only included in check messages and warnings, never in information messages about proved checks. For more information on CWE, see the MITRE Corporation’s Common Weakness Enumeration (CWE) Compatibility and Effectiveness Program (http://cwe.mitre.org/). The current version of GNATprove is based on CWE version 3.2 released on January 3, 2019.
## Messages reported by Proof

<table>
<thead>
<tr>
<th>Message Kind</th>
<th>CWE</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>run-time checks</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>divide by zero</td>
<td>CWE 369</td>
<td>Check that the second operand of the division, mod or rem operation is different from zero.</td>
</tr>
<tr>
<td>index check</td>
<td>CWE 120</td>
<td>Check that the given index is within the bounds of the array.</td>
</tr>
<tr>
<td>overflow check</td>
<td>CWE 190</td>
<td>Check that the result of the given integer arithmetic operation is within the bounds of the base type.</td>
</tr>
<tr>
<td>fp_overflow check</td>
<td>CWE 739</td>
<td>Check that the result of the given floating point operation is within the bounds of the base type.</td>
</tr>
<tr>
<td>range check</td>
<td>CWE 682</td>
<td>Check that the given value is within the bounds of the expected scalar subtype.</td>
</tr>
<tr>
<td>predicate check</td>
<td>CWE 682</td>
<td>Check that the given value respects the applicable type predicate.</td>
</tr>
<tr>
<td>predicate check on default value</td>
<td>CWE 682</td>
<td>Check that the default value for the type respects the applicable type predicate.</td>
</tr>
<tr>
<td>null pointer dereference</td>
<td>CWE 476</td>
<td>Check that the given pointer is not null so that it can be dereferenced.</td>
</tr>
<tr>
<td>null exclusion</td>
<td></td>
<td>Check that the subtype_indication of the allocator does not specify a null_exclusion</td>
</tr>
<tr>
<td>length check</td>
<td></td>
<td>Check that the given array is of the length of the expected array subtype.</td>
</tr>
<tr>
<td>discriminant check</td>
<td>CWE 136</td>
<td>Check that the discriminant of the given discriminated record has the expected value. For variant records, this can happen for a simple access to a record field. But there are other cases where a fixed value of the discriminant is required.</td>
</tr>
<tr>
<td>tag check</td>
<td>CWE 136</td>
<td>Check that the tag of the given tagged object has the expected value.</td>
</tr>
<tr>
<td>ceiling priority in Interrupt_Priority</td>
<td></td>
<td>Check that the ceiling priority specified for a protected object containing a procedure with an aspect Attach_Handler is in Interrupt_Priority.</td>
</tr>
<tr>
<td>use of an uninitialized variable</td>
<td>CWE 457</td>
<td>Check that a variable is initialized</td>
</tr>
<tr>
<td>interrupt is reserved</td>
<td></td>
<td>Check that the interrupt specified by Attach_Handler is not reserved.</td>
</tr>
<tr>
<td>invariant check</td>
<td></td>
<td>Check that the given value respects the applicable type invariant.</td>
</tr>
<tr>
<td>invariant check on default value</td>
<td></td>
<td>Check that the default value for the type respects the applicable type invariant.</td>
</tr>
<tr>
<td>ceiling priority protocol</td>
<td></td>
<td>Check that the ceiling priority protocol is respected, i.e., when a task calls a protected operation, the active priority of the task is not higher than the priority of the protected object (Ada RM Annex D.3).</td>
</tr>
<tr>
<td>task termination</td>
<td></td>
<td>Check that the task does not terminate, as required by Ravenscar.</td>
</tr>
<tr>
<td><strong>assertions</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>initial condition</td>
<td></td>
<td>Check that the initial condition of a package is true after elaboration.</td>
</tr>
<tr>
<td>Message Kind</td>
<td>CWE</td>
<td>Explanation</td>
</tr>
<tr>
<td>------------------------------</td>
<td>-----------</td>
<td>-----------------------------------------------------------------------------</td>
</tr>
<tr>
<td>default initial condition</td>
<td></td>
<td>Check that the default initial condition of a type is true after default initialization of an object of the type.</td>
</tr>
<tr>
<td>precondition</td>
<td>CWE 628</td>
<td>Check that the precondition aspect of the given call evaluates to True.</td>
</tr>
<tr>
<td>precondition of main</td>
<td>CWE 628</td>
<td>Check that the precondition aspect of the given main procedure evaluates to True after elaboration.</td>
</tr>
<tr>
<td>postcondition</td>
<td>CWE 682</td>
<td>Check that the postcondition aspect of the subprogram evaluates to True.</td>
</tr>
<tr>
<td>refined postcondition</td>
<td>CWE 682</td>
<td>Check that the refined postcondition aspect of the subprogram evaluates to True.</td>
</tr>
<tr>
<td>contract case</td>
<td>CWE 682</td>
<td>Check that all cases of the contract case evaluate to True at the end of the subprogram.</td>
</tr>
<tr>
<td>disjoint contract cases</td>
<td></td>
<td>Check that the cases of the contract cases aspect are all mutually disjoint.</td>
</tr>
<tr>
<td>complete contract cases</td>
<td></td>
<td>Check that the cases of the contract cases aspect cover the state space that is allowed by the precondition aspect.</td>
</tr>
<tr>
<td>loop invariant</td>
<td></td>
<td>Check that the loop invariant evaluates to True on all iterations of the loop.</td>
</tr>
<tr>
<td>loop invariant in first iteration</td>
<td></td>
<td>Check that the loop invariant evaluates to True on the first iteration of the loop.</td>
</tr>
<tr>
<td>loop invariant after first iteration</td>
<td></td>
<td>Check that the loop invariant evaluates to True at each further iteration of the loop.</td>
</tr>
<tr>
<td>loop variant</td>
<td>CWE 835</td>
<td>Check that the given loop variant decreases/increases as specified during each iteration of the loop. This implies termination of the loop.</td>
</tr>
<tr>
<td>assertion</td>
<td></td>
<td>Check that the given assertion evaluates to True.</td>
</tr>
<tr>
<td>raised exception</td>
<td></td>
<td>Check that the raise statement can never be reached.</td>
</tr>
<tr>
<td>Inline_For_Proof annotation</td>
<td></td>
<td>Check that an Annotate pragma with the Inline_For_Proof identifier is correct.</td>
</tr>
</tbody>
</table>

**Liskov Substitution Principle**

<table>
<thead>
<tr>
<th>Message Kind</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>precondition weaker than class-wide precondition</td>
<td>Check that the precondition aspect of the subprogram is weaker than its class-wide precondition.</td>
</tr>
<tr>
<td>precondition not True while class-wide precondition is True</td>
<td>Check that the precondition aspect of the subprogram is True if its class-wide precondition is True.</td>
</tr>
<tr>
<td>postcondition stronger than class-wide postcondition</td>
<td>Check that the postcondition aspect of the subprogram is stronger than its class-wide postcondition.</td>
</tr>
<tr>
<td>class-wide precondition weaker than overridden one</td>
<td>Check that the class-wide precondition aspect of the subprogram is weaker than its overridden class-wide precondition.</td>
</tr>
<tr>
<td>class-wide postcondition stronger than overridden one</td>
<td>Check that the class-wide postcondition aspect of the subprogram is stronger than its overridden class-wide postcondition.</td>
</tr>
</tbody>
</table>

**Messages reported by Flow Analysis**

The following table shows all flow analysis messages, (E)rrors, (W)arnings and (C)hecks.
<table>
<thead>
<tr>
<th>Message Kind</th>
<th>Class</th>
<th>CWE</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>aliasing between subprogram parameters</td>
<td>C</td>
<td></td>
<td>Aliasing between formal parameters or global objects.</td>
</tr>
<tr>
<td>invalid call in type invariant</td>
<td>C</td>
<td>CWE 674</td>
<td>A type invariant calls a boundary subprogram for the type.</td>
</tr>
<tr>
<td>invalid context for call to Current_Task</td>
<td>C</td>
<td></td>
<td>Current_Task is called from an invalid context.</td>
</tr>
<tr>
<td>race condition</td>
<td>C</td>
<td>CWE 362</td>
<td>An unsynchronized global object is accessed concurrently.</td>
</tr>
<tr>
<td>dead code</td>
<td>W</td>
<td>CWE 561</td>
<td>A statement is never executed.</td>
</tr>
<tr>
<td>wrong Default_Initial.Condition aspect</td>
<td>C</td>
<td>CWE 457</td>
<td>A type is wrongly declared as initialized by default.</td>
</tr>
<tr>
<td>input item missing from the dependency clause</td>
<td>C</td>
<td></td>
<td>An input is missing from the dependency clause.</td>
</tr>
<tr>
<td>output item missing from the dependency clause</td>
<td>C</td>
<td></td>
<td>An output item is missing from the dependency clause.</td>
</tr>
<tr>
<td>input item missing from the null dependency clause</td>
<td>C</td>
<td></td>
<td>An input item is missing from the null dependency clause.</td>
</tr>
<tr>
<td>extra input item in the dependency clause</td>
<td>C</td>
<td></td>
<td>Extra input item in the dependency clause.</td>
</tr>
<tr>
<td>subprogram output depends on a Proof_In global</td>
<td>C</td>
<td></td>
<td>Subprogram output depends on a Proof_In global.</td>
</tr>
<tr>
<td>non-ghost output of ghost procedure</td>
<td>C</td>
<td></td>
<td>A ghost procedure has a non-ghost global output.</td>
</tr>
<tr>
<td>incomplete Global or Initializes contract</td>
<td>E</td>
<td></td>
<td>A Global or Initializes contract fails to mention some objects.</td>
</tr>
<tr>
<td>an extra item in the Global or Initializes contract</td>
<td>C</td>
<td></td>
<td>A Global or Initializes contract wrongly mentions some objects.</td>
</tr>
<tr>
<td>constants with variable inputs that is not a state constituent</td>
<td>C</td>
<td></td>
<td>Constants with variable inputs that are not state constituents.</td>
</tr>
<tr>
<td>illegal write of a global input</td>
<td>C</td>
<td></td>
<td>Illegal write of a global input.</td>
</tr>
<tr>
<td>a state abstraction that is impossible to initialize</td>
<td>C</td>
<td></td>
<td>A state abstraction that is impossible to initialize.</td>
</tr>
<tr>
<td>a statement with no effect on subprogram’s outputs</td>
<td>W</td>
<td>CWE 1164</td>
<td>A statement with no effect on subprogram’s outputs.</td>
</tr>
<tr>
<td>an extra item in the Initializes contract</td>
<td>C</td>
<td></td>
<td>An object that shall not appear in the Initializes contract.</td>
</tr>
<tr>
<td>an IN OUT parameter or an In_Out global that is not written</td>
<td>C</td>
<td></td>
<td>An IN OUT parameter or an In_Out global that is not written.</td>
</tr>
<tr>
<td>all execution paths raise exceptions or do not return</td>
<td>C</td>
<td></td>
<td>All execution paths raise exceptions or do not return.</td>
</tr>
<tr>
<td>volatile function wrongly declared as non-volatile</td>
<td>C</td>
<td></td>
<td>A volatile function wrongly declared as non-volatile.</td>
</tr>
<tr>
<td>illegal write of an object declared as constant after elaboration</td>
<td>C</td>
<td></td>
<td>Illegal write of an object declared as constant after elaboration.</td>
</tr>
<tr>
<td>use of an abstract state of a package that was not yet elaborated</td>
<td>C</td>
<td></td>
<td>Use of an abstract state of a package that was not yet elaborated.</td>
</tr>
<tr>
<td>a missing pragma Elaborate_Body</td>
<td>C</td>
<td></td>
<td>A missing pragma Elaborate_Body.</td>
</tr>
<tr>
<td>protected operation blocks</td>
<td>C</td>
<td>CWE 667</td>
<td>A protected operation may block.</td>
</tr>
<tr>
<td>illegal reference to a global object in precondition of a protected operation</td>
<td>C</td>
<td></td>
<td>An illegal reference to global in precondition of a protected operation.</td>
</tr>
<tr>
<td>constant with no variable inputs as an abstract state’s constituent</td>
<td>C</td>
<td></td>
<td>Constant with no variable inputs as an abstract state’s constituent.</td>
</tr>
<tr>
<td>function with side effects</td>
<td>E</td>
<td></td>
<td>A function with side effects.</td>
</tr>
<tr>
<td>loop with stable statement</td>
<td>W</td>
<td></td>
<td>A loop with stable statement.</td>
</tr>
<tr>
<td>subprogram marked Terminating may not terminate</td>
<td>C</td>
<td>CWE 674</td>
<td>A subprogram with Terminating annotation may not terminate.</td>
</tr>
<tr>
<td>use of an uninitialized variable</td>
<td>C</td>
<td>CWE 457</td>
<td>Flow analysis has detected the use of an uninitialized variable.</td>
</tr>
<tr>
<td>object is not used</td>
<td>W</td>
<td>CWE 563</td>
<td>A global or locally declared object is never used.</td>
</tr>
<tr>
<td>initial value of an object is not used</td>
<td>W</td>
<td>CWE 563</td>
<td>The initial value of an object is not used.</td>
</tr>
<tr>
<td>non-volatile function wrongly declared as volatile</td>
<td>C</td>
<td></td>
<td>A non-volatile function wrongly declared as volatile.</td>
</tr>
</tbody>
</table>
Note: Certain messages emitted by flow analysis are classified as errors and consequently cannot be suppressed or justified.

Messages of a specific category or related to a specific CWE can be filtered inside GNAT Studio by typing the desired substring in the search bar of the Locations panel. For example, search for “CWE” to get all messages with a corresponding CWE, or “CWE 369” to get all messages related to division by zero vulnerability.

### 7.2.6 Understanding Counterexamples

When a check cannot be proved, GNATprove may generate a counterexample. A counterexample consists in two parts:

- a path (or set of paths) through the subprogram
- an assignment of values to variables that appear on that path

The best way to look at a counterexample is to display it in GNAT Studio by clicking on the icon to the left of the failed proof message, or to the left of the corresponding line in the editor (see Running GNATprove from GNAT Studio). GNATprove then displays the path in one color, and the values of variables on the path by inserting lines in the editor only (not in the file) which display these values. For example, consider procedure `Counterex`:

```plaintext
procedure Counterex (Cond : Boolean; In1, In2 : Integer; R : out Integer) with
  SPARK_Mode,
  Pre => In1 <= 25 and In2 <= 25
is
begin
  R := 0;
  if Cond then
    R := R + In1;
    if In1 < In2 then
      R := R + In2;
      pragma Assert (R < 42);
    end if;
  end if;
end Counterex;
```

The assertion on line 11 may fail when input parameter `Cond` is `True` and input parameters `I1` and `I2` are too big. The counterexample generated by GNATprove is displayed as follows in GNAT Studio, where each line highlighted in the path is followed by a line showing the value of variables from the previous line:
GNATprove also completes the message for the failed proof with an explanation giving the values of variables from the checked expression for the counterexample. Here, the message issued by GNATprove on line 11 gives the value of output parameter \( R \):

```
counterex.adb:11:25: medium: assertion might fail, cannot prove \( R < 42 \) (e.g. when \( R = 42 \))
```

The counterexample generated by GNATprove does not always correspond to a feasible execution of the program:

1. When some contracts or loop invariants are missing, thus causing the property to become unprovable (see details in section on Investigating Unprovable Properties), the counterexample may help point to the missing contract or loop invariant. For example, the postcondition of procedure `Double_In_Call` is not provable because the postcondition of the function `Double` that it calls is too weak, and the postcondition of procedure `Double_In_Loop` is not provable because its loop does not have a loop invariant:

```ada
package Counterex_Unprovable with
SPARK_Mode
is
  type Int is new Integer range -100 .. 100;

function Double (X : Int) return Int with
  Pre  => abs X <= 10,
  Post => abs Double'Result <= 20;

procedure Double_In_Call (X : in out Int) with
  Pre  => abs X <= 10,
  Post => X = 2 * X'Old;

procedure Double_In_Loop (X : in out Int) with
  Pre  => abs X <= 10,
  Post => X = 2 * X'Old;
```
```ada
package body Counterex_Unprovable with
  SPARK_Mode is

  function Double (X : Int) return Int is begin
    return 2 * X;
  end Double;

  procedure Double_In_Call (X : in out Int) is begin
    X := Double (X);
  end Double_In_Call;

  procedure Double_In_Loop (X : in out Int) is
    Result : Int := 0;
    begin
      for J in 1 .. 2 loop
        Result := Result + X;
      end loop;
      X := Result;
    end Double_In_Loop;
end Counterex_Unprovable;
```

The counterexample generated by GNATprove in both cases shows that the prover could deduce wrongly that \( X \) on output is -3 when its value is 1 on input, due to a missing contract in the function called or a missing loop invariant the loop executed:

```ada
package body Counterex_Unprovable with
  SPARK_Mode is

  function Double (X : Int) return Int is begin
    return 2 * X;
  end Double;

  procedure Double_In_Call (X : in out Int) is begin
    X := Double (X);
  end Double_In_Call;

  procedure Double_In_Loop (X : in out Int) is
    Result : Int := 0;
    begin
      for J in 1 .. 2 loop
        Result := Result + X;
      end loop;
      X := Result;
    end Double_In_Loop;
end Counterex_Unprovable;
```

2. When some property cannot be proved due to prover shortcomings (see details in section on *Investigating Prover Shortcomings*), the counterexample may explain why the prover cannot prove the property. However, note that since the counterexample is always generated only using CVC4 prover, it can just explain why this prover cannot prove the property. Also note that if CVC4 is not selected and generating of a counterexample is not disabled by --no-counterexample switch, a counterexample is still attempted to be generated using CVC4, but the proof result of CVC4 is not taken into account in this case.

3. When using a short value of timeout or steps, the prover may hit the resource bound before it has produced a full counterexample. In such a case, the counterexample produced may not correspond to a feasible execution.

4. When the value of --proof switch is per_check (the default value), then the counterexample gives values

```ada
counterex_unprovable.adb:7:16: info: overflow check proved
counterex_unprovable.adb:7:16: info: range check proved
counterex_unprovable.adb:12:12: info: precondition proved
counterex_unprovable.adb:19:27: info: range check proved
counterex_unprovable.ads:8:14: info: overflow check proved
counterex_unprovable.ads:9:14: info: overflow check proved
counterex_unprovable.ads:9:14: info: postcondition proved
counterex_unprovable.ads:12:14: info: overflow check proved
counterex_unprovable.ads:13:14: medium: postcondition might fail, cannot prove X<sub>≤</sub> <= 2 * X'old (e.g. when X = -1 and X'Old = 0)
counterex_unprovable.ads:13:20: info: overflow check proved
counterex_unprovable.ads:16:14: info: overflow check proved
counterex_unprovable.ads:17:14: info: postcondition proved
counterex_unprovable.ads:17:20: info: overflow check proved
```
to variables on all paths through the subprogram, not only the path which corresponds to the feasible execution. One can rerun GNATprove with value progressive or per_path to separate possible execution paths in the counterexample.

7.3 How to Use GNATprove in a Team

The most common use of GNATprove is as part of a regular quality control or quality assurance activity inside a team. Usually, GNATprove is run every night on the current codebase, and during the day by developers either on their computer or on servers. For both nightly and daily runs, GNATprove results need to be shared between team members, either for viewing results or to compare new results with the shared results. These various processes are supported by specific ways to run GNATprove and share its results.

In all cases, the source code should not be shared directly (say, on a shared drive) between developers, as this is bound to cause problems with file access rights and concurrent accesses. Rather, the typical usage is for each user to do a check out of the sources/environment, and use therefore her own version/copy of sources and project files, instead of physically sharing sources across all users.

The project file should also always specify a local, non shared, user writable directory as object directory (whether explicitly or implicitly, as the absence of an explicit object directory means the project file directory is used as object directory).

7.3.1 Possible Workflows

Multiple workflows allow to use GNATprove in a team:

1. GNATprove is run on a server or locally, and no warnings or check messages should be issued. Typically this is achieved by suppressing spurious warnings and justifying unproved check messages.

2. GNATprove is run on a server or locally, and textual results are shared in Configuration Management.

3. GNATprove is run on a server, and textual results are sent to a third-party qualimetry tool (like GNATdashboard, SonarQube, SQUARE, etc.)

4. GNATprove is run on a server or locally, and the GNATprove session files are shared in Configuration Management.

In all workflows (but critically for the first workflow), messages can be suppressed or justified. Indeed, like every sound and complete verification tool, GNATprove may issue false alarms. A first step is to identify the type of message:

- warnings can be suppressed, see Suppressing Warnings
- check messages can be justified, see Justifying Check Messages

Check messages from proof may also correspond to provable checks, which require interacting with GNATprove to find the correct contracts and/or analysis switches, see How to Investigate Unproved Checks.

The textual output in workflow 3 corresponds to the compiler-like output generated by GNATprove and controlled with switches --report and --warnings (see Running GNATprove from the Command Line). By default messages are issued only for unproved checks and warnings.

The textual output in workflow 2 comprises this compiler-like output, and possibly additional output generated by GNATprove in file gnatprove.out (see Effect of Mode on Output and Managing Assumptions).

Workflow 4 is explained in more detail in Sharing Proof Results with Others.
7.3.2 Suppressing Warnings

GNATprove issues two kinds of warnings, which are controlled separately:

- Compiler warnings are controlled with the usual GNAT compilation switches:
  - -gnatws suppresses all warnings
  - -gnatwa enables all optional warnings
  - -gnatw? enables a specific warning denoted by the last character
  
  See the GNAT User’s Guide for more details. These should passed through the compilation switches specified in the project file.

- GNATprove specific warnings are controlled with switch --warnings:
  - --warnings=off suppresses all warnings
  - --warnings=error treats warnings as errors
  - --warnings=continue issues warnings but does not stop analysis (default)

  The default is that GNATprove issues warnings but does not stop.

Both types of warnings can be suppressed selectively by the use of pragma Warnings in the source code. For example, GNATprove issues three warnings on procedure Warn, which are suppressed by the three pragma Warnings in the source code:

```plaintext
pragma Warnings (Off, "unused initial value of "X",";
Reason => "Parameter mode is mandated by API");

procedure Warn (X : in out Integer) with
SPARK_Mode
is
pragma Warnings (Off, "initialization has no effect",
Reason => "Coding standard requires initialization");
Y : Integer := 0;
pragma Warnings (On, "initialization has no effect");

begin
pragma Warnings (Off, "unused assignment",
Reason => "Test program requires double assignment");
X := Y;
pragma Warnings (On, "unused assignment");
X := Y;
end Warn;
```

Warnings with the specified message are suppressed in the region starting at pragma Warnings Off and ending at the matching pragma Warnings On or at the end of the file (pragma Warnings is purely textual, so its effect does not stop at the end of the enclosing scope). The Reason argument string is optional. A regular expression can be given instead of a specific message in order to suppress all warnings of a given form. Pragma Warnings Off can be added in a configuration file to suppress the corresponding warnings across all units in the project. Pragma Warnings Off can be specified for an entity to suppress all warnings related to this entity.

Pragma Warnings can also take a first argument of GNAT or GNATprove to specify that it applies only to GNAT compiler or GNATprove. For example, the previous example can be modified to use these refined pragma Warnings:

```plaintext
pragma Warnings (GNATprove, Off, "unused initial value of "X",";
Reason => "Parameter mode is mandated by API");

procedure Warn2 (X : in out Integer) with
```
Besides the documentation benefit of using this refined version of pragma Warnings, it makes it possible to detect useless pragma Warnings, that do not suppress any warning, with switch \texttt{-gnatw.w}. Indeed, this switch can then be used both during compilation with GNAT and formal verification with GNATprove, as pragma Warnings that apply to only one tool can be identified as such.

See the GNAT Reference Manual for more details.

Additionally, GNATprove can issue warnings as part of proof, on preconditions or postconditions or pragma Assume that are always false, unreachable branches in complex Boolean expressions (typically in assertions and contracts), dead code at branching points in the program. These warnings are not enabled by default, as they require calling a prover for each potential warning, which incurs a small cost (1 sec for each property thus checked). They can be enabled with switch \texttt{--proof-warnings}, and their effect is controlled by switch \texttt{--warnings} and pragma Warnings as described previously.

There are two benefits of activating these warnings:

- they may detect unintentional unreachable or useless code and assertions, which may originate from errors in either code or assertions;
- they strengthen confidence in the tool output, acting as a smoke detector for cases where the tool would get into an inconsistent context by error, and report some unreachable code or branch where there is none.

Note that GNATprove, just like GNAT, suppresses warnings about unused variables if their name contains any of the substrings DISCARD, DUMMY, IGNORE, JUNK, UNUSED, in any casing.

### 7.3.3 Suppressing Information Messages

Information messages can be suppressed by the use of pragma Warnings in the source code, like for warnings.

### 7.3.4 Justifying Check Messages

GNATprove’s analysis relies on the fact that, at any given point in the program, previous checks on any execution reaching that program point have been successful. Thus, given two successive assertions of the same property:

\begin{verbatim}
pragma Assert (Prop); -- possibly not proved
pragma Assert (Prop); -- proved
\end{verbatim}

The second assertion will be reported as proved by GNATprove, even if the first assertion is reported as not proved. This is because any execution that fails the first assertion is not analyzed further by GNATprove.

Similarly, consider two successive calls to the same procedure with a precondition:
The precondition of the second call will be reported as proved by GNATprove, even if the precondition of the first call is reported as not proved. This is because any execution that fails the first precondition is not analyzed further by GNATprove.

This applies to all proof checks, and to a lesser extent to flow analysis checks. For example, outputs of a subprogram are considered fully initialized in a caller, as explained in Data Initialization Policy. In particular, such outputs are considered to have values that respect the constraints of their type, which is used during proof.

Thus, the user should be careful when justifying check messages, as the incorrect justification of a check message that could fail could also hide other possible failures later for the same execution of the analyzed program.

**Direct Justification with Pragma Annotate**

Check messages generated by GNATprove’s flow analysis or proof can be selectively justified by adding a pragma Annotate in the source code. For example, the check message about a possible division by zero in the return expression below can be justified as follows:

```plaintext
return (X + Y) / (X - Y);
pragma Annotate (GNATprove, False_Positive,
    "divide by zero", "reviewed by John Smith");
```

The pragma has the following form:

```plaintext
pragma Annotate (GNATprove, Category, Pattern, Reason);
```

where the following table explains the different entries:

<table>
<thead>
<tr>
<th>Item</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>GNATprove</td>
<td>is a fixed identifier</td>
</tr>
<tr>
<td>Category</td>
<td>is one of False_Positive or Intentional</td>
</tr>
<tr>
<td>Pattern</td>
<td>is a string literal describing the pattern of the check messages which shall be justified</td>
</tr>
<tr>
<td>Reason</td>
<td>is a string literal providing a justification for reviews</td>
</tr>
</tbody>
</table>

All arguments should be provided.

The Category currently has no impact on the behavior of the tool but serves a documentation purpose:

- **False_Positive** indicates that the check cannot fail, although GNATprove was unable to prove it.
- **Intentional** indicates that the check can fail but that it is not considered to be a bug.

**Pattern** should be a substring of the check message to justify.

**Reason** is a string provided by the user as a justification for reviews. This reason may be present in a GNATprove report.

Placement rules are as follows: in a statement list or declaration list, pragma Annotate applies to the preceding item in the list, ignoring other pragma Annotate. If there is no preceding item, the pragma applies to the enclosing construct. For example, if the pragma is the first element of the then-branch of an if-statement, it will apply to condition in the if-statement.

If the preceding or enclosing construct is a subprogram body, the pragma applies to both the subprogram body and the spec including its contract. This allows to place a justification for a check message issued by GNATprove either on the spec when it is relevant for callers. Note that this placement of a justification is ineffective on subprograms analyzed only in the context of their calls (see details in Contextual Analysis of Subprograms Without Contracts).
An aspect on a package or subprogram declaration/body can be used instead of a pragma at the beginning of the corresponding declaration list inside the declaration/body:

```haskell
package Pack with
  Annotate => (GNATprove, False_Positive,
    "divide by zero", "reviewed by John Smith")
is
...

procedure Proc with
  Annotate => (GNATprove, False_Positive,
    "divide by zero", "reviewed by John Smith")
is
...
```

As a point of caution, the following placements of pragma Annotate will apply the pragma to a possibly large range of source lines:

- when the pragma appears in a statement list after a block, it will apply to the entire block (e.g. an if statement including all branches, or a loop including the loop body).
- when the pragma appears directly after a subprogram body, it will apply to the entire body and the spec of the subprogram.

Users should take care to not justify checks which were not intended to be justified, when placing pragma Annotate in such places.

```haskell
procedure Do_Something_1 (X, Y : in out Integer) with
  Depends => ((X, Y) => (X, Y));
pragma Annotate (GNATprove, Intentional, "incorrect dependency ""Y => X"",
  "Dependency is kept for compatibility reasons");
```

or on the body when it is an implementation choice that need not be visible to users of the unit:

```haskell
procedure Do_Something_2 (X, Y : in out Integer) with
  Depends => ((X, Y) => (X, Y));

procedure Do_Something_2 (X, Y : in out Integer) is
begin
  X := X + Y;
  Y := Y + 1;
end Do_Something_2;
pragma Annotate (GNATprove, Intentional, "incorrect dependency ""Y => X"",
  "Currently Y does not depend on X, but may change later");
```

Pragmas Annotate of the form above that do not justify any check message are useless and result in a warning by GNATprove. Like other warnings emitted by GNATprove, this warning is treated like an error if the switch --warnings=error is set.

**Indirect Justification with Pragma Assume**

Check messages generated by GNATprove's proof can alternatively be justified indirectly by adding a Pragma Assume in the source code, which allows the check to be proved. For example, the check message about a possible integer overflow in the assignment statement below can be justified as follows:

```haskell
procedure Next_Tick is
begin
```
Using `pragma Assume` is more powerful than using `pragma Annotate`, as the property assumed may be used to prove more than one check. Thus, one should in general use `pragma Annotate` rather than `pragma Assume` to justify simple runtime checks. There are some cases though where using a `pragma Assume` may be preferred. In particular:

- To keep assumptions local:

  ```ada
  pragma Assume (<External_Call's precondition>,
  "because for these internal reasons I know it holds");
  External_Call;
  ```

  If the precondition of `External_Call` changes, it may not be valid anymore to assume it here, though the assumption will stay True for the same reasons it used to be. Incompatible changes in the precondition of `External_Call` will lead to a failure in the proof of `External_Call`'s precondition.

- To sum up what is expected from the outside world so that it can be reviewed easily:

  ```ada
  External_Find (A, E, X);
  pragma Assume (X = 0 or (X in A'Range and A (X) = E),
  "because of the documentation of External_Find");
  ```

  Maintenance and review is easier with a single `pragma Assume` than if it is spread out into various pragmas `pragma Annotate`. If the information is required at several places, the `pragma Assume` can be factorized into a procedure:

  ```ada
  function External_Find_Assumption (A : Array, E : Element, X : Index) return Boolean
  is (X = 0 or (X in A'Range and A (X) = E))
  with Ghost;
  procedure Assume.getExternalFindAssumption (A : Array, E : Element, X : Index) with Ghost,
  Post => External_Find_Assumption (A, E, X)
  is
    pragma Assume (External_Find_Assumption (A, E, X),
    "because of the documentation of External_Find");
  end Assume.getExternalFindAssumption;
  ```

  In general, assumptions should be kept as small as possible (only assume what is needed for the code to work). Indirect justifications with `pragma Assume` should be carefully inspected as they can easily introduce errors in the verification process.

### 7.3.5 Sharing Proof Results with Others

GNATprove stores proof results in so-called session files. If session files are shared with others (e.g., via Configuration Management), either between members of the same team, or between the developer and users of a library, others can reproduce/recheck the proofs using the `--replay` option of GNATprove.
For a single project, proof results are typically stored in many session files, each of them having the filename `why3session.xml`. To avoid name clashes, the files are stored in subdirectories that correspond to subparts of the project (such as unit names and subprogram names). By default, these directories are stored in the `gnatprove` subdirectory of the object directory of the project. If the `Proof_Dir` attribute is set in the `Project Attributes`, the session directories will be stored in a `sessions` subdirectory of this directory. To generate session files, GNATprove should be run without the `--replay` option.

To share the session files, we recommend adding the `why3session.xml` files to version control. Note that the session directories may contain other files (the so-called shapes files `why3shapes` or `why3shapes.gz`). We advise against adding these other files to version control. To avoid version control conflicts, it can be advantageous to avoid updates to the session files by each developer, and instead update these files periodically using a centralized mechanism. For example, a nightly run on a server, or a dedicated team member, can be responsible for updating the proof directory with the latest version generated by GNATprove.

If a user has access to the session files (e.g. via the just-described version control) for a project, he can use the `--replay` option to reproduce/recheck the proofs that are stored in the session files. See Running GNATprove from the Command Line for more details on this command line option.

### 7.3.6 Sharing Proof Results Via a Memcached Server

GNATprove can cache and share results between distinct runs of the tool, even across several computers, via a Memcached server. To use this feature, you need to setup a memcached server (see [https://memcached.org/](https://memcached.org/)) on your network or on your local machine. Then, if you add the option `--memcached-server=hostname:portnumber` to your invocation of gnatprove (or use the `Switches` Attribute of the `Prove` Package of your project file), then caching will be used, and speedups should be observed in many cases.

### 7.3.7 Managing Assumptions

Because GNATprove analyzes separately subprograms and packages, its results depend on assumptions about other subprograms and packages. For example, the verification that a subprogram is free from run-time errors depends on the property that all the subprograms it calls implement their specified contract. If a program is completely analyzed with GNATprove, GNATprove will report messages on those other subprograms, if they might not implement their contract correctly. But in general, a program is partly in SPARK and partly in other languages, mostly Ada, C and assembly languages. Thus, assumptions on parts of the program that cannot be analyzed with GNATprove need to be recorded for verification by other means, like testing, manual analysis or reviews.

When switch `--assumptions` is used, GNATprove generates information about remaining assumptions in its result file `gnatprove.out`. These remaining assumptions need to be justified to ensure that the desired verification objectives are met. An assumption on a subprogram may be generated in various cases:

- the subprogram was not analyzed (for example because it is marked `SPARK_Mode => Off`)
- the subprogram was not completely verified by GNATprove (that is, some unproved checks remain)

Note that currently, only assumptions on called subprograms are output, and not assumptions on calling subprograms.

The following table explains the meaning of assumptions and claims which gnatprove may output:

<table>
<thead>
<tr>
<th>Assumption</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>effects on parameters and global variables</td>
<td>The subprogram does not read or write any other parameters or global variables than what is described in its spec (signature + data dependencies).</td>
</tr>
<tr>
<td>absence of run-time errors</td>
<td>The subprogram is free from run-time errors.</td>
</tr>
<tr>
<td>the postcondition</td>
<td>The postcondition of the subprogram holds after each call of the subprogram.</td>
</tr>
</tbody>
</table>
7.4 How to Write Subprogram Contracts

GNATprove relies on contracts to perform its analysis. User-specified subprogram contracts are assumed to analyze a subprogram’s callers, and verified when the body of the subprogram is analyzed.

By default, no contracts are compulsory in GNATprove. In the absence of user-provided contracts, GNATprove internally generates default contracts, which may or not be suitable depending on the verification objective:

- data dependencies (Global)
  See Generation of Dependency Contracts. The generated contract may be exact when completed from user-specified flow dependencies (Depends), or precise when generated from a body in SPARK, or coarse when generated from a body in full Ada.

- flow dependencies (Depends)
  See Generation of Dependency Contracts. The contract is generated from the user-specified or generated data dependencies, by considering that all outputs depend on all inputs.

- precondition (Pre)
  A default precondition of True is used in absence of a user-specified precondition.

- postcondition (Post)
  A default postcondition of True is used in absence of a user-specified postcondition, except for expression functions. For the latter, the body of the expression function is used to generate a matching postcondition. See Expression Functions.

Knowing which contracts to write depends on the specific verification objectives to achieve.

7.4.1 Generation of Dependency Contracts

By default, GNATprove does not require the user to write data dependencies (introduced with aspect Global) and flow dependencies (introduced with aspect Depends), as it can automatically generate them from the program.

This behavior can be disabled using the --no-global-generation switch, which means a missing data dependency is the same as Global => null. Note that this option also forces --no-inlining (see Contextual Analysis of Subprograms Without Contracts).

---

Note: GNATprove does not generate warning or check messages when the body of a subprogram does not respect a generated contract. Indeed, the generated contract is a safe over-approximation of the real contract, hence it is unlikely that the subprogram body respects it. The generated contract is used instead to verify proper initialization and respect of dependency contracts in the callers of the subprogram.

---

Note: Intrinsic subprograms such as arithmetic operations, and shift/rotate functions without user-provided functional contracts (precondition, postcondition or contract cases) are handled specially by GNATprove.

---

Note: The --no-global-generation switch makes GNATprove behave more like the previous SPARK 2005 tools, which makes this switch attractive for projects trying to migrate to the new GNATprove tools, or for projects that maintain dual annotations.
Auto Completion for Incomplete Contracts

When only the data dependencies (resp. only the flow dependencies) are given on a subprogram, GNATprove completes automatically the subprogram contract with the matching flow dependencies (resp. data dependencies).

Writing Only the Data Dependencies

When only the data dependencies are given on a subprogram, GNATprove completes them with flow dependencies that have all outputs depending on all inputs. This is a safe over-approximation of the real contract of the subprogram, which allows to detect all possible errors of initialization and contract violation in the subprogram and its callers, but which may also lead to false alarms because it is imprecise.

Take for example procedures Add and Swap for which data dependencies are given, but no flow dependencies:

```plaintext
package Only_Data_Dependencies with
  SPARK_Mode
is
  V : Integer;

  procedure Add (X : Integer) with
    Global => (In_Out => V);
  procedure Swap (X : in out Integer) with
    Global => (In_Out => V);
  procedure Call_Add (X, Y : Integer) with
    Global => (In_Out => V),
    Depends => (V =>+ (X, Y));
  procedure Call_Swap (X, Y : in out Integer) with
    Global => (In_Out => V),
    Depends => (X => Y, Y => X, V => V);
end Only_Data_Dependencies;
```

GNATprove completes the contract of Add and Swap with flow dependencies that are equivalent to:

```plaintext
procedure Add (X : Integer) with
  Global => (In_Out => V),
  Depends => (V =>+ X);
procedure Swap (X : in out Integer) with
  Global => (In_Out => V),
  Depends => ((X, V) => (X, V));
```

Other flow dependencies with fewer dependencies between inputs and outputs would be compatible with the given data dependencies of Add and Swap. GNATprove chooses the contracts with the most dependencies. Here, this corresponds to the actual contract for Add, but to an imprecise contract for Swap:

```plaintext
package body Only_Data_Dependencies with
  SPARK_Mode
is
  procedure Add (X : Integer) is
  begin
    V := V + X;
  end Add;
```
This results in false alarms when GNATprove verifies the dependency contract of procedure Call_Swap which calls Swap, while it succeeds in verifying the dependency contract of Call_Add which calls Add:

The most precise dependency contract for Swap would be:

If you add this precise contract in the program, then GNATprove can also verify the dependency contract of Call_Swap.

Note that the generated dependency contracts are used in the analysis of callers, but GNATprove generates no warnings or check messages if the body of Add or Swap have fewer flow dependencies, as seen above. That’s a difference between these contracts being present in the code or auto completed.

Writing Only the Flow Dependencies

When only the flow dependencies are given on a subprogram, GNATprove completes it with the only compatible data dependencies.

Take for example procedures Add and Swap as previously, expect now flow dependencies are given, but no data dependencies:
package Only_Flow_Dependencies with SPARK_Mode is
  V : Integer;

  procedure Add (X : Integer) with
    Depends => (V =>+ X);
  procedure Swap (X : in out Integer) with
    Depends => (V => X, X => V);
  procedure Call_Add (X, Y : Integer) with
    Global => (In_Out => V),
    Depends => (V =>+ (X, Y));
  procedure Call_Swap (X, Y : in out Integer) with
    Global => (In_Out => V),
    Depends => (X => Y, Y => X, V => V);
end Only_Flow_Dependencies;

The body of the unit is the same as before:

package body Only_Flow_Dependencies with SPARK_Mode is
  procedure Add (X : Integer) is
    begin
      V := V + X;
    end Add;
  procedure Swap (X : in out Integer) is
    Tmp : constant Integer := V;
    begin
      V := X;
      X := Tmp;
    end Swap;
  procedure Call_Add (X, Y : Integer) is
    begin
      Add (X);
      Add (Y);
    end Call_Add;
  procedure Call_Swap (X, Y : in out Integer) is
    begin
      Swap (X);
      Swap (Y);
      Swap (X);
    end Call_Swap;
end Only_Flow_Dependencies;

GNATprove verifies the data and flow dependencies of all subprograms, including Call_Add and Call_Swap, based on the completed contracts for Add and Swap.
Precise Generation for SPARK Subprograms

When no data or flow dependencies are given on a SPARK subprogram, GNATprove generates precise data and flow dependencies by using path-sensitive flow analysis to track data flows in the subprogram body:

- if a variable is written completely on all paths in a subprogram body, it is considered an output of the subprogram; and
- other variables that are written in a subprogram body are considered both inputs and outputs of the subprogram (even if they are not read explicitly, their output value may depend on their input value); and
- if a variable is only read in a subprogram body, it is considered an input of the subprogram; and
- all outputs are considered to potentially depend on all inputs.

Case 1: No State Abstraction

Take for example a procedure Set_Global without contract which initializes a global variable V and is called in a number of contexts:

```haskell
package Gen_Global with
  SPARK_Mode
is
  procedure Set_Global;
  procedure Do_Nothing;
  procedure Set_Global_Twice;
end Gen_Global;

package body Gen_Global with
  SPARK_Mode
is
  V : Boolean;
  procedure Set_Global is
    begin
      V := True;
      end Set_Global;
  procedure Do_Nothing is
    begin
      null;
      end Do_Nothing;
  procedure Set_Global_Twice is
    begin
      Set_Global;
      Set_Global;
      end Set_Global_Twice;
  procedure Set_Global_Conditionally (X : Boolean) with
    Global => (Output => V),
    Depends => (V => X)
  is
    begin
      if X then
```
GNATprove generates data and flow dependencies for procedure `Set_Global` that are equivalent to:

```plaintext
procedure Set_Global with
  Global => (Output => V),
  Depends => (V => null);
```

Note that the above contract would be illegal as given, because it refers to global variable `V` which is not visible at the point where `Set_Global` is declared in `gen_global.ads`. Instead, a user who would like to write this contract on `Set_Global` would have to use abstract state.

That generated contract for `Set_Global` allows GNATprove to both detect possible errors when calling `Set_Global` and to verify contracts given by the user on callers of `Set_Global`. For example, procedure `Set_Global_Twice` calls `Set_Global` twice in a row, which makes the first call useless as the value written in `V` is immediately overwritten by the second call. This is detected by GNATprove, which issues two warnings on line 18:

```
gen_global.adb:18:07: warning: statement has no effect
ngen_global.adb:18:07: warning: unused assignment to "V"
gen_global.adb:23:06: info: data dependencies proved
ngen_global.adb:23:28: info: initialization of "V" proved
ngen_global.adb:24:06: info: flow dependencies proved
ngen_global.ads:6:14: warning: subprogram "Do_Nothing" has no effect
```

Note that GNATprove also issues a warning on subprogram `Do_Nothing` which has no effect, while it correctly analyzes that `Set_Global` has an effect, even if it has the same signature with no contract as `Do_Nothing`.

GNATprove also uses the generated contract for `Set_Global` to analyze procedure `Set_Global_Conditionally`, which allows it to verify the contract given by the user for `Set_Global_Conditionally`:

```plaintext
procedure Set_Global_Conditionally (X : Boolean) with
  Global => (Output => V),
  Depends => (V => X)
```

**Case 2: State Abstraction Without Dependencies**

If an abstract state (see *State Abstraction*) is declared by the user but no dependencies are specified on subprogram declarations, then GNATprove generates data and flow dependencies which take abstract state into account.

For example, take unit `Gen_Global` previously seen, where an abstract state `State` is defined for package `Gen_Abstract_Global`, and refined into global variable `V` in the body of the package:

```plaintext
package Gen_Abstract_Global with
  SPARK_Mode,
  Abstract_State => State
is
  procedure Set_Global;
```
procedure Set_Global_Twice;

procedure Set_Global_Conditionally (X : Boolean) with
  Global => (Output => State),
  Depends => (State => X);
end Gen_Abstract_Global;

package body Gen_Abstract_Global with
  SPARK_Mode,
  Refined_State => (State => V)
is
  V : Boolean;

  procedure Set_Global is
  begin
    V := True;
  end Set_Global;

  procedure Set_Global_Twice is
  begin
    Set_Global;
    Set_Global;
  end Set_Global_Twice;

  procedure Set_Global_Conditionally (X : Boolean) with
    Refined_Global => (Output => V),
    Refined_Depends => (V => X)
  is
    Begin
      if X then
        Set_Global;
      else
        V := False;
      end if;
    end Set_Global_Conditionally;
end Gen_Abstract_Global;

We have chosen here to declare procedure Set_Global_Conditionally in gen_abstract_global.ads, and so to express its user contract abstractly. We could also have kept it local to the unit.

GNATprove gives the same results on this unit as before: it issues warnings for the possible error in Set_Global_Twice and it verifies the contract given by the user for Set_Global_Conditionally:

```
gen_abstract_global.adb:14:07: warning: statement has no effect
gen_abstract_global.adb:14:07: warning: unused assignment to "V" constituent of "State"
gen_abstract_global.adb:19:36: info: initialization of "V" constituent of "State" proved
ngen_abstract_global.ads:10:06: info: data dependencies proved
ngen_abstract_global.ads:11:06: info: flow dependencies proved``
Case 3: State Abstraction Without Refined Dependencies

If abstract state is declared by the user and abstract dependencies are specified on subprogram declarations, but no refined dependencies are specified on subprogram implementations (as described State Abstraction and Dependencies), then GNATprove generates refined data and flow dependencies for subprogram implementations.

For example, take unit Gen_Abstract_Global previously seen, where only abstract data and flow dependencies are specified:

```vhdl
package Gen_Refined_Global with
SPARK_Mode,
Abstract_State => State
is
procure Set_Global with
Global => (Output => State);
procure Set_Global_Twice with
Global => (Output => State);
procure Set_Global_Conditionally (X : Boolean) with
Global => (Output => State),
Depends => (State => X);
end Gen_Refined_Global;
```

```vhdl
package body Gen_Refined_Global with
SPARK_Mode,
Refined_State => (State => V)
is
V : Boolean;
procure Set_Global is
begin
V := True;
end Set_Global;
procure Set_Global_Twice is
begin
Set_Global;
Set_Global;
end Set_Global_Twice;
procure Set_Global_Conditionally (X : Boolean) is
begin
if X then
Set_Global;
else
Set_Global;
end if;
end Set_Global_Conditionally;
end Gen_Refined_Global;
```

GNATprove gives the same results on this unit as before: it issues warnings for the possible error in Set_Global_Twice and it verifies the contract given by the user for Set_Global_Conditionally:
Note that although abstract and refined dependencies are the same here, this is not always the case, and GNATprove will use the more precise generated dependencies to analyze calls to subprograms inside the unit.

Coarse Generation for Non-SPARK Subprograms

When no data or flow dependencies are given on a non-SPARK subprogram, GNATprove generates coarser data and flow dependencies based on the reads and writes to variables in the subprogram body:

- if a variable is written in a subprogram body, it is considered both an input and an output of the subprogram; and
- if a variable is only read in a subprogram body, it is considered an input of the subprogram; and
- all outputs are considered to potentially depend on all inputs.

For example, take unit Gen_Global previously seen, where the body of Set_Global is marked with SPARK_Mode => Off:

```ada
package Gen_Ada_Global with SPARK_Mode is
    procedure Set_Global;
    procedure Set_Global_Twice;
end Gen_Ada_Global;

package body Gen_Ada_Global with SPARK_Mode is
    V : Boolean;

    procedure Set_Global with SPARK_Mode => Off is
        begin
            V := True;
        end Set_Global;

    procedure Set_Global_Twice is
        begin
            Set_Global;
            Set_Global;
        end Set_Global_Twice;

    procedure Set_Global_Conditionally (X : Boolean) with
        Global => (Output => V),
        Depends => (V => X) is
        begin
```
if X then
    Set_Global;
else
    V := False;
end if;
end Set_Global_Conditionally;

end Gen_Ada_Global;

GNATprove generates a data and flow dependencies for procedure Set_Global that are equivalent to:

\begin{verbatim}
procedure Set_Global with
    Global  => (In_Out => V),
    Depends => (V => V);
\end{verbatim}

This is a safe over-approximation of the real contract for Set_Global, which allows to detect all possible errors of initialization and contract violation in Set_Global callers, but which may also lead to false alarms because it is imprecise. Here, GNATprove generates a wrong high message that the call to Set_Global on line 25 reads an uninitialized value for V:

\begin{verbatim}
gen_ada_global.adb:20:06: info: data dependencies proved
gen_ada_global.adb:21:06: info: flow dependencies proved
gen_ada_global.adb:25:10: high: "V" is not an input in the Global contract of...
gen_ada_global.adb:25:10: high: "V" is not initialized
gen_ada_global.adb:25:10: high: either make "V" an input in the Global contract or...

 genie_ada_global.adb:25:10: high: initialize it before use
\end{verbatim}

This is because the generated contract for Set_Global is not precise enough, and considers V as an input of the procedure. Even if the body of Set_Global is not in SPARK, the user can easily provide the precise information to GNATprove by adding a suitable contract to Set_Global, which requires to define an abstract state State like in the previous section:

\begin{verbatim}
procedure Set_Global with
    Global  => (Output => State),
    Depends => (State => null);
\end{verbatim}

With such a user contract on Set_Global, GNATprove can verify the contract of Set_Global_Conditionally without false alarms.

**Writing Dependency Contracts**

Since GNATprove generates data and flow dependencies, you don’t need in general to add such contracts if you don’t want to.

The main reason to add such contracts is when you want GNATprove to verify that the implementation respects specified data dependencies and flow dependencies. For those projects submitted to certification, verification of data coupling and input/output relations may be a required verification objective, which can be achieved automatically with GNATprove provided the specifications are written as contracts.

Even if you write dependency contracts for the publicly visible subprograms, which describe the services offered by the unit, there is no need to write similar contracts on internal subprograms defined in the unit body. GNATprove can generate data and flow dependencies on these.

Also, as seen in the previous section, the data and flow dependencies generated by GNATprove may be imprecise, in which case it is necessary to add manual contracts to avoid false alarms.
7.4.2 Writing Contracts for Program Integrity

The most common use of contracts is to ensure program integrity, that is, the program keeps running within safe boundaries. For example, this includes the fact that the control flow of the program cannot be circumvented (e.g. through a buffer overflow vulnerability) and that data is not corrupted (e.g. data invariants are preserved).

Preconditions can be written to ensure program integrity, and in particular they ensure:

- absence of run-time errors (AoRTE): no violations of language rules which would lead to raising an exception at run time (preconditions added to all subprograms which may raise a run-time error); and
- defensive programming: no execution of a subprogram from an unexpected state (preconditions added to subprograms in the public API, to guard against possible misuse by client units); and
- support of maintenance: prevent decrease in integrity (regressions, code rot) introduced during program evolution (preconditions added to internal subprograms, to guard against violations of the conditions to call these subprograms inside the unit itself); and
- invariant checking: ensure key data invariants are maintained throughout execution (preconditions added to all subprograms which may break the invariant).

For example, unit Integrity contains examples of all four kinds of preconditions:

- Precondition \( X \geq 0 \) on procedure Seen_One ensures AoRTE, as otherwise a negative value for \( X \) would cause the call to Update to fail a range check, as Update expects a non-negative value for its parameter.
- Precondition \( X < Y \) on procedure Seen_Two ensures defensive programming, as the logic of the procedure is only correctly updating global variables Max1 and Max2 to the two maximal values seen if parameters \( X \) and \( Y \) are given in strictly increasing order.
- Precondition \( X > \text{Max2} \) on procedure Update ensures support of maintenance, as this internal procedure relies on this condition on its parameter to operate properly.
- Precondition Invariant on procedure Update ensures invariant checking, as the property that \( \text{Max2} \) is less than \( \text{Max1} \) expressed in Invariant should be always respected.

```plaintext
pragma Assertion_Policy (Pre => Check);

package Integrity with
  SPARK_Mode
is
  procedure Seen_One (X : Integer) with
    Pre => X >= 0; -- AoRTE

  procedure Seen_Two (X, Y : Natural) with
    Pre => X < Y; -- defensive programming

end Integrity;

package body Integrity with
  SPARK_Mode
is
  Max1 : Natural := 0; -- max value seen
  Max2 : Natural := 0; -- second max value seen

  function Invariant return Boolean is
    (Max2 <= Max1);

  procedure Update (X : Natural) with
    Pre => X > Max2 and then -- support of maintenance
    Invariant -- invariant checking
```
is
begin
  if X > Max1 then
    Max2 := Max1;
    Max1 := X;
  elsif X < Max1 then
    Max2 := X;
  end if;
end Update;

procedure Seen_One (X : Integer) is
begin
  if X > Max2 then
    Update (X);
  end if;
end Seen_One;

procedure Seen_Two (X, Y : Natural) is
begin
  if X > Max1 then
    Max1 := Y;
    Max2 := X;
  elsif X > Max2 then
    Update (Y);
    Seen_One (X);
  else
    Seen_One (Y);
  end if;
end Seen_Two;
end Integrity;

Note that pragma Assertion_Policy (Pre => Check) in integrity.ads ensures that the preconditions on the public procedures Seen_One and Seen_Two are always enabled at run time, while the precondition on internal subprogram Update is only enabled at run time if compiled with switch -gnata (typically set only for debugging or testing). GNATprove always takes contracts into account, whatever value of Assertion_Policy.

GNATprove cannot verify that all preconditions on Integrity are respected. Namely, it cannot verify that the call to Update inside Seen_One respects its precondition, as it is not known from the calling context that Invariant holds:

Note that, although Invariant is not required to hold either on entry to Seen_Two, the tests performed in if-statements in the body of Seen_Two ensure that Invariant holds when calling Update inside Seen_Two.

To prove completely the integrity of unit Integrity, it is sufficient to add Invariant as a precondition and postcondition on every subprogram which modifies the value of global variables Max1 and Max2:

pragma Assertion_Policy (Pre => Check);

package Integrity_Proved with
package body Integrity_Proved with
SPARK_Mode
is
  Max1 : Natural := 0;  -- max value seen
  Max2 : Natural := 0;  -- second max value seen

  function Invariant return Boolean is (Max2 <= Max1);

  procedure Update (X : Natural) with
  Pre => X > Max2 and then -- support of maintenance
    Invariant,        -- invariant checking
  Post => Invariant   -- invariant checking
  is
  begin
    if X > Max1 then
      Max2 := Max1;
      Max1 := X;
    elsif X < Max1 then
      Max2 := X;
    end if;
  end Update;

  procedure Seen_One (X : Integer) is
  begin
    if X > Max2 then
      Update (X);
    end if;
  end Seen_One;

  procedure Seen_Two (X, Y : Natural) is
  begin
    if X > Max1 then
      Max1 := Y;
      Max2 := X;
    elsif X > Max2 then
      Update (Y);
      Seen_One (X);
    else
      Seen_One (Y);
    end if;
  endSeen_Two;
Here is the result of running GNATprove:

```
integrity_proved.adb:12:14: info: postcondition proved
integrity_proved.adb:26:10: info: precondition proved
integrity_proved.adb:26:18: info: range check proved
integrity_proved.adb:36:10: info: precondition proved
integrity_proved.adb:37:10: info: precondition proved
integrity_proved.adb:39:10: info: precondition proved
integrity_proved.ads:9:14: info: postcondition proved
```

### 7.4.3 Writing Contracts for Functional Correctness

Going beyond program integrity, it is possible to express functional properties of the program as subprogram contracts. Such a contract can express either partially or completely the behavior of the subprogram. Typical simple functional properties express the range/constraints for parameters on entry and exit of subprograms (encoding their type-state), and the state of the module/program on entry and exit of subprograms (encoding a safety or security automaton). For those projects submitted to certification, expressing a subprogram requirement or specification as a complete functional contract allows GNATprove to verify automatically the implementation against the requirement/specification.

For example, unit `Functional` is the same as `Integrity_Proved` seen previously, with additional functional contracts:

- The postcondition on procedure `Update` (expressed as a `Post` aspect) is a complete functional description of the behavior of the subprogram. Note the use of an if-expression.

- The postcondition on procedure `Seen_Two` (expressed as a `Post` aspect) is a partial functional description of the behavior of the subprogram.

- The postcondition on procedure `Seen_One` (expressed as a `Contract_Cases` aspect) is a complete functional description of the behavior of the subprogram. There are three cases which correspond to different possible behaviors depending on the values of parameter `X` and global variables `Max1` and `Max2`. The benefit of expressing the postcondition as contract cases is both the gain in readability (no need to use ‘Old for the guards, as in the postcondition of `Update`) and the automatic verification that the cases are disjoint and complete.

Note that global variables `Max1` and `Max2` are referred to through public accessor functions `Max_Value_Seen` and `Second_Max_Value_Seen`. These accessor functions can be declared after the contracts in which they appear, as contracts are semantically analyzed only at the end of package declaration.

```ada
pragma Assertion_Policy (Pre => Check);

package Functional with
   SPARK_Mode
is
   procedure Seen_One (X : Integer) with
      Pre => X >= 0 and then -- AoRTE
      Invariant, -- invariant checking
      Post => Invariant, -- invariant checking
      Contract_Cases => -- full functional
      (X > Max_Value_Seen =>
       -- max value updated
       Max_Value_Seen = X and
       Second_Max_Value_Seen = Max_Value_Seen'Old,
       X > Second_Max_Value_Seen and
       X < Max_Value_Seen =>
```
-- second max value updated  
Max_Value_Seen = Max_Value_Seen'Old and  
Second_Max_Value_Seen = X,  
X = Max_Value_Seen or  
X <= Second_Max_Value_Seen =>  
-- no value updated  
Max_Value_Seen = Max_Value_Seen'Old and  
Second_Max_Value_Seen = Second_Max_Value_Seen'Old);  

procedure Seen_Two (X, Y : Natural) with  
Pre => X < Y and then -- defensive programming  
Invariant, -- invariant checking  
Post => Invariant and then -- invariant checking  
Max_Value_Seen > 0 and then -- partial functional  
Max_Value_Seen /= Second_Max_Value_Seen;  

function Invariant return Boolean;  
function Max_Value_Seen return Integer;  
function Second_Max_Value_Seen return Integer;  

end Functional;  

package body Functional with  
SPARK_Mode  
is  
Max1 : Natural := 0; -- max value seen  
Max2 : Natural := 0; -- second max value seen  

function Invariant return Boolean is (Max2 <= Max1);  
function Max_Value_Seen return Integer is (Max1);  
function Second_Max_Value_Seen return Integer is (Max2);  

procedure Update (X : Natural) with  
Pre => X > Max2 and then -- support of maintenance  
Invariant, -- invariant checking  
Post => Invariant and then -- invariant checking  
if X > Max1'Old then -- complete functional  
Max2 = Max1'Old and Max1 = X  
elsif X < Max1'Old then  
Max2 = X and Max1 = Max1'Old  
else  
Max2 = Max2'Old and Max1 = Max1'Old)  
is  
begin  
if X > Max1 then  
Max2 := Max1;  
Max1 := X;  
elsif X < Max1 then  
Max2 := X;  
end if;  
end Update;  

procedure Seen_One (X : Integer) is  
begin
GNATprove manages to prove automatically almost all of these functional contracts, except for the postcondition of `Seen_Two` (note in particular the proof that the contract cases for `Seen_One` on line 10 are disjoint and complete):

The counterexample displayed for the postcondition not proved corresponds to a case where `Max1 = Max2 = 2` on entry to procedure `Seen_Two`. By highlighting the path for the counterexample in GNAT Studio (see Running GNATprove from GNAT Studio), the values of parameters for this counterexample are also displayed, here `X = 0` and `Y = 1`. With these values, `Max1` and `Max2` would still be equal to 2 on exit, thus violating the part of the postcondition stating that `Max_Value_Seen /= Second_Max_Value_Seen`.

Another way to see it is to run GNATprove in mode `per_path` (see Running GNATprove from the Command Line or Running GNATprove from GNAT Studio), and highlight the path on which the postcondition is not proved, which shows that when the last branch of the if-statement is taken, the following property is not proved:

The missing piece of information here is that `Max1` and `Max2` are never equal, except when they are both zero (the initial value). This can be added to function `Invariant` as follows:

With this more precise definition for `Invariant`, all contracts are now proved by GNATprove:
In general, it may be needed to further refine the preconditions of subprograms to be able to prove their functional postconditions, to express either specific constraints on their calling context, or invariants maintained throughout the execution.

### 7.4.4 Writing Contracts on Main Programs

Parameterless procedures and parameterless functions with Integer return type, that are in their own compilation unit, are identified by GNATprove as potential main subprograms. These subprograms are special because they can serve as an entry point to the program. If a main subprogram has a precondition, SPARK will generate a check that this precondition holds at the beginning of the execution of the main program, assuming the `Initial_Condition` aspects of all with’ed packages.

Note that apart from this additional check, main subprograms behave like any other subprogram. They can be called from anywhere, and their preconditions need to be checked when they are called.

### 7.4.5 Writing Contracts on Imported Subprograms

Contracts are particularly useful to specify the behavior of imported subprograms, which cannot be analyzed by GNATprove. It is compulsory to specify in data dependencies the global variables these imported subprograms may read and/or write, otherwise GNATprove assumes null data dependencies (no global variable read or written).

**Note:** A subprogram whose implementation is not available to GNATprove, either because the corresponding unit body has not been developed yet, or because the unit body is not part of the files analyzed by GNATprove (see Specifying Files To Analyze and Excluding Files From Analysis), is treated by GNATprove like an imported subprogram.

**Note:** Intrinsic subprograms such as arithmetic operations and shift/rotate functions are handled specially by GNATprove. Except for shift/rotate operations with a user-provided functional contract (precondition, postcondition or contract cases) which are treated like regular functions.

For example, unit `Gen_Imported_Global` is a modified version of the `Gen_Abstract_Global` unit seen previously in Generation of Dependency Contracts, where procedure `Set_Global` is imported from C:

```plaintext
package Gen_Imported_Global with
SPARK_Mode,
Abstract_State => State
is
  procedure Set_Global with
```
Note that we added data dependencies to procedure Set_Global, which can be used to analyze its callers. We did not add flow dependencies, as they are the same as the auto completed ones (see Auto Completion for Incomplete Contracts).

Note that we added an Address aspect to global variable V, so that it can be read/written from a C file.

GNATprove gives the same results on this unit as before: it issues warnings for the possible error in Set_Global_Twice and it verifies the contract given by the user for Set_Global_Conditionally:
It is also possible to add functional contracts on imported subprograms, which GNATprove uses to prove properties of their callers. It is compulsory to specify in a precondition the conditions for calling these imported subprograms without errors, otherwise GNATprove assumes a default precondition of True (no constraints on the calling context). One benefit of these contracts is that they are verified at run time when the corresponding assertion is enabled in Ada (either with pragma Assertion_Policy or compilation switch -gnata).

Note: A subprogram whose implementation is not in SPARK is treated by GNATprove almost like an imported subprogram, except that coarse data and flow dependencies are generated (see Coarse Generation for non-SPARK Subprograms). In particular, unless the user adds a precondition to such a subprogram, GNATprove assumes a default precondition of True.

For example, unit Functional_Imported is a modified version of the Functional_Proved unit seen previously in Writing Contracts for Functional Correctness, where procedures Update and Seen_One are imported from C:

```ada
pragma Assertion_Policy (Pre => Check);

package Functional_Imported with
  SPARK_Mode,
  Abstract_State => Max_And_Snd,
  Initializes => Max_And_Snd
is
  procedure Seen_One (X : Integer) with
    Import,
    Convention => C,
    Global => (In_Out => Max_And_Snd),
    Pre => X >= 0 and then -- AoRTE
    Invariant, -- invariant checking
    Post => Invariant, -- invariant checking
    Contract_Cases => -- full functional
      (X > Max_Value_Seen =>
       -- max value updated
       Max_Value_Seen = X and
       Second_Max_Value_Seen = Max_Value_Seen'Old,
       X > Second_Max_Value_Seen and
       X < Max_Value_Seen =>
       -- second max value updated
       Max_Value_Seen = Max_Value_Seen'Old and
       Second_Max_Value_Seen = X,
       X = Max_Value_Seen or
       X <= Second_Max_Value_Seen =>
       -- no value updated
       Max_Value_Seen = Max_Value_Seen'Old and
       Second_Max_Value_Seen = Second_Max_Value_Seen'Old);

  procedure Seen_Two (X, Y : Natural) with
    Pre => X < Y and then -- defensive programming
    Invariant,
    Post => Invariant and then -- invariant checking
    Max_Value_Seen > 0 and then -- partial functional
    Max_Value_Seen /= Second_Max_Value_Seen;

  function Invariant return Boolean;

  function Max_Value_Seen return Integer;
```
function Second_Max_Value_Seen return Integer;
end Functional_Imported;

with System.Storage_Elements;

package body Functional_Imported with
  SPARK_Mode,
  Refined_State => (Max_And_Snd => (Max, Snd))
is
  Max : Natural := 0; -- max value seen
  for Max'Address use System.Storage_Elements.To_Address (16#8000_0000#);
  Snd : Natural := 0; -- second max value seen
  for Snd'Address use System.Storage_Elements.To_Address (16#8000_0004#);

  function Invariant return Boolean is
    (if Max = 0 then Snd = 0 else Snd < Max);
  function Max_Value_Seen return Integer is (Max);
  function Second_Max_Value_Seen return Integer is (Snd);

  procedure Update (X : Natural) with
    Import,
    Convention => C,
    Global => (In_Out => (Max, Snd)),
    Pre => X > Snd and then -- support of maintenance
      Invariant, -- invariant checking
    Post => Invariant and then -- invariant checking
      (if X > Max'Old then -- complete functional
        Snd = Max'Old and Max = X
      elsif X < Max'Old then
        Snd = X and Max = Max'Old
      else
        Snd = Snd'Old and Max = Max'Old);

  procedure Seen_Two (X, Y : Natural) is
  begin
    if X > Max then
      Max := Y;
      Snd := X;
    elsif X > Snd then
      Update (Y);
      Seen_One (X);
    else
      Seen_One (Y);
    end if;
  end Seen_Two;
end Functional_Imported;

Note that we added data dependencies to the imported procedures, as GNATprove would assume otherwise incorrectly null data dependencies.

As before, all contracts are proved by GNATprove:
7.4.6 Contextual Analysis of Subprograms Without Contracts

It may be convenient to create local subprograms without necessarily specifying a contract for these. GNATprove
attempts to perform a contextual analysis of these local subprograms without contract, at each call site, as if the code
of the subprograms was inlined. Thus, the analysis proceeds in that case as if it had the most precise contract for the
local subprogram, in the context of its calls.

Let’s consider as previously a subprogram which adds two to its integer input:

```ada
package Arith_With_Local_Subp with SPARK_Mode is
    procedure Add_Two (X : in out Integer) with
        Pre => X <= Integer’Last - 2,
        Post => X = X’Old + 2;
end Arith_With_Local_Subp;
```

And let’s implement it by calling two local subprograms without contracts (which may or not have a separate declara-
tion), which each increment the input by one:

```ada
package body Arith_With_Local_Subp with SPARK_Mode is
    -- Local procedure without external visibility
    procedure Increment_In_Body (X : in out Integer) is begin X := X + 1; end Increment_In_Body;

    procedure Add_Two (X : in out Integer) is
        -- Local procedure defined inside Add_Two
        procedure Increment_Nested (X : in out Integer) is begin X := X + 1; end Increment_Nested;

        begin
            Increment_In_Body (X);
            Increment_Nested (X);
        end Ad
```
that the contract of \texttt{Add\_Two} is respected. But since it analyzes these subprograms in the context of their calls only, it proves here that no overflow is possible, and that the two increments correctly implement the contract of \texttt{Add\_Two}:

```
1  arith_with_local_subp.adb:7:14: info: overflow check proved, in call inlined at arith_
   → with_local_subp.adb:19
2  arith_with_local_subp.adb:15:17: info: overflow check proved, in call inlined at arith_
   → with_local_subp.adb:20
3  arith_with_local_subp.ads:6:14: info: postcondition proved
4  arith_with_local_subp.ads:6:24: info: overflow check proved
```

This contextual analysis is available only for regular functions (not expression functions) or procedures that are not externally visible (not declared in the public part of the unit), without contracts (any of \texttt{Global}, \texttt{Depends}, \texttt{Pre}, \texttt{Post}, \texttt{Contract\_Cases}), and respect the following conditions:

- not dispatching
- not marked \texttt{No\_Return}
- not a generic instance
- not defined in a generic instance
- not defined in a protected type
- without a parameter of unconstrained record type with discriminant dependent components
- without a parameter or result of deep type (access type or composite type containing an access type)
- not a traversal function

Subprograms that respects all of the above conditions are candidates for contextual analysis, and calls to such subprograms are inlined provided the subprogram and its calls respect the following additional conditions:

- does not contain nested subprogram or package declarations or instantiations
- not recursive
- has a single point of return at the end of the subprogram
- not called in an assertion or a contract
- not called in a potentially unevaluated context
- not called before its body is seen

If any of the above conditions is violated, GNATprove issues an info message to explain why the subprogram could not be analyzed in the context of its calls, and then proceeds to analyze it normally, using the default contract. Otherwise, both flow analysis and proof are done for the subprogram in the context of its calls.

Note that it is very simple to prevent contextual analysis of a local subprogram, by adding a contract to it, for example a simple \texttt{Pre => True or Global => null}. To prevent contextual analysis of all subprograms, pass the switch \texttt{--no-inlining} to GNATprove. This may be convenient during development if the ultimate goal is to add contracts to subprograms to analyze them separately, as contextual analysis may cause the analysis to take much more time and memory.

### 7.4.7 Subprogram Termination

GNATprove is only concerned with partial correctness of subprograms, that is, it only checks that the contract of a subprogram holds when it terminates normally. What is more, GNATprove will enforce that no exception will be raised at runtime. Together, these two points ensure that every SPARK subprogram formally verified using GNATprove will always return normally in a state that respects its postcondition, as long as it terminates.
In general, GNATprove does not attempt to verify termination of subprograms. It can be instructed to do so using a GNATprove specific Annotate pragma. On the following example, we instruct GNATprove that the five \( F \) functions should terminate:

``` LombText
package Terminating_Annotations with SPARK_Mode is
  function F_Rec (X : Natural) return Natural;
  pragma Annotate (GNATprove, Terminating, F_Rec);

  function F_While (X : Natural) return Natural;
  pragma Annotate (GNATprove, Terminating, F_While);

  function F_Not_SPARK (X : Natural) return Natural;
  pragma Annotate (GNATprove, Terminating, F_Not_SPARK);

  procedure Not_SPARK (X : Natural);

  function F_Call (X : Natural) return Natural;
  pragma Annotate (GNATprove, Terminating, F_Call);

  function F_Term (X : Natural) return Natural;
  pragma Annotate (GNATprove, Terminating, F_Term);
end Terminating_Annotations;
```

If every subprogram in a package is terminating, the package itself can be annotated with the terminating annotation. If the annotation is located on a generic package, then it should be valid for every instance of the package.

An aspect can be used instead of a pragma for both packages and subprograms:

```LombText
package Pack with
  Annotate => (GNATprove, Terminating)
is
  procedure Proc with
    Annotate => (GNATprove, Terminating);
...;
```

If a subprogram in SPARK is explicitly annotated as terminating, flow analysis will attempt to make sure that all the paths through the subprogram effectively return. In effect, it will look for while loops with no loop variants, recursive calls and calls to subprograms which are not known to be terminating. If GNATprove cannot make sure that the annotated subprogram is always terminating, it will then emit a failed check. As an example, let us consider the following implementation of the five \( F \) functions:

```LombText
package body Terminating_Annotations with SPARK_Mode is
  function F_Rec (X : Natural) return Natural is
    begin
      if X = 0 then
        return 0;
      else
        return F_Rec (X - 1);
      end if;
    end F_Rec;

  function F_While (X : Natural) return Natural is
    Y : Natural := X;
    begin
      while Y > 0 loop
        Y := Y - 1;
      end loop;
```

As can be easily verified by review, all these functions terminate, and all return 0. As can be seen below, GNATprove will fail to verify that \( F_\text{Rec} \), \( F_\text{While} \), and \( F_\text{Call} \) terminate.

Let us look at each function to understand what happens. The function \( F_\text{Rec} \) is recursive, and the function \( F_\text{While} \) contains a while loop. Both cases can theoretically lead to an infinite path in the subprogram, which is why GNATprove cannot verify that they terminate. GNATprove does not complain about not being able to verify the termination of \( F_\text{Not_SPARK} \). Clearly, it is not because it could verify it, as it contains exactly the same loop as \( F_\text{While} \). It is because, as the body of \( F_\text{Not_SPARK} \) has been excluded from analysis using \( \text{SPARK\_Mode} \Rightarrow \text{Off} \), GNATprove does not attempt to prove that it terminates. When looking at the body of \( F_\text{Call} \), we can see that it calls a procedure.
Not_SPARK. Clearly, this procedure is terminating, as it does not do anything. But, as the body of No_SPARK has been hidden from analysis using SPARK_Mode => Off, GNATprove cannot deduce that it terminates. As a result, it stays in the safe side, and assumes that Not_SPARK could loop, which causes the verification of F_Call to fail. Finally, GNATprove is able to verify that F_Term terminates, though it contains a while loop. Indeed, the number of possible iterations of the loop has been bounded using a Loop_Variant. Also note that, though it was not able to prove termination of F_Rec, F_While, and F_Call, GNATprove will still trust the annotation and consider them as terminating when verifying F_Term.

**Note:** Possible nontermination of a subprogram may influence GNATprove proof capabilities. Indeed, to avoid soundness issues due to nontermination in logical formulas, GNATprove will not be able to see the contract of nonterminating functions if they are called from definitions of constants, from contracts, or from assertions. In such a case, an information message will be emitted, stating that (implicit) contracts of the function are not available for proof. This message won’t appear if a Terminating annotation is supplied for the function as explained above.

### 7.5 How to Write Object Oriented Contracts

Object Oriented Programming (OOP) may require the use of special *Class-Wide Subprogram Contracts* for dispatching subprograms, so that GNATprove can check Liskov Substitution Principle on every overriding subprogram.

#### 7.5.1 Object Oriented Code Without Dispatching

In the special case where OOP is used without dispatching, it is possible to use the regular *Subprogram Contracts* instead of the special *Class-Wide Subprogram Contracts*.

For example, consider a variant of the Logging and Range_Logging units presented in *Class-Wide Subprogram Contracts*, where no dispatching is allowed. Then, it is possible to use regular preconditions and postconditions as contracts, provided Log_Type is publicly declared as an untagged private type in both units:

```gherkin
package Logging_No_Dispatch with
    SPARK_Mode
is
    Max_Count : constant := 10_000;

    type Log_Count is range 0 .. Max_Count;

    type Log_Type is private;

    function Log_Size (Log : Log_Type) return Log_Count;

    procedure Init_Log (Log : out Log_Type) with
        Post => Log_Size (Log) = 0;

    procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
        Pre => Log_Size (Log) < Max_Count,
        Post => Log_Size (Log) = Log_Size (Log)'Old + 1;

private

    subtype Log_Index is Log_Count range 1 .. Max_Count;
    type Integer_Array is array (Log_Index) of Integer;

    type Log_Type is tagged record
```
Log_Data : Integer_Array;
Log_Size : Log_Count;
end record;

function Log_Size (Log : Log_Type) return Log_Count is (Log.Log_Size);
end Logging_No_Dispatch;

with Logging_No_Dispatch; use Logging_No_Dispatch;

package Range_Logging_No_Dispatch with
SPARK_Mode
is
type Log_Type is private;

function Log_Size (Log : Log_Type) return Log_Count;
function Log_Min (Log : Log_Type) return Integer;
function Log_Max (Log : Log_Type) return Integer;

procedure Init_Log (Log : out Log_Type) with
  Post => Log_Size (Log) = 0 and
         Log_Min (Log) = Integer'Last and
         Log_Max (Log) = Integer'First;

procedure Append_To_Log (Log : in out Log_Type; Incr : in Integer) with
  Pre => Log_Size (Log) < Logging_No_Dispatch.Max_Count,
  Post => Log_Size (Log) = Log_Size (Log)'Old + 1 and
         Log_Min (Log) = Integer'Min (Log_Min (Log)'Old, Incr) and
         Log_Max (Log) = Integer'Max (Log_Max (Log)'Old, Incr);

private

type Log_Type is tagged record
  Log : Logging_No_Dispatch.Log_Type;
  Min_Entry : Integer;
  Max_Entry : Integer;
end record;

function Log_Size (Log : Log_Type) return Log_Count is (Log_Size (Log.Log));
function Log_Min (Log : Log_Type) return Integer is (Log.Min_Entry);
function Log_Max (Log : Log_Type) return Integer is (Log.Max_Entry);
end Range_Logging_No_Dispatch;

### 7.5.2 Writing Contracts on Dispatching Subprograms

Whenever dispatching is used, the contract that applies in proof to a dispatching call is the class-wide contract, defined as the first one present in the following list:

1. the class-wide precondition (resp. postcondition) attached to the subprogram
2. or otherwise the class-wide precondition (resp. postcondition) being inherited by the subprogram from the subprogram it overrides
3. or otherwise the default class-wide precondition (resp. postcondition) of True.

For abstract subprograms (on interfaces or regular tagged types), only a class-wide contract can be specified. For other dispatching subprograms, it is possible to specify both a regular contract and a class-wide contract. In such a case, GNATprove uses the regular contract to analyze static calls to the subprogram and the class-wide contract to analyze dispatching calls to the subprogram, and it checks that the specific contract is a refinement of the class-wide contract, as explained in *Mixing Class-Wide and Specific Subprogram Contracts*.

Let’s consider the various cases that may occur when overridding a subprogram:

```plaintext
package Geometry with
  SPARK_Mode is
  type Shape is tagged record
    Pos_X, Pos_Y : Float;
  end record;

  function Valid (S : Shape) return Boolean is
    (S.Pos_X in -100.0 .. 100.0 and S.Pos_Y in -100.0 .. 100.0);

  procedure Operate (S : in out Shape) with
    Pre'Class => Valid (S);

  procedure Set_Default (S : in out Shape) with
    Post'Class => Valid (S);

  procedure Set_Default_Repeat (S : in out Shape) with
    Post'Class => Valid (S);

  procedure Set_Default_No_Post (S : in out Shape);

  type Rectangle is new Shape with record
    Len_X, Len_Y : Float;
  end record;

  function Valid (S : Rectangle) return Boolean is
    (Valid (Shape (S)) and S.Len_X in 0.0 .. 10.0 and S.Len_Y in 0.0 .. 10.0);

  procedure Operate (S : in out Rectangle);

  procedure Set_Default (S : in out Rectangle);

  procedure Set_Default_Repeat (S : in out Rectangle) with
    Post'Class => Valid (S);

  procedure Set_Default_No_Post (S : in out Rectangle) with
    Post'Class => Valid (S);
end Geometry;
```

In package Geometry, a type Shape is derived in a type Rectangle. A function Shape.Valid defines what it is to be a valid shape. It is overridden by Rectangle.Valid which defines what it is to be a valid rectangle. Here, a valid rectangle is also a valid shape, but that need not be the case. Procedure Set_Default and its variants demonstrate the various configurations that can be found in practice:

1. The overridden subprogram Shape.Set_Default defines a class-wide contract (here only a postcondition), which is inherited in the overriding subprogram Rectangle.Set_Default. By the semantics of Ada, the postcondition of Shape.Set_Default calls Shape.Valid, while the inherited postcondition of Rectangle.Set_Default calls Rectangle.Valid.
2. Both the overridden subprogram `Shape.Set_Default_Repeat` and the overriding subprogram `Rectangle.Set_Default_Repeat` define a class-wide contract (here only a postcondition). Here, since the contract is simply repeated, this is equivalent to case 1 above of inheriting the contract: the postcondition of `Shape.Set_Default_Repeat` calls `Shape.Valid`, while the postcondition of `Rectangle.Set_Default_Repeat` calls `Rectangle.Valid`.

3. Only the overriding subprogram `Rectangle.Set_Default_No_Post` defines a class-wide contract (here only a postcondition). The default class-wide postcondition of `True` is used for the overridden `Shape.Set_Default_No_Post`.

In case 1, the overriding subprogram satisfies Liskov Substitution Principle by construction, so GNATprove emits no check in that case. Note that this is not the same as saying that `Shape.Set_Default` and `Rectangle.Set_Default` have the same contract: here the two postconditions differ, as one calls `Shape.Valid`, while the other calls `Rectangle.Valid`.

In case 2, GNATprove checks that Liskov Substitution Principle is verified between the contracts of the overridden and the overriding subprograms. Here, it checks that the postcondition of `Rectangle.Set_Default_Repeat` is stronger than the postcondition of `Shape.Set_Default_Repeat`.

In case 3, GNATprove also checks that Liskov Substitution Principle is verified between the default contract of the overridden subprogram and the specified contract of the overriding subprograms. Here, only a postcondition is specified for `Rectangle.Set_Default_No_Post`, so it is indeed stronger than the default postcondition of `Shape.Set_Default_No_Post`.

Hence the results of GNATprove’s analysis on this program:

```
geometry.ads:34:20: info: class-wide postcondition is stronger than overridden one
geometry.ads:37:20: info: class-wide postcondition is stronger than overridden one
```

Let’s consider now calls to these subprograms in procedure `Use_Geometry`:

```haskell
with Geometry; use Geometry;

procedure Use_Geometry (S : in out Shape'Class) with SPARK_Mode is begin
    S.Set_Default;
    S.Operate;
    S.Set_Default_Repeat;
    S.Operate;
    S.Set_Default_No_Post;
    S.Operate;
end Use_Geometry;
```

Here are the results of GNATprove’s analysis on this program:

```
use_geometry.adb:8:05: info: precondition proved
use_geometry.adb:11:05: info: precondition proved
use_geometry.adb:14:05: medium: precondition might fail, cannot prove Valid (S) ...
   [possible explanation: call at line 13 should mention S (for argument S) in a ...]
```

Parameter `S` is of class-wide type `Shape'Class`, so it can be dynamically of both types `Shape` or `Rectangle`. All calls on `S` are dispatching. In this program, GNATprove needs to check that the precondition of the calls to `Operate` is satisfied. As procedures `Shape.Set_Default` and `Shape.Set_Default_Repeat` state precisely this condition in postcondition, the precondition to the calls to `Operate` that follow can be proved. As procedure `Shape`. …
Set_Default_No_Post has no postcondition, the precondition to the last call to Operate cannot be proved. Note that these proofs take into account both possible types of S, for example:

- If S is dynamically a shape, then the call to Shape.Set_Default on line 7 ensures that Shape.Valid holds, which ensures that the precondition to the call to Shape.Operate is satisfied on line 8.
- If S is dynamically a rectangle, then the call to Rectangle.Set_Default on line 7 ensures that Rectangle.Valid holds, which ensures that the precondition to the call to Rectangle.Operate is satisfied on line 8.

7.5.3 Writing Contracts on Subprograms with Class-wide Parameters

Subprograms with class-wide parameters are not in general dispatching subprograms, hence they are specified through regular Subprogram Contracts, not Class-Wide Subprogram Contracts. Inside the regular contract, calls on primitive subprograms of the class-wide parameters are dispatching though, like in the code. For example, consider procedure More_Use_Geometry which takes four class-wide parameters of type Shape'Class, which can all be dynamically of both types Shape or Rectangle:

```plaintext
with Geometry; use Geometry;

procedure More_Use_Geometry (S1, S2, S3, S4 : in out Shape'Class) with
  SPARK_Mode,
  Pre => S1.Valid
is
begin
  S1.Operate;
  if S2.Valid then
    S2.Operate;
  end if;
  S3.Set_Default;
  S3.Operate;
  S4.Operate;
end More_Use_Geometry;
```

The precondition of More_Use_Geometry specifies that S1.Valid holds, which takes into account both possible types of S1:

- If S1 is dynamically a shape, then the precondition specifies that Shape.Valid holds, which ensures that the precondition to the call to Shape.Operate is satisfied on line 8.
- If S1 is dynamically a rectangle, then the precondition specifies that Rectangle.Valid holds, which ensures that the precondition to the call to Rectangle.Operate is satisfied on line 8.

Similarly, the test on S2.Valid on line 10 ensures that the precondition to the call to S2.Operate on line 11 is satisfied, and the call to S3.Set_Default on line 14 ensures through its postcondition that the precondition to the call to S3.Operate on line 15 is satisfied. But no precondition or test or call ensures that the precondition to the call to S4.Operate on line 17 is satisfied. Hence the results of GNATprove’s analysis on this program:

```plaintext
more_use_geometry.adb:8:06: info: precondition proved
more_use_geometry.adb:11:09: info: precondition proved
more_use_geometry.adb:15:06: info: precondition proved
more_use_geometry.adb:17:06: medium: precondition might fail, cannot prove Valid (S)
  →[possible explanation: precondition of subprogram at line 3 should mention S4]```

7.6 How to Write Package Contracts

Like for subprogram contracts, GNATprove can generate default package contracts when not specified by a user. By default, GNATprove does not require the user to write any package contracts.

The default state abstraction generated by GNATprove maps every internal global variable to a different internal abstract state (which is not really abstract as a result).

The default package initialization generated by GNATprove lists all variables initialized either at declaration or in the package body statements. The generated Initializes aspect is an over-approximation of the actual Initializes aspect. All outputs are considered to be initialized from all inputs. For example, consider package Init_Data which initializes all its global variables during elaboration, from either constants or variables:

```plaintext
package External_Data with
  SPARK_Mode
is
  Val : Integer with Import;
end External_Data;

with External_Data;
pragma Elaborate_All(External_Data);

package Init_Data with
  SPARK_Mode
is
  pragma Elaborate_Body;
  Start_From_Zero : Integer := 0;
  Start_From_Val   : Integer := External_Data.Val;
  Start_From_Zero_Bis : Integer;
  Start_From_Val_Bis : Integer;
end Init_Data;

package body Init_Data with
  SPARK_Mode
is
  begin
  Start_From_Zero_Bis := 0;
  Start_From_Val_Bis := External_Data.Val;
end Init_Data;
```

GNATprove generates a package initialization contract on package Init_Data which is equivalent to:

```
Initializes => (Start_From_Zero => External_Data.Val,
                Start_From_Zero_Bis => External_Data.Val,
                Start_From_Val   => External_Data.Val,
                Start_From_Val_Bis => External_Data.Val)
```

As a result, GNATprove can check that global variables are properly initialized when calling the main procedure Main_Proc, and it does not issue any message when analyzing this code:

```plaintext
with Init_Data;
procedure Main_Proc with
  SPARK_Mode
is
  Tmp : Integer;
begin
  Tmp := Init_Data.Start_From_Zero;
```
The user may specify explicitly package contracts to:

- name explicitly the parts of state abstraction that can be used in subprogram dependency contracts, in order to
  *Address Data and Control Coupling*; or

- improve scalability and running time of GNATprove's analysis, as a single explicit abstract state may be mapped
to hundreds of concrete global variables, which would otherwise be considered separately in the analysis; or

- check that initialization of global data at elaboration is as specified in the specified package initialization con-
  tracts.

### 7.7 How to Write Loop Invariants

As described in *Loop Invariants*, proving properties of subprograms that contain loops may require the addition of
explicit loop invariant contracts. This section describes a systematic approach for writing loop invariants.

#### 7.7.1 Automatic Unrolling of Simple For-Loops

GNATprove automatically unrolls simple for-loops, defined as:

- for-loops over a range,
- with a number of iterations smaller than 20,
- without *Loop Invariants* or *Loop Variants*,
- that declare no local variables, or only variables of scalar type.

In addition, GNATprove always unrolls loops of the form `for J in 1 .. 1 loop` that don’t have a *Loop Invari-
ants* or *Loop Variants*, even when they declare local variables of non-scalar type.

As a result of unrolling, GNATprove conveys the exact meaning of the loop to provers, without requiring a loop
invariant. While this is quite powerful, it is best applied to loops where the body of the loop is small, otherwise the
unrolling may lead to complex formulas that provers cannot prove.

For example, consider the subprograms *Init* and *Sum* below:

```plaintext
package Loop_Unrolling with
  SPARK_Mode
is
  subtype Index is Integer range 1 .. 10;
type Arr is array (Index) of Integer;

procedure Init (A : out Arr) with
  Post => (for all J in Index => A(J) = J);

function Sum (A : Arr) return Integer with
  Pre => (for all J in Index => A(J) = J),
  Post => Sum'Result = (A'First + A'Last) * A'Length / 2;
end Loop_Unrolling;
```
As the loops in both subprograms are simple for-loops, GNATprove unrolls them and manages to prove the postconditions of `Init` and `Sum` without requiring a loop invariant:

```
package body Loop_Unrolling with SPARK_Mode is
  procedure Init (A : out Arr) is begin
    for J in Index loop
      A (J) := J;
    end loop;
  end Init;

  function Sum (A : Arr) return Integer is
    Result : Integer := 0;
    begin
      for J in Index loop
        Result := Result + A (J);
      end loop;
      return Result;
    end Sum;
  end Loop_Unrolling;
```

Automatic loop unrolling can be disabled locally by explicitly adding a default loop invariant at the start of the loop:

```
for X in A .. B loop
  pragma Loop_Invariant (True);
  ...
end loop;
```

It can also be disabled globally by using the switch `--no-loop-unrolling`.

### 7.7.2 Automatically Generated Loop Invariants

In general, GNATprove relies on the user to manually supply the necessary information about variables modified by loop statements in the loop invariant. Though variables which are not modified in the loop need not be mentioned in the invariant, it is usually necessary to state explicitly the preservation of unmodified object parts, such as record or array components. In particular, when a loop modifies a collection, which can be either an array or a container (see `Formal Containers Library`), it may be necessary to state in the loop invariant those parts of the collection that have not been modified up to the current iteration. This property called frame condition in the scientific literature is essential for GNATprove, which otherwise must assume that all elements in the collection may have been modified. Special care should be taken to write adequate frame conditions, as they usually look obvious to programmers, and so it is very common to forget to write them and not being able to realize what’s the problem afterwards.

To alleviate this problem, the GNATprove tool generates automatically frame conditions in some cases. As examples of use of such generated frame conditions, consider the code of procedures `Update_Arr` and `Update_Rec` below:

```
package Frame_Condition with SPARK_Mode is
```

...
Without this feature, GNATprove would not be able to prove the postconditions of either procedure because:

- To prove the postcondition of `Update_Arr`, one needs to know that only the indexes up to `Idx` have been updated in the loop.
- To prove the postcondition of `Update_Rec`, one needs to know that only the component `A` of record `R` has been updated in the loop.

Thanks to this feature, GNATprove automatically proves the postconditions of both procedures, without the need for loop invariants:

```plaintext
frame_condition.ads:8:14: info: postcondition proved
frame_condition.ads:8:14: info: range check proved
frame_condition.ads:8:37: info: range check proved
frame_condition.ads:16:14: info: postcondition proved
```

In particular, it is able to infer the preservation of unmodified components of record variables. It also handles unmodified components of array variables as long as they are preserved at every index in the array. As an example, consider the following loop which only updates some record component of a nested data structure:

```plaintext
procedure Preserved_Fields with SPARK_Mode is
  type R is record
    F1 : Integer := 0;
end record;
```
Despite the absence of a loop invariant in the above code, GNATprove is able to prove that the assertions on lines 19-21 about variable D which is modified in the loop are proved, thanks to the generated loop invariants:

Note that GNATprove will not generate a frame condition for a record component if the record variable is modified as a whole either through an assignment or through a procedure call, et cetera, even if the component happens to be preserved by the modification.

GNATprove can also infer preservation of unmodified array components for arrays that are only updated at constant indexes or at indexes equal to the loop index. As an example, consider the following loops, only updating some cells of a matrix of arrays:

```ada
procedure Preserved_Components with SPARK_Mode is

  type A is array (1 .. 100) of Natural with Default_Component_Value => 1;

  type A_Matrix is array (1 .. 100, 1 .. 100) of A;

  M : A_Matrix;

begin
  L1: for I in 1 .. 100 loop
      M (I, 1) (1 .. 50) := (others => 0);
      pragma Assert (for all K1 in 1 .. 100 =>
          M (K1, 1) (1 .. 50) = M'Loop_Entry (K1, 1) (1 .. 50));
  end loop L1;

  L2: for I in 1 .. 99 loop
      M (I + 1, I) (I .. 100) := (others => 0);

end Preserved_Components;
```
Despite the absence of a loop invariant in the above code, GNATprove can successfully verify the assertion on line 13 thanks to the generated loop invariant. Note that loop invariant generation for preserved array components is based on heuristics, and that it is therefore far from complete. In particular, it does not handle updates to variable indexes different from the loop index, as can be seen by the failed attempt to verify the assertion on line 22. GNATprove does not either handle dependences between indexes in an update, resulting in the failed attempt to verify the assertion on line 33:

7.7.3 The Four Properties of a Good Loop Invariant

A loop invariant can describe more or less precisely the behavior of a loop. What matters is that the loop invariant allows proving absence of run-time errors in the subprogram, that the subprogram respects its contract, and that the loop invariant itself holds at each iteration of the loop. There are four properties that a good loop invariant should fulfill:

1. [INIT] It should be provable in the first iteration of the loop.
2. [INSIDE] It should allow proving absence of run-time errors and local assertions inside the loop.
3. [AFTER] It should allow proving absence of run-time errors, local assertions and the subprogram postcondition after the loop.
4. [PRESERVE] It should be provable after the first iteration of the loop.

As a first example, here is a variant of the search algorithm described in SPARK Tutorial, which returns whether a collection contains a desired value, and if so, at which index. The collection is implemented as an array.

The specification of Linear_Search is given in file linear_search.ads. The postcondition of Search expresses that, either the search returns a result within the array bounds, in which case it is the desired index, otherwise the array does not contain the value searched.
package Linear_Search
  with SPARK_Mode
is
  type Opt_Index is new Natural;

  subtype Index is Opt_Index range 1 .. Opt_Index'Last - 1;

  No_Index : constant Opt_Index := 0;

  type Ar is array (Index range <>) of Integer;

  function Search (A : Ar; I : Integer) return Opt_Index with
    Post => (if Search'Result in A'Range then A (Search'Result) = I
      else (for all K in A'Range => A (K) /= I));

end Linear_Search;

The implementation of Linear_Search is given in file linear_search.adb. The loop invariant of Search expresses that, at the end of each iteration, if the loop has not been exited before, then the value searched is not in the range of indexes between the start of the array A'First and the current index Pos.

package body Linear_Search
  with SPARK_Mode
is

  function Search (A : Ar; I : Integer) return Opt_Index is
  begin
    for Pos in A'Range loop
      if A (Pos) = I then
        return Pos;
      end if;
    end loop;

    pragma Loop_Invariant (for all K in A'First .. Pos => A (K) /= I);
  end loop;

  return No_Index;

end Search;

end Linear_Search;

With this loop invariant, GNATprove is able to prove all checks in Linear_Search, both those related to absence of run-time errors and those related to verification of contracts:

linear_search.adb:9:20: info: range check proved
linear_search.adb:12:33: info: loop invariant initialization proved
linear_search.adb:12:33: info: loop invariant preservation proved
linear_search.adb:12:67: info: index check proved
linear_search.ads:13:14: info: postcondition proved
linear_search.ads:13:57: info: index check proved
linear_search.ads:14:48: info: index check proved

In particular, the loop invariant fulfills all four properties that we listed above:

1. [INIT] It is proved in the first iteration (message on line 2).
2. [INSIDE] It allows proving absence of run-time errors inside the loop (messages on lines 1 and 4).
3. [AFTER] It allows proving absence of run-time errors after the loop (messages on lines 6 and 7) and the subprogram postcondition (message on line 5).
4. [PRESERVE] It is proved after the first iteration (message on line 3).

Note that the loop invariant closely resembles the second line in the postcondition of the subprogram, except with a different range of values in the quantification: instead of stating a property for all indexes in the array A, the loop invariant states the same property for all indexes up to the current loop index Pos. In fact, if we equate Pos to A'Last for the last iteration of the loop, the two properties are equal. This explains here how the loop invariant allows proving the subprogram postcondition when the value searched is not found.

Note also that we chose to put the loop invariant at the end of the loop. We could as easily put it at the start of the loop. In that case, the range of values in the quantification should be modified to state that, at the start of each iteration, if the loop has not been exited before, then the value searched is not in the range of indexes between the start of the array A'First and the current index Pos excluded:

```plaintext
pragma Loop_Invariant (for all K in A'First .. Pos - 1 => A (K) /= I);
```

Indeed, the test for the value at index Pos is done after the loop invariant in that case.

We will now demonstrate techniques to complete a loop invariant so that it fulfills all four properties [INIT], [INSIDE], [AFTER] and [PRESERVE], on a more complex algorithm searching in an ordered collection of elements. Like the naive search algorithm just described, this algorithm returns whether the collection contains the desired value, and if so, at which index. The collection is also implemented as an array.

The specification of this Binary_Search is given in file binary_search.ads:

```plaintext
package Binary_Search
  with SPARK_Mode
is
  type Opt_Index is new Natural;
  subtype Index is Opt_Index range 1 .. Opt_Index'Last - 1;
  No_Index : constant Opt_Index := 0;
  type Ar is array (Index range <>) of Integer;

  function Empty (A : Ar) return Boolean is (A'First > A'Last);
  function Sorted (A : Ar) return Boolean is
    (for all I1 in A'Range =>
     (for all I2 in I1 .. A'Last => A (I1) <= A (I2)));
  function Search (A : Ar; I : Integer) return Opt_Index with
    Pre => Sorted (A),
    Post => (if Search'Result in A'Range then A (Search'Result) = I
              else (for all Index in A'Range => A (Index) /= I));
end Binary_Search;
```

The implementation of Binary_Search is given in file binary_search.adb:

```plaintext
package body Binary_Search
  with SPARK_Mode
is
  type Opt_Index is new Natural;
  subtype Index is Opt_Index range 1 .. Opt_Index'Last - 1;
  No_Index : constant Opt_Index := 0;
  type Ar is array (Index range <>) of Integer;

  function Empty (A : Ar) return Boolean is (A'First > A'Last);
  function Sorted (A : Ar) return Boolean is
    (for all I1 in A'Range =>
     (for all I2 in I1 .. A'Last => A (I1) <= A (I2)));
  function Search (A : Ar; I : Integer) return Opt_Index with
    Pre => Sorted (A),
    Post => (if Search'Result in A'Range then A (Search'Result) = I
              else (for all Index in A'Range => A (Index) /= I)));
end Binary_Search;
```
if Empty (A) then
  return No_Index;
end if;

Left := A'First;
Right := A'Last;

if Left = Right and A (Left) = I then
  return Left;
elsif A (Left) > I or A (Right) < I then
  return No_Index;
end if;

while Left <= Right loop
  Med := Left + (Right - Left) / 2;
  if A (Med) < I then
    Left := Med + 1;
  elsif A (Med) > I then
    Right := Med - 1;
  else
    return Med;
  end if;
end loop;

return No_Index;
end Search;
end Binary_Search;

Note that, although function Search has a loop, we have not given an explicit loop invariant yet, so the default loop invariant of True will be used by GNATprove. We are running GNATprove with a prover timeout of 60 seconds (switch --timeout=60) to get the results presented in the rest of this section.

7.7.4 Proving a Loop Invariant in the First Iteration

Property [INIT] is the easiest one to prove. This is equivalent to proving a pragma Assert in the sequence of statements obtained by unrolling the loop once. In particular, if the loop invariant is at the start of the loop, this is equivalent to proving a pragma Assert just before the loop. Therefore, the usual techniques for investigating unproved checks apply, see How to Investigate Unproved Checks.

7.7.5 Completing a Loop Invariant to Prove Checks Inside the Loop

Let's start by running GNATprove on program Binary_Search without loop invariant. It generates two medium messages, one corresponding to a possible run-time check failure, and one corresponding to a possible failure of the postcondition:

binary_search.adb:26:16: medium: array index check might fail [possible explanation: loop at line 23 should mention Med in a loop invariant]
binary_search.ads:21:49: medium: postcondition might fail, cannot prove A (Index) /= I

We will focus here on the message inside the loop, which corresponds to property [INSIDE]. The problem is that variable Med varies in the loop, so GNATprove only knows that its value is in the range of its type Index at the start of an iteration (line 23), and that it is then assigned the value of Left + (Right - Left) / 2 (line 24) before
being used as an index into array \texttt{A} (lines 26 and 28) and inside expressions assigned to \texttt{Left} and \texttt{Right} (lines 27 and 29).

As \texttt{Left} and \texttt{Right} also vary in the loop, GNATprove cannot use the assignment on line 24 to compute a more precise range for variable \texttt{Med}, hence the message on index check.

What is needed here is a loop invariant that states that the values of \texttt{Left} and \texttt{Right} stay within the bounds of \texttt{A} inside the loop:

```
while Left <= Right loop
  pragma Loop_Invariant (Left in A'Range and Right in A'Range);
  Med := Left + (Right - Left) / 2;
end loop;
```

With this simple loop invariant, GNATprove now reports that the check on line 26 is proved. GNATprove computes that the value assigned to \texttt{Med} in the loop is also within the bounds of \texttt{A}.

### 7.7.6 Completing a Loop Invariant to Prove Checks After the Loop

With the simple loop invariant given before, GNATprove still reports that the postcondition of \texttt{Search} may fail, which corresponds to property \texttt{[AFTER]}. By instructing GNATprove to prove checks progressively, as seen in \textit{Proving SPARK Programs}, we even get a precise message pointing to the part of the postcondition that could not be proved:

```
binary_search.ads:21:49: medium: postcondition might fail, cannot prove A (Index) /= I (e.g. when A = (1 => 0, 3 => 0, 4 => 0, others => -1) and A'First = 2 and A'Last = 4 and I = 0 and Index = 3)
```

Here, the message shows that the second line of the postcondition could not be proved. This line expresses that, in the case where \texttt{Search} returns \texttt{No_Index} after the loop, the array \texttt{A} should not contain the value searched \texttt{I}.

One can very easily check that, if GNATprove can prove this property, it can also prove the postcondition. Simply insert a pragma \texttt{Assert} after the loop stating this property:

```
end loop;
pragma Assert (for all Index in A'Range => A (Index) /= I);
return No_Index;
```

GNATprove now succeeds in proving the postcondition, but it fails to prove the assertion:

```
binary_search.adb:36:50: medium: assertion might fail, cannot prove A (Index) /= I (e.g. when A = (1 => -1, others => 0) and A'First = 1 and A'Last = 2 and I = 0 and Index = 2) [possible explanation: precondition of subprogram at binary_search.ads:18 should mention I]
```

The problem is that GNATprove only knows what the user specified about \texttt{A} in the precondition, namely that it is sorted in ascending order. Nowhere it is said that \texttt{A} does not contain the value \texttt{I}. Note that adding this assertion is not compulsory. It simply helps identifying what is needed to achieve property \texttt{[AFTER]}, but it can be removed afterwards.

What is needed here is a loop invariant stating that, if \texttt{A} contains the value \texttt{I}, it must be at an index in the range \texttt{Left..Right}, so when the loop exits because \texttt{Left > Right} (so the loop test becomes false), \texttt{A} cannot contain the value \texttt{I}.

One way to express this property is to state that the value of \texttt{A} at index \texttt{Left - 1} is less than \texttt{I}, while the value of \texttt{A} at index \texttt{Right + 1} is greater than \texttt{I}. Taking into account the possibility that there are no such indexes in \texttt{A} if either \texttt{Left} or \texttt{Right} are at the boundaries of the array, we can express it as follows:
while Left <= Right loop
pragma Loop.Invariant (Left in A'Range and Right in A'Range);
pragma Loop.Invariant (Left = A.First or else A (Left - 1) < I);
pragma Loop.Invariant (Right = A.Last or else I < A (Right + 1));
Med := Left + (Right - Left) / 2;

GNATprove manages to prove these additional loop invariants, but it still cannot prove the assertion after the loop. The reason is both simple and far-reaching. Although the above loop invariant together with the property that the array is sorted imply the property we want to express, it still requires additional work for the prover to reach the same conclusion, which may prevent automatic proof in the allocated time. In that case, it is better to express the equivalent but more explicit property directly, as follows:

while Left <= Right loop
pragma Loop.Invariant (Left in A'Range and Right in A'Range);
pragma Loop.Invariant (for all Index in A.First .. Left - 1 => A (Index) < I);
pragma Loop.Invariant (for all Index in A.Range =>
(if Index > Right then I < A (Index)));
Med := Left + (Right - Left) / 2;

GNATprove now proves the assertion after the loop. In general, it is simpler to understand the relationship between the loop invariant and the checks that follow the loop when the loop invariant is directly followed by the exit statement that controls loop termination. In a “for” or “while” loop, this can mean it is easier to place the Loop.Invariant pragmas at the end of the loop body, where they precede the (implicit) exit statement. In such cases, the loop invariant is more likely to resemble the postcondition.

7.7.7 Proving a Loop Invariant After the First Iteration

With the loop invariant given before, GNATprove also proves that the loop invariant of Search holds after the first iteration, which corresponds to property [PRESERVE]. In fact, we have now arrived at a loop invariant which allows GNATprove to prove all checks for subprogram Search.

This is not always the case. In general, when the loop invariant is not proved after the first iteration, the problem is that the loop invariant is not precise enough. The only information that GNATprove knows about the value of variables that are modified in the loop, at each loop iteration, is the information provided in the loop invariant. If the loop invariant is missing some crucial information about these variables, which is needed to prove the loop invariant after N iterations, GNATprove won’t be able to prove that the loop invariant holds at each iteration.

In loops that modify variables of composite types (records and arrays), it is usually necessary at this stage to add in the loop invariant some information about those parts of the modified variables which are not modified by the loop, or which are not modified in the first N iterations of the loop. Otherwise, GNATprove assumes that these parts may also be modified, which can prevent it from proving the preservation of the loop invariant. See Loop Invariants for an example where this is needed.

In other cases, it may be necessary to guide the prover with intermediate assertions. A rule of thumb for deciding which properties to assert, and where to assert them, is to try to locate at which program point the prover does not succeed in proving the property of interest, and to restate other properties that are useful for the proof.

In yet other cases, where the difficulty is related to the size of the loop rather than the complexity of the properties, it may be useful to factor the loop into local subprograms so that the subprograms’ preconditions and postconditions provide the intermediate assertions that are needed to prove the loop invariant.
7.8 How to Investigate Unproved Checks

One of the most challenging aspects of formal verification is the analysis of failed proofs. If GNATprove fails to prove automatically that a run-time check or an assertion holds, there might be various reasons:

- [CODE] The check or assertion does not hold, because the code is wrong.
- [ASSERT] The assertion does not hold, because it is incorrect.
- [SPEC] The check or assertion cannot be proved, because of some missing assertions about the behavior of the program.
- [MODEL] The check or assertion is not proved because of current limitations in the model used by GNATprove.
- [TIMEOUT] The check or assertion is not proved because the prover timeouts.
- [PROVER] The check or assertion is not proved because the prover is not smart enough.

7.8.1 Investigating Incorrect Code or Assertion

The first step is to check whether the code is incorrect [CODE] or the assertion is incorrect [ASSERT], or both. Since run-time checks and assertions can be executed at run time, one way to increase confidence in the correction of the code and assertions is to test the program on representative inputs. The following GNAT switches can be used:

- \(-\text{gnato}\): enable run-time checking of intermediate overflows
- \(-\text{gnat-p}\): reenable run-time checking even if \(-\text{gnatp}\) was used to suppress all checks
- \(-\text{gnata}\): enable run-time checking of assertions

7.8.2 Investigating Unprovable Properties

The second step is to consider whether the property is provable [SPEC]. A check or assertion might be unprovable because a necessary annotation is missing:

- the precondition of the enclosing subprogram might be too weak; or
- the postcondition of a subprogram called might be too weak; or
- a loop invariant for an enclosing loop might be too weak; or
- a loop invariant for a loop before the check or assertion might be too weak.

In particular, GNATprove does not look into subprogram bodies, so all the necessary information for calls should be explicit in the subprogram contracts. GNATprove may emit a tentative explanation for the unprovable property when it suspects a missing precondition, postcondition or loop invariant to be the cause of the unprovability. The explanation part follows the usual message of the form:

```
file:line:col: severity: check might fail
```

with a part in square brackets such as:

```
[possible explanation: subprogram at line xxx should mention Var in a precondition]
[possible explanation: loop at line xxx should mention Var in a loop invariant]
[possible explanation: call at line xxx should mention Var in a postcondition]
```

A focused manual review of the code and assertions can efficiently diagnose many cases of missing annotations. Even when an assertion is quite large, GNATprove precisely locates the part that it cannot prove, which can help figuring out
the problem. It may useful to simplify the code during this investigation, for example by adding a simpler assertion and trying to prove it.

GNATprove provides path information that might help the code review. You can display inside the editor the path on which the proof failed, as described in Running GNATprove from GNAT Studio. In some cases, a counterexample is also generated on the path, with values of variables which exhibit the problem (see Understanding Counterexamples). In many cases, this is sufficient to spot a missing assertion.

A property can also be conceptually provable, but the model used by GNATprove can currently not reason about it [MODEL]. (See GNATprove Limitations for a list of the current limitations in GNATprove.) In particular using the following features of the language may yield checks that should be true, but cannot be proved:

- Floating point arithmetic (although using CodePeer integration may help here)
- The specific value of dispatching calls when the tag is known

To use CodePeer integration, pass the switch --codepeer=on to GNATprove. In those cases where no prover, including CodePeer, can prove the check, the missing information can usually be added using pragma Assume.

It may be difficult sometimes to distinguish between unprovable properties and prover shortcomings (the next section). The most generally useful action to narrow down the issue to its core is to insert assertions in the code that test whether the property (or part of it) can be proved at some specific point in the program. For example, if a postcondition states a property (P or Q), and the implementation contains many branches and paths, try adding assertions that P holds or Q holds where they are expected to hold. This can help distinguish between the two cases:

- In the case of an unprovable property, this may point to a specific path in the program, and a specific part of the property, which cause the issue.
- In the case of a prover shortcoming, this may also help provers to manage to prove both the assertion and the property. Then, it is good practice to keep in the code only those assertions that help getting automatic proof, and to remove other assertions that were inserted during interaction.

When using switch --info, GNATprove issues information messages regarding internal decisions that could influence provability:

- whether candidate loops for Automatic Unrolling of Simple For-Loops are effectively unrolled or not;
- whether candidate subprograms for Contextual Analysis of Subprograms Without Contracts are effectively inlined for proof or not;
- whether possible subprogram nontermination impacts the proof of calls to that subprogram (see the note in the section on Subprogram Termination)

### 7.8.3 Investigating Prover Shortcomings

The last step is to investigate if the prover would find a proof given enough time [TIMEOUT] or if another prover can find a proof [PROVER]. To that end, GNATprove provides switch --level, usable either from the command-line (see Running GNATprove from the Command Line), inside GNAT Studio (see Running GNATprove from GNAT Studio) or inside GNATbench (see Running GNATprove from GNATbench). The level of 0 is only adequate for simple proofs. In general, one should increase the level of proof (up to level 4) until no more automatic proofs can be obtained.

As described in the section about Running GNATprove from the Command Line, switch --level is equivalent to setting directly various lower level switches like --timeout, --prover, and --proof. Hence, one can also set more powerful (and thus leading to longer proof time) values for the individual switches rather than using the predefined combinations set through --level.

Note that for the above experiments, it is quite convenient to use the SPARK → Prove Line or SPARK → Prove Subprogram menus in GNAT Studio, as described in Running GNATprove from GNAT Studio and Running GNATprove from GNATbench, to get faster results for the desired line or subprogram.
A current limitation of automatic provers is that they don’t handle floating-point arithmetic very precisely, in particular when there are either a lot of operations, or some non-linear operations (multiplication, division, exponentiation). In that case, it may be profitable to use CodePeer integration, which is activated with the switch --codepeer=on, as CodePeer is both fast and precise for proving bounds of floating-point operations.

Another common limitation of automatic provers is that they don’t handle non-linear arithmetic well. For example, they might fail to prove simple checks involving multiplication, division, modulo or exponentiation.

In that case, a user may either:

- add in the code a call to a lemma from the SPARK lemma library (see details in Manual Proof Using SPARK Lemma Library), or
- add in the code a call to a user lemma (see details in Manual Proof Using User Lemmas), or
- add an assumption in the code (see details in Indirect Justification with Pragma Assume), or
- add a justification in the code (see details in Direct Justification with Pragma Annotate), or
- manually review the unproved checks and record that they can be trusted (for example by storing the result of GNATprove under version control).

In the future, GNATprove may provide a user view of the formula passed to the prover, for advanced users to inspect. This view would express in an Ada-like syntax the actual formula whose proof failed, to make it easier for users to interpret it. This format is yet to be defined.

For advanced users, in particular those who would like to do manual proof, we will provide a description of the format of the proof files generated by GNATprove, so that users can understand the actual files passed to the prover. Each individual file is stored under the sub-directory gnatprove of the project object directory (default is the project directory). The file name follows the convention:

<file>_<line>_<column>_<check>_<num>.<ext>

where:

- file is the name of the Ada source file for the check
- line is the line where the check appears
- column is the column
- check is an identifier for the check
- num is an optional number and identifies different paths through the program, between the start of the subprogram and the location of the check
- ext is the extension corresponding to the file format chosen. The format of the file depends on the prover used.

For example, files for Alt-Ergo are are in Why3 format, and files for CVC4 are in SMTLIB2 format.

For example, the proof files generated for prover Alt-Ergo for a range check at line 160, column 42, of the file f.adb are stored in:

f.adb_160_42_range_check.why
f.adb_160_42_range_check_2.why
f.adb_160_42_range_check_3.why
...

Corresponding proof files generated for prover CVC4 are stored in:

f.adb_160_42_range_check.smt2
f.adb_160_42_range_check_2.smt2
f.adb_160_42_range_check_3.smt2
...
To be able to inspect these files, you should instruct GNATprove to keep them around by adding the switch \(-d\) to GNATprove’s command line. You can also use the switch \(-v\) to get a detailed log of which proof files GNATprove is producing and attempting to prove.

### 7.8.4 Looking at Machine-Parsable GNATprove Output

GNATprove generates files which contain the results of SPARK analysis in machine-parsable form. These files are located in the `gnatprove` subdirectory of the project object directory, and have the suffix `.spark`. The structure of these files exposes internal details such as the exact way some checks are proved, therefore the structure of these files may change. Still, we provide here the structure of these files for convenience.

At various places in these files, we refer to entities. These are Ada entities, either subprograms or packages. Entities are defined by their name and their source location (file and line). In JSON this translates to the following dictionary for entities:

```json
{ "name" : string,
  "file" : string,
  "line" : int }
```

A `.spark` file is of this form:

```json
{ "spark" : list spark_result,
  "flow" : list flow_result,
  "proof" : list proof_result }
```

Each entry is mapped to a list of entries whose format is described below.

The `spark_result` entry is simply an entity, with an extra field for spark status, so that the entire dictionary looks like this:

```json
spark_result = { "name" : string,
                 "file" : string,
                 "line" : int,
                 "spark" : string }
```

Field “spark” takes value in “spec”, “all” or “no” to denote respectively that only the spec is in SPARK, both spec/body are in SPARK (or spec is in SPARK for a package without body), or the spec is not in SPARK.

Entries for proof are of the following form:

```json
proof_result =
  { "file" : string,
    "line" : int,
    "col" : int,
    "suppressed" : string,
    "rule" : string,
    "severity" : string,
    "tracefile" : string,
    "check_tree" : list goal,
    "msg_id" : int,
    "how_proved" : string,
    "entity" : entity }
```

- (“file”, “line”, “col”) describe the source location of the message.
- “rule” describes the kind of check.
• “severity” describes the kind status of the message, possible values used by gnatwhy3 are “info”, “low”, “medium”, “high” and “error”.

• “tracefile” contains the name of a trace file, if any.

• “entity” contains the entity dictionary for the entity that this check belongs to.

• “msg_id” - if present indicates that this entry corresponds to a message issued on the commandline, with the exact same msg_id in brackets: “[#12]”

• “suppressed” - if present, the message is in fact suppressed by a pragma Annotate, and this field contains the justification message.

• “how_proved” - if present, indicates how the check has been proved (i.e. which prover). Special values are “interval” and “codepeer”, which designate the special interval analysis, done in the frontend, and the CodePeer analysis, respectively. Both have their own column in the summary table.

• “check_tree” basically contains a copy of the session tree in JSON format. It’s a tree structure whose nodes are goals, transformations and proof attempts:

```
goal = { "transformations" : list trans,  
        "pa" : proof_attempt }
trans = { [transname : goal] }
proof_attempt = { [prover : infos] }
infos = { "time" : float,  
          "steps" : integer,  
          "result" : string }
```

Flow entries are of the same form as for proof. Differences are in the possible values for “rule”, which can only be the ones for flow messages. Also “how_proved” field is never set.

### 7.8.5 Understanding Proof Strategies

We now explain in more detail how the provers are run on the logical formula(s) generated for a given check, a.k.a. Verification Conditions or VCs.

• In per_check mode, a single VC is generated for each check at the source level (e.g. an assertion, run-time check, or postcondition); in some cases two VCs can appear. Before attempting proof, this VC is then split into the conjuncts, that is, the parts that are combined with and or and then. All provers are tried on the VCs obtained in this way until one of them proves the VC or no more provers are left.

• In per_path mode, a VC is generated not only for each check at the source level, but for each path to the check. For example, for an assertion that appears after an if-statement, at least two VCs will be generated - one for each path through the if-statement. For each such VC, all provers are attempted. Unproved VCs are then further split into their conjuncts, and proof is again attempted.

• In progressive mode, first the actions described for per_check are tried. For all unproved VCs, the VC is then split into the paths that lead to the check, like for per_path. Each part is then attempted to be proved independently.

### 7.9 GNATprove by Example

GNATprove is based on advanced technology for modular static analysis and deductive verification. It is very different both from compilers, which do very little analysis of the code, and static analyzers, which execute symbolically the
program. GNATprove does a very powerful local analysis of the program, but it generally does not cross subprogram boundaries. Instead, it uses the Subprogram Contracts provided by users to analyze calls. GNATprove also requires sometimes that users direct the analysis with Assertion Pragmas. Thus, it is essential to understand how GNATprove uses contracts and assertion pragmas. This section aims at providing a deeper insight into how GNATprove's flow analysis and proof work, through a step-by-step exploration of small code examples.

All the examples presented in this section, as well as some code snippets presented in the Overview of SPARK Language, are available in the example called gnatprove_by_example distributed with the SPARK toolset. It can be found in the share/examples/spark directory below the directory where the toolset is installed, and can be accessed from the IDE (either GNAT Studio or GNATBench) via the Help → SPARK → Examples menu item.

7.9.1 Basic Examples

The examples in this section have no loops, and do not use more complex features of SPARK like Ghost Code, Interfaces to the Physical World, or Object Oriented Programming and Liskov Substitution Principle.

Increment

Consider a simple procedure that increments its integer parameter X:

```plaintext
procedure Increment (X : in out Integer) with
  SPARK_Mode
is
  begin
  X := X + 1;
end Increment;
```

As this procedure does not have a contract yet, GNATprove only checks that there are no possible reads of uninitialized data and no possible run-time errors in the procedure. Here, it issues a message about a possible overflow check failure on X + 1:

```
increment.adb:5:11: medium: overflow check might fail (e.g. when X = Integer'Last)
  ➥ [possible explanation: subprogram at line 1 should mention X in a precondition]
```

The counterexample displayed tells us that Increment could be called on value Integer'Last for parameter X, which would cause the increment to raise a run-time error. As suggested by the possible explanation in the message issued by GNATprove, one way to eliminate this vulnerability is to add a precondition to Increment specifying that X should be less than Integer'Last when calling the procedure:

```plaintext
procedure Increment_Guarded (X : in out Integer) with
  SPARK_Mode,
  Pre => X < Integer'Last
is
  begin
  X := X + 1;
end Increment_Guarded;
```

As this procedure has a contract now, GNATprove checks like before that there are no possible reads of uninitialized data and no possible run-time errors in the procedure, including in its contrat, and that the procedure implements its contract. As expected, GNATprove now proves that there is no possible overflow check failure on X + 1:

```
increment_guarded.adb:6:11: info: overflow check proved
```

The precondition is usually the first contract added to a subprogram, but there are other Subprogram Contracts. Here is a version of Increment with:
• global dependencies (aspect Global) stating that the procedure reads and writes no global variables
• flow dependencies (aspect Depends) stating that the final value of parameter X only depends on its input value
• a precondition (aspect Pre) stating that parameter X should be less than \texttt{Integer'Last} on entry
• a postcondition (aspect Post) stating that parameter X should have been incremented by the procedure on exit

```
procedure Increment_Full (X : in out Integer) with
  SPARK_Mode,
  Global => null,
  Depends => (X => X),
  Pre => X < Integer'Last,
  Post => X = X'Old + 1
is
begin
  X := X + 1;
end Increment_Full;
```

GNATprove checks that \texttt{Increment_Full} implements its contract, and that it cannot raise run-time errors or read uninitialized data. By default, GNATprove’s output is empty in such a case, but we can request that it prints one line per check proved by using switch \texttt{--report=all}, which we do here:

```
increment_full.adb:3:03: info: data dependencies proved
increment_full.adb:4:03: info: flow dependencies proved
increment_full.adb:6:14: info: postcondition proved
increment_full.adb:9:11: info: overflow check proved
```

As subprogram contracts are used to analyze callers of a subprogram, let’s consider a procedure \texttt{Increment_Calls} that calls the different versions of \texttt{Increment} presented so far:

```
with Increment;
with Increment_Guarded;
with Increment_Full;

procedure Increment_Calls with
  SPARK_Mode
is
  X : Integer;
begin
  X := 0;
  Increment (X);
  Increment (X);
  X := 0;
  Increment_Guarded (X);
  Increment_Guarded (X);
  X := 0;
  Increment_Full (X);
  Increment_Full (X);
end Increment_Calls;
```

GNATprove proves all preconditions expect the one on the second call to \texttt{Increment_Guarded}:

```
increment_calls.adb:8:04: info: initialization of "X" proved
increment_calls.adb:15:04: info: precondition proved
increment_calls.adb:16:04: medium: precondition might fail, cannot prove X < Integer'Last (e.g. when X = Integer'Last) [possible explanation: call at line 15 should mention X (for argument X) in a postcondition]
```
Increment has no precondition, so there is nothing to check here except the initialization of X when calling Increment on lines 11 and 12. But remember that GNATprove did issue a message about a true vulnerability on Increment's implementation.

This vulnerability was corrected by adding a precondition to Increment_Guarded. This has the effect of pushing the constraint on callers, here procedure Increment_Calls. As expected, GNATprove proves that the first call to Increment_Guarded on line 15 satisfies its precondition. But it does not prove the same for the second call to Increment_Guarded on line 16, because the value of X on line 16 was set by the call to Increment_Guarded on line 15, and the contract of Increment_Guarded does not say anything about the possible values of X on exit.

As suggested by the possible explanation in the message issued by GNATprove, a postcondition like the one on Increment_Full is needed so that GNATprove can check the second call to increment X. As expected, GNATprove proves that both calls to Increment_Full on lines 19 and 20 satisfy their precondition.

In some cases, the user is not interested in specifying and verifying a complete contract like the one on Increment_Full, typically for helper subprograms defined locally in a subprogram or package body. GNATprove allows performing Contextual Analysis of Subprograms Without Contracts for these local subprograms. For example, consider a local definition of Increment inside procedure Increment_Local:

```ada
procedure Increment_Local with
  SPARK_Mode
is
  procedure Increment (X : in out Integer) is
  begin
    X := X + 1;
  end Increment;
  X : Integer;
begin
  X := 0;
  Increment (X);
  Increment (X);
pragma Assert (X = 2);
end Increment_Local;
```

Although Increment has no contract (like the previous non-local version), GNATprove proves that this program is free from run-time errors, and that the assertion on line 15 holds:

Swap

Consider a simple procedure that swaps its integer parameters X and Y, whose simple-minded implementation is wrong:

```ada
procedure Swap_Bad (X, Y : in out Integer) with
  SPARK_Mode
```

```ada```
As this procedure does not have a contract yet, GNATprove only checks that there are no possible reads of uninitialized data and no possible run-time errors in the procedure. Here, it simply issues a warning:

```
Warning: unused initial value of "X"
```

But we know the procedure is wrong, so we'd like to get an error of some sort! We could not detect it with GNATprove because the error is functional, and GNATprove cannot guess the intended functionality of `Swap_Bad`. Fortunately, we can give this information to GNATprove by adding a contract to `Swap_Bad`.

One such contract is the flow dependencies introduced by aspect `Depends`. Here it specifies that the final value of `X` (resp. `Y`) should depend on the initial value of `Y` (resp. `X`):

```
procedure Swap_Bad_Depends (X, Y : in out Integer) with
  SPARK_Mode,
  Depends => (X => Y, Y => X)
is
begin
  X := Y;
  Y := X;
end Swap_Bad_Depends;
```

GNATprove issues 3 check messages on `Swap_Bad_Depends`:

```
Warning: unused initial value of "X"
Warning: missing dependency "null => X"
Warning: incorrect dependency "Y => X"
```

The last message informs us that the dependency `Y => X` stated in `Swap_Bad_Depends`'s contract is incorrect for the given implementation. That might be either an error in the code or an error in the contract. Here this is an error in the code. The two other messages are consequences of this error.

Another possible contract is the postcondition introduced by aspect `Post`. Here it specifies that the final value of `X` (resp. `Y`) is equal to the initial value of `Y` (resp. `X`):

```
procedure Swap_Bad_Post (X, Y : in out Integer) with
  SPARK_Mode,
  Post => X = Y'Old and Y = X'Old
is
begin
  X := Y;
  Y := X;
end Swap_Bad_Post;
```

GNATprove issues one check message on the unproved postcondition of `Swap_Bad_Post`, with a counterexample giving concrete values of a wrong execution:

```
Warning: postcondition might fail, cannot prove Y = X'old (e.g. when X'Old = 0 and Y = 1)
```

Both the check messages on `Swap_Bad_Depends` and on `Swap_Bad_Post` inform us that the intended functionality as expressed in the contracts is not implemented in the procedure. And looking again at the warning issued...
by GNATprove on Swap_Bad, this was already pointing at the same issue: swapping the values of \( X \) and \( Y \) should obviously lead to reading the initial value of \( X \); the fact that this value is not used is a clear sign that there is an error in the implementation. The correct version of Swap uses a temporary value to hold the value of \( X \):

```plaintext
procedure Swap (X, Y : in out Integer) with
  SPARK_Mode,
  Depends => (X => Y, Y => X),
  Post => X = Y'Old and Y = X'Old
is
  Tmp : constant Integer := X;
begin
  X := Y;
  Y := Tmp;
end Swap;
```

GNATprove proves both contracts on Swap and it informs us that the postcondition was proved:

```plaintext
swap.adb:3:03: info: flow dependencies proved
swap.adb:4:14: info: postcondition proved
```

Let’s now consider a well-known in place implementation of Swap that avoids introducing a temporary variable by using bitwise operations:

```plaintext
with Interfaces; use Interfaces;
procedure Swap_Modulo (X, Y : in out Unsigned_32) with
  SPARK_Mode,
  Post => X = Y'Old and Y = X'Old
is
begin
  X := X xor Y;
  Y := X xor Y;
  X := X xor Y;
end Swap_Modulo;
```

GNATprove understands the bitwise operations on values of modular types, and it proves here that the postcondition of Swap_Modulo is proved:

```plaintext
swap_modulo.adb:5:11: info: postcondition proved
```

GNATprove’s flow analysis issues warnings like the one on Swap_Bad whenever it detects that some variables or statements are not used in the computation, which is likely uncovering an error. For example, consider procedure Swap_Warn which assigns \( X \) and Tmp_Y out of order:

```plaintext
procedure Swap_Warn (X, Y : in out Integer) with
  SPARK_Mode
is
  Tmp_X : Integer;
  Tmp_Y : Integer;
begin
  Tmp_X := X;
  X := Tmp_Y;
  Tmp_Y := Y;
  Y := Tmp_X;
end Swap_Warn;
```

On this wrong implementation, GNATprove issues a high check message for the certain read of an uninitialized variable, and two warnings that point to unused constructs:
In general, warnings issued by GNATprove’s flow analysis should be carefully reviewed, as they may lead to the discovery of errors in the program.

**Addition**

Consider a simple function `Addition` that returns the sum of its integer parameters `X` and `Y`. As in `Increment`, we add a suitable precondition and postcondition for this function:

```ada
function Addition (X, Y : Integer) return Integer with
  SPARK_Mode,
  Depends => (Addition'Result => (X, Y)),
  Pre => X + Y in Integer,
  Post => Addition'Result = X + Y
is
begin
  return X + Y;
end Addition;
```

We also added flow dependencies to `Addition` for illustration purposes, but they are the same as the default generated ones (the result of the function depends on all its inputs), so are not in general given explicitly.

GNATprove issues a check message about a possible overflow in the precondition of `Addition`:

```ada
addition.adb:3:03: info: flow dependencies proved
addition.adb:4:16: medium: overflow check might fail (e.g. when X = -1 and Y = Integer'First)
addition.adb:5:14: info: postcondition proved
addition.adb:5:34: info: overflow check proved
addition.adb:8:13: info: overflow check proved
```

Indeed, if we call for example `Addition` on values `Integer'Last` for `X` and `1` for `Y`, the expression `X + Y` evaluated in the precondition does not fit in a machine integer and raises an exception at run time. In this specific case, some people may consider that it does not really matter that an exception is raised due to overflow as the failure of the precondition should also raise a run-time exception. But in general the precondition should not fail (just consider the precondition `X + Y not in Integer` for example), and even here, the different exceptions raised may be treated differently (`Constraint_Error` in the case of an overflow, `Assertion_Error` in the case of a failing precondition).

One way to avoid this vulnerability is to rewrite the precondition so that no overflow can occur:

```ada
function Addition_Rewrite (X, Y : Integer) return Integer with
  SPARK_Mode,
  Depends => (Addition_Rewrite'Result => (X, Y)),
  Pre => (X >= 0 and then Y <= Integer'Last - X) or else (X < 0 and then Y >= -Integer'First - X),
  Post => Addition_Rewrite'Result = X + Y
is
begin
  return X + Y;
end Addition_Rewrite;
```
Although GNATprove proves that Addition_Rewrite implements its contract and is free from run-time errors, the rewritten precondition is not so readable anymore:

```
addition_rewrite.adb:3:03: info: flow dependencies proved
addition_rewrite.adb:4:49: info: overflow check proved
addition_rewrite.adb:4:97: info: overflow check proved
addition_rewrite.adb:5:14: info: postcondition proved
addition_rewrite.adb:5:42: info: overflow check proved
addition_rewrite.adb:8:13: info: overflow check proved
```

A better way to achieve the same goal without losing in readability is to execute and analyze contracts in a special mode where overflows cannot occur, as explained in Overflow Modes. In that case, GNATprove proves that there are no run-time errors in function Addition, and that it implements its contract.

Finally, we can choose to expand the range of applicability of the function, by accepting any values of inputs $X$ and $Y$, and saturating when the addition would overflow the bounds of machine integers. That’s what function Addition_Saturated does, and its saturating behavior is expressed in Contract Cases:

```
function Addition_Saturated (X, Y : Integer) return Integer with
SPARK_Mode,
  Contract_Cases => ((X + Y in Integer) => Addition_Saturated'Result = X + Y,
    X + Y < Integer'First => Addition_Saturated'Result = Integer
    'First,
    X + Y > Integer'Last => Addition_Saturated'Result = Integer
    'Last)
is
begin
  if X < 0 and Y < 0 then -- both negative
    if X < Integer'First - Y then
      return Integer'First;
    else
      return X + Y;
    end if;
  elsif X > 0 and Y > 0 then -- both positive
    if X > Integer'Last - Y then
      return Integer'Last;
    else
      return X + Y;
    end if;
  else -- one positive or null, one negative or null, adding them is safe
    return X + Y;
  end if;
end Addition_Saturated;
```

GNATprove proves that Addition_Saturated implements its contract and is free from run-time errors:

```
addition_saturated.adb:3:03: info: complete contract cases proved
addition_saturated.adb:3:03: info: disjoint contract cases proved
addition_saturated.adb:3:44: info: contract case proved
addition_saturated.adb:4:44: info: contract case proved
addition_saturated.adb:5:44: info: contract case proved
addition_saturated.adb:9:28: info: overflow check proved
addition_saturated.adb:12:19: info: overflow check proved
addition_saturated.adb:16:27: info: overflow check proved
addition_saturated.adb:19:19: info: overflow check proved
addition_saturated.adb:23:16: info: overflow check proved
```
Note that we analyzed this function in ELIMINATED overflow mode, using the switch -gnat0l3, otherwise there would be possible overflows in the guard expressions of the contract cases.

**7.9.2 Loop Examples**

The examples in this section contain loops, and thus require in general that users write suitable *Loop Invariants*. We start by explaining the need for a loop invariant, and we continue with a description of the most common patterns of loops and their loop invariant. We summarize each pattern in a table of the following form:

<table>
<thead>
<tr>
<th>Loop Pattern</th>
<th>Loop Over Data Structure</th>
<th>Proof Objective</th>
<th>Loop Behavior</th>
<th>Loop Invariant</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Establish property P.</td>
<td>Loops over the data structure and establishes P.</td>
<td>Property P is established for the part of the data structure looped over so far.</td>
</tr>
</tbody>
</table>

The examples in this section use the types defined in package *Loop_Types*:

```ada
with Ada.Containers.Formal_Doubly_Linked_Lists;
with Ada.Containers.Formal_Vectors;
package Loop_Types is
with SPARK_Mode;
subtype Index_T is Positive range 1 .. 1000;
subtype Opt_Index_T is Natural range 0 .. 1000;
subtype Component_T is Natural;
type Arr_T is array (Index_T) of Component_T;
package Vectors is new Ada.Containers.Formal_Vectors (Index_T, Component_T);
subtype Vec_T is Vectors.Vector;
package Lists is new Ada.Containers.Formal_Doubly_Linked_Lists (Component_T);
subtype List_T is Lists.List;
end Loop_Types;
```

**The Need for a Loop Invariant**

Consider a simple procedure that increments its integer parameter X a number N of times:

```ada
procedure Increment_Loop (X : in out Integer; N : Natural) with
SPARK_Mode,
Pre => X <= Integer'Last - N,
Post => X = X'Old + N
is
begin
  for I in 1 .. N loop
    X := X + 1;
  end loop;
end Increment_Loop;
```

The precondition of *Increment_Loop* ensures that there is no overflow when incrementing X in the loop, and its postcondition states that X has been incremented N times. This contract is a generalization of the contract given for a single increment in *Increment*. GNATprove does not manage to prove either the absence of overflow or the postcondition of *Increment_Loop*:
As described in *How to Write Loop Invariants*, this is because variable X is modified in the loop, hence GNATprove knows nothing about it unless it is stated in a loop invariant. If we add such a loop invariant, as suggested by the possible explanation in the message issued by GNATprove, that describes precisely the value of X in each iteration of the loop:

```
procedure Increment_Loop_Inv (X : in out Integer; N : Natural) with
  SPARK_Mode,
  Pre => X <= Integer'Last - N,
  Post => X = X'Old + N
is
begin
  for I in 1 .. N loop
    X := X + 1;
    pragma Loop_Invariant (X = X'Loop_Entry + I);
  end loop;
end Increment_Loop_Inv;
```

then GNATprove proves both the absence of overflow and the postcondition of `Increment_Loop_Inv`:

```
increment_loop_inv.adb:3:29: info: overflow check proved
increment_loop_inv.adb:4:11: info: postcondition proved
increment_loop_inv.adb:4:21: info: overflow check proved
increment_loop_inv.adb:8:14: info: overflow check proved
increment_loop_inv.adb:9:30: info: loop invariant initialization proved
increment_loop_inv.adb:9:30: info: loop invariant preservation proved
increment_loop_inv.adb:9:47: info: overflow check proved
```

Fortunately, many loops fall into some broad categories for which the loop invariant is known. In the following sections, we describe these common patterns of loops and their loop invariant, which involve in general iterating over the content of a collection (either an array or a container from the *Formal Containers Library*).

### Initialization Loops

This kind of loops iterates over a collection to initialize every element of the collection to a given value:

<table>
<thead>
<tr>
<th>Loop Pattern</th>
<th>Separate Initialization of Each Element</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proof Objective</td>
<td>Every element of the collection has a specific value.</td>
</tr>
<tr>
<td>Loop Behavior</td>
<td>Loops over the collection and initializes every element of the collection.</td>
</tr>
<tr>
<td>Loop Invariant</td>
<td>Every element initialized so far has its specific value.</td>
</tr>
</tbody>
</table>

In the simplest case, every element is assigned the same value. For example, in procedure `Init_Arr_Zero` below, value zero is assigned to every element of array A:

```
with Loop_Types; use Loop_Types;

procedure Init_Arr_Zero (A : out Arr_T) with
  SPARK_Mode,
  Post => (for all J in A'Range => A(J) = 0)
is
```
pragma Annotate (GNATprove, False_Positive, """"A"" might not be initialized", "Entire array is initialized element-by-element in a loop");

begin
  for J in A'Range loop
    A(J) := 0;
    pragma Loop_Invariant (for all K in A'First .. J => A(K) = 0);
    pragma Annotate (GNATprove, False_Positive, """"A"" might not be initialized", "Part of array up to index J is initialized at this point");
  end loop;
end Init_Arr_Zero;

The loop invariant expresses that all elements up to the current loop index J have the value zero. With this loop invariant, GNATprove is able to prove the postcondition of Init_Arr_Zero, namely that all elements of the array have value zero:

init_arr_zero.adb:5:11: info: postcondition proved
init_arr_zero.adb:12:30: info: loop invariant initialization proved
init_arr_zero.adb:12:30: info: loop invariant preservation proved
init_arr_zero.adb:12:61: info: index check proved

Note: Pragma Annotate is used in Init_Arr_Zero to justify a message issued by flow analysis, about the possible read of uninitialized value A(K) in the loop invariant. Indeed, flow analysis is not currently able to infer that all elements up to the loop index J have been initialized, hence it issues a message that "A" might not be initialized. For more details, see section on Justifying Check Messages.

Consider now a variant of the same initialization loop over a vector:

with Loop_Types; use Loop_Types; use Loop_Types.Vectors;

procedure Init_Vec_Zero (V : in out Vec_T) with
  SPARK_Mode,
  Post => (for all J in First_Index (V) .. Last_Index (V) => Element (V, J) = 0)
is
begin
  for J in First_Index (V) .. Last_Index (V) loop
    Replace_Element (V, J, 0);
    pragma Loop_Invariant (Last_Index (V) = Last_Index (V)'Loop_Entry);
    pragma Loop_Invariant (for all K in First_Index (V) .. J => Element (V, K) = 0);
  end loop;
end Init_Vec_Zero;

Like before, the loop invariant expresses that all elements up to the current loop index J have the value zero. Another loop invariant is needed here to express that the length of the vector does not change in the loop: as variable V is modified in the loop, GNATprove does not know its length stays the same (for example, calling procedure Append or Delete_Last would change this length) unless the user says so in the loop invariant. This is different from arrays whose length cannot change. With this loop invariant, GNATprove is able to prove the postcondition of Init_Vec_Zero, namely that all elements of the vector have value zero:

init_vec_zero.adb:5:11: info: postcondition proved
init_vec_zero.adb:5:62: info: precondition proved
init_vec_zero.adb:5:74: info: range check proved
init_vec_zero.adb:9:07: info: precondition proved
init_vec_zero.adb:9:27: info: range check proved
init_vec_zero.adb:10:30: info: loop invariant initialization proved
init_vec_zero.adb:10:30: info: loop invariant preservation proved
Similarly, consider a variant of the same initialization loop over a list:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
with Ada.Containers; use Ada.Containers; use Loop_Types.Lists/Formal_Model;

procedure Init_List_Zero (L : in out List_T) with
  SPARK_Mode,
  Post => (for all E of L => E = 0)
is
  Cu : Cursor := First (L);
begin
  while Has_Element (L, Cu) loop
    pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
                            Element (Model (L), I) = 0);
    Replace_Element (L, Cu, 0);
    Next (L, Cu);
  end loop;
end Init_List_Zero;
```

Contrary to arrays and vectors, lists are not indexed. Instead, a cursor can be defined to iterate over the list. The loop invariant expresses that all elements up to the current cursor Cu have the value zero. To access the element stored at a given position in a list, we use the function Model which computes the mathematical sequence of the elements stored in the list. The position of a cursor in this sequence is retrieved using the Positions function. Contrary to the case of vectors, no loop invariant is needed to express that the length of the list does not change in the loop, because the postcondition remains provable here even if the length of the list changes. With this loop invariant, GNATprove is able to prove the postcondition of Init_List_Zero, namely that all elements of the list have value zero:

The case of sets and maps is similar to the case of lists.

**Note:** The parameter of Init_Vec_Zero and Init_List_Zero is an in out parameter. This is because some components of the vector/list parameter are preserved by the initialization procedure (in particular the component corresponding to its length). This is different from Init_Arr_Zero which takes an out parameter, as all components of the array are initialized by the procedure (the bounds of an array are not modifiable, hence considered separately from the parameter mode).

Consider now a case where the value assigned to each element is not the same. For example, in procedure Init_Arr_Index below, each element of array A is assigned the value of its index:

```ada
with Loop_Types; use Loop_Types;

procedure Init_Arr_Index (A : out Arr_T) with
The loop invariant expresses that all elements up to the current loop index \( J \) have the value of their index. With this loop invariant, GNATprove is able to prove the postcondition of \( \text{Init}_\text{Arr}_\text{Index} \), namely that all elements of the array have the value of their index:

```
init_arr_index.adb:5:11: info: postcondition proved
init_arr_index.adb:12:30: info: loop invariant initialization proved
init_arr_index.adb:12:30: info: loop invariant preservation proved
init_arr_index.adb:12:61: info: index check proved
```

Similarly, variants of \( \text{Init}_\text{Vec}_\text{Zero} \) and \( \text{Init}_\text{List}_\text{Zero} \) that assign a different value to each element of the collection would be proved by GNATprove.

### Mapping Loops

This kind of loops iterates over a collection to map every element of the collection to a new value:

<table>
<thead>
<tr>
<th>Loop Pattern</th>
<th>Separate Modification of Each Element</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proof Objective</td>
<td>Every element of the collection has an updated value.</td>
</tr>
<tr>
<td>Loop Behavior</td>
<td>Loops over the collection and updates every element of the collection.</td>
</tr>
<tr>
<td>Loop Invariant</td>
<td>Every element updated so far has its specific value.</td>
</tr>
</tbody>
</table>

In the simplest case, every element is assigned a new value based only on its initial value. For example, in procedure \( \text{Map}_\text{Arr}_\text{Incr} \) below, every element of array \( A \) is incremented by one:

```
with Loop_Types; use Loop_Types;

procedure Map_Arr_Incr (A : in out Arr_T) with
  SPARK_Mode,
  Pre => (for all J in A'Range => A(J) /= Component_T'Last),
  Post => (for all J in A'Range => A(J) = A'Old(J) + 1)
is
begin
  for J in A'Range loop
    A(J) := A(J) + 1;
    pragma Loop_Invariant (for all K in A'First .. J => A(K) = A'Loop_Entry(K) + 1);
    -- The following loop invariant is generated automatically by GNATprove:
    --  pragma Loop_Invariant (for all K in J + 1 .. A'Last => A(K) = A'Loop_Entry(K));
  end loop;
end Map_Arr_Incr;
```

The loop invariant expresses that all elements up to the current loop index \( J \) have been incremented (using \text{Attribute Loop_Entry} \). With this loop invariant, GNATprove is able to prove the postcondition of \( \text{Map}_\text{Arr}_\text{Incr} \), namely
that all elements of the array have been incremented:

map_arr_incr.adb:6:11: info: postcondition proved
map_arr_incr.adb:6:52: info: overflow check proved
map_arr_incr.adb:10:20: info: overflow check proved
map_arr_incr.adb:11:30: info: loop invariant initialization proved
map_arr_incr.adb:11:30: info: loop invariant preservation proved
map_arr_incr.adb:11:61: info: index check proved
map_arr_incr.adb:11:79: info: index check proved
map_arr_incr.adb:11:82: info: overflow check proved

Note that the commented loop invariant expressing that other elements have not been modified is not needed, as it is
an example of **Automatically Generated Loop Invariants**.

Consider now a variant of the same initialization loop over a vector:

```plaintext
pragma Unevaluated_Use_Of_Old (Allow);
with Loop_Types; use Loop_Types;
use Loop_Types.Vectors;
use Loop_Types.Vectors.Formal_Model;

procedure Map_Vec_Incr (V : in out Vec_T) with
  SPARK_Mode,
  Pre => (for all I in 1 .. Last_Index (V) =>
    Element (V, I) /= Component_T'Last),
  Post => Last_Index (V) = Last_Index (V)'Old
  and then (for all I in 1 .. Last_Index (V) =>
    Element (V, I) = Element (Model (V)'Old, I) + 1)
is
  begin
    for J in 1 .. Last_Index (V) loop
      pragma Loop_Invariant (Last_Index (V) = Last_Index (V)'Loop_Entry);
      pragma Loop_Invariant
      (for all I in 1 .. J - 1 =>
        Element (V, I) = Element (Model (V)'Loop_Entry, I) + 1);
      pragma Loop_Invariant
      (for all I in J .. Last_Index (V) =>
        Element (V, I) = Element (Model (V)'Loop_Entry, I));
      Replace_Element (V, J, Element (V, J) + 1);
    end loop;
  end Map_Vec_Incr;
```

Like before, we need an additional loop invariant to state that the length of the vector is not modified by the loop. The other two invariants are direct translations of those used for the loop over arrays: the first one expresses that all elements up to the current loop index \( J \) have been incremented, and the second one expresses that other elements have not been modified. Note that, as formal vectors are limited, we need to use the \texttt{Model} function of vectors to express the set of elements contained in the vector before the loop (using attributes \texttt{Loop_Entry} and \texttt{Old}). With this loop invariant, GNATprove is able to prove the postcondition of \texttt{Map_Vec_Incr}, namely that all elements of the vector have been incremented:

map_vec_incr.adb:8:16: info: precondition proved
map_vec_incr.adb:8:28: info: range check proved
map_vec_incr.adb:9:11: info: postcondition proved
map_vec_incr.adb:11:18: info: precondition proved
map_vec_incr.adb:11:30: info: range check proved
map_vec_incr.adb:11:35: info: precondition proved
map_vec_incr.adb:11:59: info: range check proved
map_vec_incr.adb:11:62: info: overflow check proved
map_vec_incr.adb:15:30: info: loop invariant initialization proved
Similarly, consider a variant of the same initialization loop over a list:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;

procedure Map_List_Incr (L : in out List_T) with
  SPARK_Mode,
  Pre => (for all E of L => E /= Component_T'Last),
  Post => Length (L) = Length (L)'Old
  and then (for all I in 1 .. Length (L) =>
    Element (Model (L), I) = Element (Model (L'Old), I) + 1)
is
  Cu : Cursor := First (L);
begin
  while Has_Element (L, Cu) loop
    pragma Loop_Invariant (Length (L) = Length (L)'Loop_Entry);
    pragma Loop_Invariant
      (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
        Element (Model (L), I) = Element (Model (L'Loop_Entry), I) + 1);
    pragma Loop_Invariant
      (for all I in P.Get (Positions (L), Cu) .. Length (L) =>
        Element (Model (L), I) = Element (Model (L'Loop_Entry), I));
    Replace_Element (L, Cu, Element (L, Cu) + 1);
    Next (L, Cu);
  end loop;
end Map_List_Incr;
```

Like before, we need to use a cursor to iterate over the list. The loop invariants express that all elements up to the current loop index \( J \) have been incremented and that other elements have not been modified. Note that it is necessary to state here that the length of the list is not modified during the loop. It is because the length is used to bound the quantification over the elements of the list both in the invariant and in the postcondition. With this loop invariant, GNATprove is able to prove the postcondition of `Map_List_Incr`, namely that all elements of the list have been incremented:
Validation Loops

This kind of loops iterates over a collection to validate that every element of the collection has a valid value. The most common pattern is to exit or return from the loop if an invalid value if encountered:

<table>
<thead>
<tr>
<th>Loop Pattern</th>
<th>Sequence Validation with Early Exit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proof Objective</td>
<td>Determine (flag) if there are any invalid elements in a given collection.</td>
</tr>
<tr>
<td>Loop Behavior</td>
<td>Loops over the collection and exits/returns if an invalid element is encountered.</td>
</tr>
<tr>
<td>Loop Invariant</td>
<td>Every element encountered so far is valid.</td>
</tr>
</tbody>
</table>

Consider a procedure `Validate_Arr_Zero` that checks that all elements of an array `A` have value zero:

```plaintext
with Loop_Types; use Loop_Types;

procedure Validate_Arr_Zero (A : Arr_T; Success : out Boolean) with SPARK_Mode, Post => Success = (for all J in A'Range => A(J) = 0) is
begin
  for J in A'Range loop
    if A(J) /= 0 then
      Success := False;
      return;
    end if;
    pragma Loop_Invariant (for all K in A'First .. J => A(K) = 0);
  end loop;
  Success := True;
end Validate_Arr_Zero;
```

The loop invariant expresses that all elements up to the current loop index `J` have value zero. With this loop invariant, GNATprove is able to prove the postcondition of `Validate_Arr_Zero`, namely that output parameter `Success` is True if-and-only-if all elements of the array have value zero:
Consider now a variant of the same validation loop over a vector:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Vectors;

procedure Validate_Vec_Zero (V : Vec_T; Success : out Boolean) with
  SPARK_Mode,
  Post => Success = (for all J in First_Index (V) .. Last_Index (V) => Element (V, J) \(\rightarrow\) 0)
is
  begin
    for J in First_Index (V) .. Last_Index (V) loop
      if Element (V, J) /= 0 then
        Success := False;
        return;
      end if;
      pragma Loop_Invariant (for all K in First_Index (V) .. J => Element (V, K) = 0);
    end loop;
    Success := True;
  end Validate_Vec_Zero;
```

Like before, the loop invariant expresses that all elements up to the current loop index \(J\) have the value zero. Since variable \(V\) is not modified in the loop, no additional loop invariant is needed here for GNATprove to know that its length stays the same (this is different from the case of \(\text{Init}_\text{Vec}_\text{Zero}\) seen previously). With this loop invariant, GNATprove is able to prove the postcondition of \(\text{Validate}_\text{Vec}_\text{Zero}\), namely that output parameter \(\text{Success}\) is True if-and-only-if all elements of the vector have value zero:

```ada
validate_vec_zero.adb:3:41: info: initialization of "Success" proved
validate_vec_zero.adb:5:11: info: postcondition proved
validate_vec_zero.adb:5:84: info: range check proved
validate_vec_zero.adb:9:10: info: precondition proved
validate_vec_zero.adb:9:22: info: range check proved
validate_vec_zero.adb:13:30: info: loop invariant initialization proved
validate_vec_zero.adb:13:30: info: loop invariant preservation proved
validate_vec_zero.adb:13:67: info: precondition proved
validate_vec_zero.adb:13:79: info: range check proved
```

Similarly, consider a variant of the same validation loop over a list:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;

procedure Validate_List_Zero (L : List_T; Success : out Boolean) with
  SPARK_Mode,
  Post => Success = (for all E of L => E = 0)
is
  Cu : Cursor := First (L);
begin
  while Has_Element (L, Cu) loop
    pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 => Element (Model (L), I) = 0);
```

```ada
validate_list_zero.adb:3:41: info: initialization of "Success" proved
validate_list_zero.adb:5:11: info: postcondition proved
validate_list_zero.adb:5:84: info: range check proved
validate_list_zero.adb:9:10: info: precondition proved
validate_list_zero.adb:9:22: info: range check proved
validate_list_zero.adb:13:30: info: loop invariant initialization proved
validate_list_zero.adb:13:30: info: loop invariant preservation proved
validate_list_zero.adb:13:67: info: precondition proved
validate_list_zero.adb:13:79: info: range check proved
```
Like in the case of `Init_List_Zero` seen previously, we need to define a cursor here to iterate over the list. The loop invariant expresses that all elements up to the current cursor `Cu` have the value zero. With this loop invariant, GNATprove is able to prove the postcondition of `Validate_List_Zero`, namely that output parameter `Success` is True if-and-only-if all elements of the list have value zero:

The case of sets and maps is similar to the case of lists.

A variant of the previous validation pattern is to continue validating elements even after an invalid value has been encountered, which allows for example logging all invalid values:

Consider a variant of `Validate_Arr_Zero` that keeps validating elements of the array after a non-zero element has been encountered:

```ada
with Loop_Types; use Loop_Types;

procedure Validate_Full_Arr_Zero (A : Arr_T; Success : out Boolean) with
  SPARK_Mode,
  Post => Success = (for all J in A'Range => A(J) = 0)
is
begin
  Success := True;

  for J in A'Range loop
    if A(J) /= 0 then
      Success := False;
      -- perform some logging here instead of returning
      end if;
    pragma Loop_Invariant (Success = (for all K in A'First .. J => A(K) = 0));
  end loop;
end Validate_Full_Arr_Zero;
```
The loop invariant has been modified to state that all elements up to the current loop index J have value zero if-and-only-if the output parameter Success is True. This in turn requires to move the assignment of Success before the loop. With this loop invariant, GNATprove is able to prove the postcondition of Validate_Full_Arr_Zero, which is the same as the postcondition of Validate_Arr_Zero, namely that output parameter Success is True if-and-only-if all elements of the array have value zero:

Similarly, variants of Validate_Vec_Zero and Validate_List_Zero that keep validating elements of the collection after a non-zero element has been encountered would be proved by GNATprove.

### Counting Loops

This kind of loops iterates over a collection to count the number of elements of the collection that satisfy a given criterion:

<table>
<thead>
<tr>
<th>Loop Pattern</th>
<th>Count Elements Satisfying Criterion</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proof Objective</td>
<td>Count elements that satisfy a given criterion.</td>
</tr>
<tr>
<td>Loop Behavior</td>
<td>Loops over the collection. Increments a counter each time the value of an element satisfies the criterion.</td>
</tr>
<tr>
<td>Loop Invariant</td>
<td>The value of the counter is either 0 when no element encountered so far satisfies the criterion, or a positive number bounded by the current iteration of the loop otherwise.</td>
</tr>
</tbody>
</table>

Consider a procedure Count_Arr_Zero that counts elements with value zero in array A:

```plaintext
with Loop_Types; use Loop_Types;

procedure Count_Arr_Zero (A : Arr_T; Counter : out Natural) with SPARK_Mode,
Post => (Counter in 0 .. A'Length) and then
((Counter = 0) = (for all K in A'Range => A(K) /= 0))
is
begin
Counter := 0;
for J in A'Range loop
if A(J) = 0 then
    Counter := Counter + 1;
end if;
pragma Loop_Invariant (Counter in 0 .. J);
pragma Loop_Invariant ((Counter = 0) = (for all K in A'First .. J => A(K) /= 0));
end loop;
end Count_Arr_Zero;
```
The loop invariant expresses that the value of \texttt{Counter} is a natural number bounded by the current loop index \(J\), and that \texttt{Counter} is equal to zero exactly when all elements up to the current loop index have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of \texttt{Count\_Arr\_Zero}, namely that output parameter \texttt{Counter} is a natural number bounded by the length of the array \(A\), and that \texttt{Counter} is equal to zero exactly when all elements in \(A\) have a non-zero value:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Vectors;

procedure Count_Vec_Zero (V : Vec_T; Counter : out Natural) with
SPARK_Mode,
Post => (Counter in 0 .. Natural (Length (V))) and then
((Counter = 0) = (for all K in First_Index (V) .. Last_Index (V) => Element (V, K) /= 0))

is
begin
Counter := 0;
for J in First_Index (V) .. Last_Index (V) loop
  if Element (V, J) = 0 then
    Counter := Counter + 1;
  end if;
pragma Loop_Invariant (Counter in 0 .. J);
pragma Loop_Invariant ((Counter = 0) = (for all K in First_Index (V) .. J => Element (V, K) /= 0));
end loop;
end Count_Vec_Zero;
```

Like before, the loop invariant expresses that the value of \texttt{Counter} is a natural number bounded by the current loop index \(J\), and that \texttt{Counter} is equal to zero exactly when all elements up to the current loop index have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of \texttt{Count\_Vec\_Zero}, namely that output parameter \texttt{Counter} is a natural number bounded by the length of the vector \(V\), and that \texttt{Counter} is equal to zero exactly when all elements in \(V\) have a non-zero value:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Vectors;

procedure Count_Vec_Zero (V : Vec_T; Counter : out Natural) with
SPARK_Mode,
Post => (Counter in 0 .. Natural (Length (V))) and then
((Counter = 0) = (for all K in First_Index (V) .. Last_Index (V) => Element (V, K) /= 0))

is
begin
Counter := 0;
for J in First_Index (V) .. Last_Index (V) loop
  if Element (V, J) = 0 then
    Counter := Counter + 1;
  end if;
pragma Loop_Invariant (Counter in 0 .. J);
pragma Loop_Invariant ((Counter = 0) = (for all K in First_Index (V) .. J => Element (V, K) /= 0));
end loop;
end Count_Vec_Zero;
```
Search Loops

This kind of loops iterates over a collection to search an element of the collection that meets a given search criterion:

<table>
<thead>
<tr>
<th>Loop Pattern</th>
<th>Search with Early Exit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proof</td>
<td>Find an element or position that meets a search criterion.</td>
</tr>
<tr>
<td>Objective</td>
<td>Loops over the collection. Exits when an element that meets the search criterion is found.</td>
</tr>
<tr>
<td>Loop Invariant</td>
<td>Every element encountered so far does not meet the search criterion.</td>
</tr>
</tbody>
</table>

Consider a procedure `Search_Arr_Zero` that searches an element with value zero in array `A`:

```cpp
with Loop_Types; use Loop_Types;

procedure Search_Arr_Zero (A : Arr_T; Pos : out Opt_Index_T; Success : out Boolean)
with SPARK_Mode,
Post => Success = (for some J in A'Range => A(J) = 0) and then
(if Success then A(Pos) = 0)
begin
for J in A'Range loop
  if A(J) = 0 then
    Success := True;
    Pos := J;
    return;
  end if;
pragma Loop_Invariant (for all K in A'First .. J => A(K) /= 0);
end loop;
Success := False;
Pos := 0;
end Search_Arr_Zero;
```

The loop invariant expresses that all elements up to the current loop index `J` have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of `Search_Arr_Zero`, namely that output parameter `Success` is True if-and-only-if there is an element of the array that has value zero, and that `Pos` is the index of such an element:

```plaintext
search_arr_zero.adb:3:39: info: initialization of "Pos" proved
search_arr_zero.adb:3:62: info: initialization of "Success" proved
search_arr_zero.adb:5:11: info: postcondition proved
search_arr_zero.adb:6:31: info: index check proved
search_arr_zero.adb:15:30: info: loop invariant initialization proved
search_arr_zero.adb:15:30: info: loop invariant preservation proved
search_arr_zero.adb:15:61: info: index check proved
```

Consider now a variant of the same search loop over a vector:

```cpp
with Loop_Types; use Loop_Types; use Loop_Types.Vectors;

procedure Search_Vec_Zero (V : Vec_T; Pos : out Opt_Index_T; Success : out Boolean)
with SPARK_Mode,
Post => Success = (for some J in First_Index (V) .. Last_Index (V) => Element (V, J) = 0) and then
(if Success then Element (V, Pos) = 0)
```

```plaintext
with Loop_Types; use Loop_Types; use Loop_Types.Vectors;

procedure Search_Vec_Zero (V : Vec_T; Pos : out Opt_Index_T; Success : out Boolean)
with SPARK_Mode,
Post => Success = (for some J in First_Index (V) .. Last_Index (V) => Element (V, J) = 0) and then
(if Success then Element (V, Pos) = 0)
```
Like before, the loop invariant expresses that all elements up to the current loop index \( J \) have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of Search_Vec_Zero, namely that output parameter \( \text{Success} \) is True if-and-only-if there is an element of the vector that has value zero, and that \( \text{Pos} \) is the index of such an element:

```ada
search_vec_zero.adb:3:39: info: initialization of "Pos" proved
search_vec_zero.adb:3:62: info: initialization of "Success" proved
search_vec_zero.adb:5:11: info: postcondition proved
search_vec_zero.adb:5:73: info: precondition proved
search_vec_zero.adb:5:85: info: range check proved
search_vec_zero.adb:6:28: info: precondition proved
search_vec_zero.adb:6:40: info: range check proved
search_vec_zero.adb:10:10: info: precondition proved
search_vec_zero.adb:10:22: info: range check proved
search_vec_zero.adb:12:17: info: range check proved
search_vec_zero.adb:15:30: info: loop invariant initialization proved
search_vec_zero.adb:15:30: info: loop invariant preservation proved
search_vec_zero.adb:15:67: info: precondition proved
search_vec_zero.adb:15:79: info: range check proved
```

Similarly, consider a variant of the same search loop over a list:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
with Ada.Containers; use Ada.Containers; use Loop_Types.Lists/Formal_Model;

procedure Search_List_Zero (L : List_T; Pos : out Cursor; Success : out Boolean) with
SPARK_Mode,
Post => Success = (for some E of L => E = 0) and then
(if Success then Element (L, Pos) = 0)
is
   Cu : Cursor := First (L);
begin
   while Has_Element (L, Cu) loop
      pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
         Element (Model (L), I) /= 0);
      if Element (L, Cu) = 0 then
         Success := True;
         Pos := Cu;
         return;
      end if;
      Next (L, Cu);
   end loop;
```

Success := False;
Pos := No_Element;
end Search_List_Zero;

The loop invariant expresses that all elements up to the current cursor Cu have a non-zero value. With this loop invariant, GNATprove is able to prove the postcondition of Search_List_Zero, namely that output parameter Success is True if-and-only-if there is an element of the list that has value zero, and that Pos is the cursor of such an element:

search_list_zero.adb:4:41: info: initialization of "Pos" proved
search_list_zero.adb:4:59: info: initialization of "Success" proved
search_list_zero.adb:6:11: info: precondition proved
search_list_zero.adb:6:22: info: precondition proved
search_list_zero.adb:7:28: info: precondition proved
search_list_zero.adb:12:30: info: loop invariant initialization proved
search_list_zero.adb:12:30: info: loop invariant preservation proved
search_list_zero.adb:12:49: info: precondition proved
search_list_zero.adb:13:32: info: precondition proved
search_list_zero.adb:14:10: info: precondition proved
search_list_zero.adb:19:07: info: precondition proved

The case of sets and maps is similar to the case of lists. For more complex examples of search loops, see the SPARK Tutorial as well as the section on How to Write Loop Invariants.

Maximize Loops

This kind of loops iterates over a collection to search an element of the collection that maximizes a given optimality criterion:

<table>
<thead>
<tr>
<th>Loop Pattern</th>
<th>Search Optimum to Criterion</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proof Objective</td>
<td>Find an element or position that maximizes an optimality criterion.</td>
</tr>
<tr>
<td>Loop Behavior</td>
<td>Loops over the collection. Records maximum value of criterion so far and possibly index that maximizes this criterion.</td>
</tr>
<tr>
<td>Loop Invariant</td>
<td>Exactly one element encountered so far corresponds to the recorded maximum over other elements encountered so far.</td>
</tr>
</tbody>
</table>

Consider a procedure Search_Arr_Max that searches an element maximum value in array A:

```ada
with Loop_Types; use Loop_Types;

procedure Search_Arr_Max (A : Arr_T; Pos : out Index_T; Max : out Component_T) with SPARK_Mode,  
Post => (for all J in A'Range => A(J) <= Max) and then  
(for some J in A'Range => A(J) = Max) and then  
A(Pos) = Max  
is begin  
Max := 0;  
Pos := A'First;  
for J in A'Range loop  
if A(J) > Max then  
Max := A(J);  
Pos := J;```
The loop invariant expresses that all elements up to the current loop index \( J \) have a value less than \( \text{Max} \), and that \( \text{Max} \) is the value of one of these elements. The last loop invariant gives in fact this element, it is \( A(\text{Pos}) \), but this part of the loop invariant may not be present if the position \( \text{Pos} \) for the optimum is not recorded. With this loop invariant, GNATprove is able to prove the postcondition of \text{Search_Arr_Max}, namely that output parameter \( \text{Max} \) is the maximum of the elements in the array, and that \( \text{Pos} \) is the index of such an element:

Consider now a variant of the same search loop over a vector:

```
with Loop_Types; use Loop_Types; use Loop_Types.Vectors;

procedure Search_Vec_Max (V : Vec_T; Pos : out Index_T; Max : out Component_T) with SPARK_Mode,
  Pre => not Is_Empty (V),
  Post => (for all J in First_Index (V) .. Last_Index (V) => Element (V, J) <= Max) 
    → and then
    (for some J in First_Index (V) .. Last_Index (V) => Element (V, J) = Max) 
    → and then
    Pos in First_Index (V) .. Last_Index (V) and then
    Element (V, Pos) = Max 
is 
begin
  Max := 0;
  Pos := First_Index (V);
  for J in First_Index (V) .. Last_Index (V) loop
    if Element (V, J) > Max then
      Max := Element (V, J);
      Pos := J;
      end if;
      pragma Loop_Invariant (for all K in First_Index (V) .. J => Element (V, K) <= Max);
      pragma Loop_Invariant (for some K in First_Index (V) .. J => Element (V, K) = Max);
      pragma Loop_Invariant (Pos in First_Index (V) .. J);
      pragma Loop_Invariant (Element (V, Pos) = Max);
    end loop;
  end Search_Vec_Max;
```

Like before, the loop invariant expresses that all elements up to the current loop index \( J \) have a value less than \( \text{Max} \), and
that Max is the value of one of these elements, most precisely the value of Element (V, Pos) if the position Pos for the optimum is recorded. An additional loop invariant is needed here compared to the case of arrays to state that Pos remains within the bounds of the vector. With this loop invariant, GNATprove is able to prove the postcondition of Search_Vec_Max, namely that output parameter Max is the maximum of the elements in the vector, and that Pos is the index of such an element:

Similarly, consider a variant of the same search loop over a list:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;

procedure Search_List_Max (L : List_T; Pos : out Cursor; Max : out Component_T) with SPARK_Mode,
Pre => not Is_Empty (L),
Post => (for all E of L => E <= Max) and then
       (for some E of L => E = Max) and then
       Has_Element (L, Pos) and then
       Element (L, Pos) = Max
is
   Cu : Cursor := First (L);
begin
   Max := 0;
   Pos := Cu;
   while Has_Element (L, Cu) loop
     pragma Loop_Invariant (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
                          Element (Model (L), I) <= Max);
     pragma Loop_Invariant (Has_Element (L, Pos));
     pragma Loop_Invariant (Max = 0 or else Element (L, Pos) = Max);
     if Element (L, Cu) > Max then
```
Max := Element (L, Cu);
Pos := Cu;

end if;
Next (L, Cu);
end loop;
end Search_List_Max;

The loop invariant expresses that all elements up to the current cursor Cu have a value less than Max, and that Max is the value of one of these elements, most precisely the value of Element (L, Pos) if the cursor Pos for the optimum is recorded. Like for vectors, an additional loop invariant is needed here compared to the case of arrays to state that cursor Pos is a valid cursor of the list. A minor difference is that a loop invariant now starts with Max = 0 or else .. because the loop invariant is stated at the start of the loop (for convenience with the use of First_To_Previous) which requires this modification. With this loop invariant, GNATprove is able to prove the postcondition of Search_List_Max, namely that output parameter Max is the maximum of the elements in the list, and that Pos is the cursor of such an element:

| search_list_max.adb:4:40: info: initialization of "Pos" proved |
| search_list_max.adb:4:58: info: initialization of "Max" proved |
| search_list_max.adb:7:11: info: postcondition proved |
| search_list_max.adb:7:12: info: precondition proved |
| search_list_max.adb:8:12: info: precondition proved |
| search_list_max.adb:10:11: info: precondition proved |
| search_list_max.adb:18:30: info: loop invariant initialization proved |
| search_list_max.adb:18:30: info: loop invariant preservation proved |
| search_list_max.adb:18:49: info: precondition proved |
| search_list_max.adb:19:32: info: precondition proved |
| search_list_max.adb:20:30: info: loop invariant initialization proved |
| search_list_max.adb:20:30: info: loop invariant preservation proved |
| search_list_max.adb:21:30: info: loop invariant initialization proved |
| search_list_max.adb:21:30: info: loop invariant preservation proved |
| search_list_max.adb:21:46: info: precondition proved |
| search_list_max.adb:23:10: info: precondition proved |
| search_list_max.adb:24:17: info: precondition proved |
| search_list_max.adb:27:07: info: precondition proved |

The case of sets and maps is similar to the case of lists. For more complex examples of search loops, see the SPARK Tutorial as well as the section on How to Write Loop Invariants.

**Update Loops**

This kind of loops iterates over a collection to update individual elements based either on their value or on their position. The first pattern we consider is the one that updates elements based on their value:

<table>
<thead>
<tr>
<th>Loop Pattern</th>
<th>Modification of Elements Based on Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proof Objective</td>
<td>Elements of the collection are updated based on their value.</td>
</tr>
<tr>
<td>Loop Behavior</td>
<td>Loops over a collection and assigns the elements whose value satisfies a given modification criterion.</td>
</tr>
<tr>
<td>Loop Invariant</td>
<td>Every element encountered so far has been assigned according to its value.</td>
</tr>
</tbody>
</table>

Consider a procedure Update_Arr_Zero that sets to zero all elements in array A that have a value smaller than a given Threshold:
with Loop_Types; use Loop_Types;

procedure Update_Arr_Zero (A : in out Arr_T; Threshold : Component_T) with
  SPARK_Mode,
  Post => (for all J in A'Range => A(J) = (if A'Old(J) <= Threshold then 0 else A
    →'Old(J))));

is
  begin
    for J in A'Range loop
      if A(J) <= Threshold then
        A(J) := 0;
      end if;
  pragma Loop_Invariant (for all K in A'First .. J => A(K) = (if A'Loop_Entry(K)
    →'Loop_Entry(K))));
    -- The following loop invariant is generated automatically by GNATprove:
    -- pragma Loop_Invariant (for all K in J + 1 .. A'Last => A(K) = A'Loop_
      →'Entry(K));
  end loop;
end Update_Arr_Zero;

The loop invariant expresses that all elements up to the current loop index J have been zeroed out if initially smaller than Threshold (using Attribute Loop_Entry). With this loop invariant, GNATprove is able to prove the postcondition of Update_Arr_Zero, namely that all elements initially smaller than Threshold have been zeroed out, and that other elements have not been modified:

update_arr_zero.adb:5:11: info: postcondition proved
update_arr_zero.adb:12:30: info: loop invariant initialization proved
update_arr_zero.adb:12:30: info: loop invariant preservation proved
update_arr_zero.adb:12:61: info: index check proved
update_arr_zero.adb:12:83: info: index check proved
update_arr_zero.adb:12:124: info: index check proved

Note that the commented loop invariant expressing that other elements have not been modified is not needed, as it is an example of Automatically Generated Loop Invariants.

Consider now a variant of the same update loop over a vector:

pragma Unevaluated_Use_Of_Old (Allow);
with Loop_Types; use Loop_Types; use Loop_Types.Vectors;
use Loop_Types.Vectors.Formal_Model;

procedure Update_Vec_Zero (V : in out Vec_T; Threshold : Component_T) with
  SPARK_Mode,
  Post => Last_Index (V) = Last_Index (V)'Old
  and (for all I in 1 .. Last_Index (V) =>
    Element (V, I) =
      (if Element (Model (V)'Old, I) <= Threshold then 0
        else Element (Model (V)'Old, I)))

is
  begin
    for J in First_Index (V) .. Last_Index (V) loop
      pragma Loop_Invariant (Last_Index (V) = Last_Index (V)'Loop_Entry);
      pragma Loop_Invariant
        (for all I in 1 .. J - 1 =>
          Element (V, I) =
            (if Element (Model (V)'Loop_Entry, I) <= Threshold then 0
              else Element (Model (V)'Loop_Entry, I)));
      pragma Loop_Invariant

Like for `Map_Vec_Incr`, we need to use the `Model` function over arrays to access elements of the vector before the loop as the vector type is limited. The loop invariant expresses that all elements up to the current loop index \( J \) have been zeroed out if initially smaller than `Threshold`, that elements that follow the current loop index have not been modified, and that the length of `V` is not modified (like in `Init_Vec_Zero`). With this loop invariant, GNATprove is able to prove the postcondition of `Update_Vec_Zero`:

```ada
similarly, consider a variant of the same update loop over a list:

with Loop_Types; use Loop_Types; use Loop_Types.Lists;
with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;
procedure Update_List_Zero (L : in out List_T; Threshold : Component_T) with
  SPARK_Mode,
  Post => Length (L) = Length (L)'Old
and (for all I in 1 .. Length (L) =>
  Element (Model (L), I) =
    (if Element (Model (L'Old), I) <= Threshold then 0
    else Element (Model (L'Old), I)))
is
  Cu : Cursor := First (L);
begin
```

while Has_Element (L, Cu) loop
  pragma Loop_Invariant (Length (L) = Length (L)'Loop_Entry);
  pragma Loop_Invariant
    (for all I in 1 .. P.Get (Positions (L), Cu) - 1 =>
      Element (Model (L), I) =
        (if Element (Model (L'Loop_Entry), I) <= Threshold then 0
            else Element (Model (L'Loop_Entry), I)));
  pragma Loop_Invariant
    (for all I in P.Get (Positions (L), Cu) .. Length (L) =>
      Element (Model (L), I) = Element (Model (L'Loop_Entry), I));
  if Element (L, Cu) <= Threshold then
    Replace_Element (L, Cu, 0);
  end if;
  Next (L, Cu);
end loop;
end Update_List_Zero;

The loop invariant expresses that all elements up to the current cursor Cu have been zeroed out if initially smaller than Threshold (using function Model to access the element stored at a given position in the list and function Positions to query the position of the current cursor), and that elements that follow the current loop index have not been modified. Note that it is necessary to state here that the length of the list is not modified during the loop. It is because the length is used to bound the quantification over the elements of the list both in the invariant and in the postcondition.

With this loop invariant, GNATprove is able to prove the postcondition of Update_List_Zero, namely that all elements initially smaller than Threshold have been zeroed out, and that other elements have not been modified:

update_list_zero.adb:6:11: info: postcondition proved
update_list_zero.adb:8:13: info: precondition proved
update_list_zero.adb:9:18: info: precondition proved
update_list_zero.adb:10:20: info: precondition proved
update_list_zero.adb:15:30: info: loop invariant initialization proved
update_list_zero.adb:15:30: info: loop invariant preservation proved
update_list_zero.adb:17:10: info: loop invariant initialization proved
update_list_zero.adb:17:10: info: loop invariant preservation proved
update_list_zero.adb:17:29: info: precondition proved
update_list_zero.adb:18:13: info: precondition proved
update_list_zero.adb:19:18: info: precondition proved
update_list_zero.adb:20:20: info: precondition proved
update_list_zero.adb:22:10: info: loop invariant initialization proved
update_list_zero.adb:22:10: info: loop invariant preservation proved
update_list_zero.adb:22:24: info: precondition proved
update_list_zero.adb:23:33: info: range check proved
update_list_zero.adb:23:38: info: precondition proved
update_list_zero.adb:23:69: info: range check proved
update_list_zero.adb:24:10: info: precondition proved
update_list_zero.adb:25:10: info: precondition proved
update_list_zero.adb:27:07: info: precondition proved

The case of sets and maps is similar to the case of lists.

The second pattern of update loops that we consider now is the one that updates elements based on their position:
Consider a procedure `Update_Range_Arr_Zero` that sets to zero all elements in array `A` between indexes `First` and `Last`:

```ada
with Loop_Types; use Loop_Types;

procedure Update_Range_Arr_Zero (A : in out Arr_T; First, Last : Index_T) with
  SPARK_Mode,
  Post => A = A'Old'Update (First .. Last => 0)
is
  begin
    for J in First .. Last loop
      A(J) := 0;
      pragma Loop_Invariant (A = A'Loop_Entry'Update (First .. J => 0));
    end loop;
  end Update_Range_Arr_Zero;
```

The loop invariant expresses that all elements between `First` and the current loop index `J` have been zeroed out, and that other elements have not been modified (using a combination of `Attribute Loop_Entry` and `Attribute Update` to express this concisely). With this loop invariant, GNATprove is able to prove the postcondition of `Update_Range_Arr_Zero`, namely that all elements between `First` and `Last` have been zeroed out, and that other elements have not been modified:

```
update_range_arr_zero.adb:5:11: info: postcondition proved
update_range_arr_zero.adb:10:30: info: loop invariant initialization proved
update_range_arr_zero.adb:10:64: info: range check proved
```

Consider now a variant of the same update loop over a vector:

```ada
pragma Unevaluated_Use_Of_Old (Allow);
with Loop_Types; use Loop_Types; use Loop_Types.Vectors;
use Loop_Types.Vectors/Formal_Model;

procedure Update_Range_Vec_Zero (V : in out Vec_T; First, Last : Index_T) with
  SPARK_Mode,
  Pre => Last <= Last_Index (V),
  Post => (for all J in 1 .. Last_Index (V) =>
    if J in First .. Last then Element (V, J) = 0
    else Element (V, J) = Element (Model (V)'Old, J)))
is
  begin
    for J in First .. Last loop
      Replace_Element (V, J, 0);
      pragma Loop_Invariant (Last_Index (V) = Last_Index (V)'Loop_Entry);
      pragma Loop_Invariant
        (for all I in 1 .. Last_Index (V) =>
          if I in First .. J then Element (V, I) = 0
          else Element (V, I) = Element (Model (V)'Loop_Entry, I)));
    end loop;
```
Like for Map_Vec_Incr, we need to use the Model function over arrays to access elements of the vector before the loop as the vector type is limited. The loop invariant expresses that all elements between First and current loop index J have been zeroed, and that other elements have not been modified. With this loop invariant, GNATprove is able to prove the postcondition of Update_Range_Vec_Zero:

```ada
update_range_vec_zero.adb:8:11: info: postcondition proved
update_range_vec_zero.adb:9:44: info: precondition proved
update_range_vec_zero.adb:9:56: info: range check proved
update_range_vec_zero.adb:10:22: info: precondition proved
update_range_vec_zero.adb:10:34: info: range check proved
update_range_vec_zero.adb:10:39: info: precondition proved
update_range_vec_zero.adb:10:63: info: range check proved
update_range_vec_zero.adb:14:07: info: precondition proved
update_range_vec_zero.adb:15:30: info: loop invariant initialization proved
update_range_vec_zero.adb:15:30: info: loop invariant preservation proved
update_range_vec_zero.adb:17:10: info: loop invariant initialization proved
update_range_vec_zero.adb:17:10: info: loop invariant preservation proved
update_range_vec_zero.adb:18:41: info: precondition proved
update_range_vec_zero.adb:18:53: info: range check proved
update_range_vec_zero.adb:19:34: info: range check proved
update_range_vec_zero.adb:19:39: info: precondition proved
update_range_vec_zero.adb:19:70: info: range check proved
```

Similarly, consider a variant of the same update loop over a list:

```ada
with Loop_Types; use Loop_Types; use Loop_Types.Lists;
with Ada.Containers; use Ada.Containers; use Loop_Types.Lists.Formal_Model;

procedure Update_Range_List_Zero (L : in out List_T; First, Last : Cursor) with
  SPARK_Mode,
  Pre => Has_Element (L, First) and then Has_Element (L, Last)
  and then P.Get (Positions (L), First) <= P.Get (Positions (L), Last),
  Post => Length (L) = Length (L)'Old
  and Positions (L) = Positions (L)'Old
  and (for all I in 1 .. Length (L) =>
    (if I in P.Get (Positions (L), First) .. P.Get (Positions (L), Last) then
      Element (Model (L), I) = 0
    else
      Element (Model (L), I) = Element (Model (L'Old), I)))
  is
    Cu : Cursor := First;
begin
  loop
    pragma Loop_Invariant (Has_Element (L, Cu));
    pragma Loop_Invariant (P.Get (Positions (L), Cu) in P.Get (Positions (L),
      First) .. P.Get (Positions (L), Last));
    pragma Loop_Invariant (Length (L) = Length (L)'Loop_Entry);
    pragma Loop_Invariant (Positions (L) = Positions (L)'Loop_Entry);
    pragma Loop_Invariant (for all I in 1 .. Length (L) =>
      (if I in P.Get (Positions (L), First) .. P.Get (Positions (L),
        Entry), I)));
    Replace_Element (L, Cu, 0);
    exit when Cu = Last;
```
Compared to the vector example, it requires three additional invariants. As the loop is done via a cursor, the first two loop invariants are necessary to know that the current cursor \texttt{Cu} stays between \texttt{First} and \texttt{Last} in the list. The fourth loop invariant states that the position of cursors in \texttt{L} is not modified during the loop. It is necessary to know that the two cursors \texttt{First} and \texttt{Last} keep designating the same range after the loop. With this loop invariant, GNATprove is able to prove the postcondition of \texttt{Update\_Range\_List\_Zero}, namely that all elements between \texttt{First} and \texttt{Last} have been zeroed out, and that other elements have not been modified:

```ada
Next (L, Cu);
end loop;
end Update\_Range\_List\_Zero;
```

### 7.9.3 Manual Proof Examples

The examples in this section contain properties that are difficult to prove automatically and thus require more user interaction to prove completely. The degree of interaction required depends on the difficulty of the proof:

- simple addition of calls to ghost lemmas for arithmetic properties involving multiplication, division and modulo operations, as described in \textit{Manual Proof Using SPARK Lemma Library}
- more involved addition of ghost code for universally or existentially quantified properties on data structures and containers, as described in \textit{Manual Proof Using Ghost Code}
- interaction at the level of Verification Condition formulas in the syntax of an interactive prover for arbitrary complex properties, as described in \textit{Manual Proof Using Coq}
- interaction at the level of Verification Condition formulas in the syntax of Why3 for arbitrary complex properties, as described in \textit{Manual Proof Using GNAT Studio}
Manual Proof Using SPARK Lemma Library

If the property to prove is part of the SPARK Lemma Library, then manual proof simply consists in calling the appropriate lemma in your code. For example, consider the following assertion to prove, where X1, X2 and Y may be signed or modular positive integers:

```plaintext
R1 := X1 / Y;
R2 := X2 / Y;
pragma Assert (R1 <= R2);
```

The property here is the monotonicity of division on positive values. There is a corresponding lemma for both signed and modular integers, for both 32 bits and 64 bits integers:

- for signed 32 bits integers, use SPARK.Integer_Arithmetic_Lemmas.Lemma_Div_Is_Monotonic
- for signed 64 bits integers, use SPARK.Long_Integer_Arithmetic_Lemmas.Lemma_Div_Is_Monotonic
- for modular 32 bits integers, use SPARK.Mod32_Arithmetic_Lemmas.Lemma_Div_Is_Monotonic
- for modular 64 bits integers, use SPARK.Mod64_Arithmetic_Lemmas.Lemma_Div_Is_Monotonic

For example, the lemma for signed integers has the following signature:

```plaintext
procedure Lemma_Div_Is_Monotonic
  (Val1 : Int;
   Val2 : Int;
   Denom : Pos)
with
  Global => null,
  Pre  => Val1 <= Val2,
  Post => Val1 / Denom <= Val2 / Denom;
```

Assuming the appropriate library unit is with’ed and used in your code (see SPARK Lemma Library for details), using the lemma is simply a call to the ghost procedure Lemma_Div_Is_Monotonic:

```plaintext
R1 := X1 / Y;
R2 := X2 / Y;
Lemma_Div_Is_Monotonic (X1, X2, Y);
-- at this program point, the prover knows that R1 <= R2
-- the following assertion is proved automatically:
pragma Assert (R1 <= R2);
```

Note that the lemma may have a precondition, stating in which contexts the lemma holds, which you will need to prove when calling it. For example, a precondition check is generated in the code above to show that X1 <= X2. Similarly, the types of parameters in the lemma may restrict the contexts in which the lemma holds. For example, the type Pos for parameter Denom of Lemma_Div_Is_Monotonic is the type of positive integers. Hence, a range check may be generated in the code above to show that Y is positive.

To apply lemmas to signed or modular integers of different types than the ones used in the instances provided in the library, just convert the expressions passed in arguments, as follows:

```plaintext
R1 := X1 / Y;
R2 := X2 / Y;
Lemma_Div_Is_Monotonic (Integer(X1), Integer(X2), Integer(Y));
-- at this program point, the prover knows that R1 <= R2
-- the following assertion is proved automatically:
pragma Assert (R1 <= R2);
```
Manual Proof Using User Lemmas

If the property to prove is not part of the SPARK Lemma Library, then a user can easily add it as a separate lemma in her program. For example, suppose you need to have a proof that a fix list of numbers are prime numbers. This can be expressed easily in a lemma as follows:

```plaintext
function Is_Prime (N : Positive) return Boolean is
  (for all J in Positive range 2 .. N - 1 => N mod J /= 0);

procedure Number_Is_Prime (N : Positive) with
  Ghost, Global => null, Pre => N in 15486209 | 15487001 | 15487469, Post => Is_Prime (N);

Using the lemma is simply a call to the ghost procedure Number_Is_Prime:

Number_Is_Prime (15486209); -- at this program point, the prover knows that 15486209 is prime, so
-- the following assertion is proved automatically:
pragma Assert (Is_Prime (15486209));

Note that the lemma here has a precondition, which you will need to prove when calling it. For example, the following incorrect call to the lemma will be detected as a precondition check failure:

Number_Is_Prime (10); -- check message issued here

Then, the lemma procedure can be either implemented as a null procedure, in which case GNATprove will issue a check message about the unproved postcondition, which can be justified (see Justifying Check Messages) or proved with Coq (see Manual Proof Using Coq):

```plaintext
procedure Number_Is_Prime (N : Positive) is null;
```

Or it can be implemented as a normal procedure body with a single assumption:

```plaintext
procedure Number_Is_Prime (N : Positive) is
begin
  pragma Assume (Is_Prime (N));
  end Number_Is_Prime;
```

Or it can be implemented in some cases as a normal procedure body with ghost code to achieve fully automatic proof, see Manual Proof Using Ghost Code.

Manual Proof Using Ghost Code

Guiding automatic solvers by adding intermediate assertions is a commonly used technique. More generally, whole pieces of Ghost Code can be added to enhance automated reasoning.

Proving Existential Quantification

Existentially quantified properties are difficult to verify for automatic solvers. Indeed, it requires coming up with a concrete value for which the property holds and solvers are not good at guessing. As an example, consider the following program:
Here we assume that the first element of an array \( A \) is 0, whereas is last element is positive. In such a case, we are sure that there is an index \( I \) in the array such \( A(I) = 0 \) but not \( A(I+1) \). Indeed, we know that \( A \) starts with a non-empty sequence of zeros. The last element of this sequence has the expected property. However, automatic solvers are unable to prove such a property automatically because they cannot guess which index they should consider. To help them, we can define a ghost function returning a value for which the property holds, and call it from an assertion:

\[
\text{function Find_Pos (A : Nat_Array) return Positive with Ghost,}
\]

\[
\text{Pre} \Rightarrow \text{A (A'First) = 0 and then A (A'Last) > 0,}
\]

\[
\text{Post} \Rightarrow \text{Find_Pos'Result in A'First .. A'Last - 1 and then}
\]

\[
\text{A (Find_Pos'Result) = 0 and then A (Find_Pos'Result + 1) > 0;}
\]

Automatic solvers are now able to discharge the proof.

**Performing Induction**

Another difficult point for automated solvers is proof by induction. Though some automatic solvers do have heuristics allowing them to perform the most simple inductive proofs, they generally are lost when the induction is less straightforward. For example, in the example below, we state that the array \( A \) is sorted in two different ways, first by saying that each element is bigger than the one just before, and then by saying that each element is bigger than all the ones before:

\[
\text{pragma Assume (for all I in A'Range =>}
\]

\[
\text{(if I > A'First then A (I) > A (I - 1))});
\]

\[
\text{pragma Assert (for all J in A'Range => (if I > J then A (I) > A (J)))};
\]

The second assertion is provable from the first one by induction over the number of elements separating \( I \) and \( J \), but automatic solvers are unable to verify this code. To help them, we can use a ghost loop. In the loop invariant, we say that the property holds for all indexes \( I \) and \( J \) separated by less than \( K \) elements:

\[
\text{procedure Prove_Sorted (A : Nat_Array) with Ghost is}
\]

\[
\text{begin}
\]

\[
\text{for K in 0 .. A'Length loop}
\]

\[
\text{pragma Loop_Invariant}
\]

\[
\text{(for all I in A'Range => (for all J in A'Range =>}
\]

\[
\text{(if I > J and then I - J <= K then A (I) > A (J)))};
\]

\[
\text{end loop;}
\]

\[
\text{end Prove_Sorted;}
\]

GNATprove will verify that the invariant holds in two steps, first it will show that the property holds at the first iteration, and then that, if it holds at a given iteration, then it also holds at the next (see *Loop Invariants*). Both proofs are straightforward using the assumption.
Note that we have introduced a ghost subprogram above to contain the loop. This will allow the compiler to recognize that this loop is ghost, so that it can be entirely removed when assertions are disabled.

If Prove_Sorted is declared locally to the subprogram that we want to verify, it is not necessary to supply a contract for it, as local subprograms with no contracts are inlined (see Contextual Analysis of Subprograms Without Contracts). We can still choose to provide such a contract to turn Prove_Sorted into a lemma (see Manual Proof Using User Lemmas).

A Concrete Example: a Sort Algorithm

We show how to prove the correctness of a sorting procedure on arrays using ghost code. In particular, we want to show that the sorted array is a permutation of the input array. A common way to define permutations is to use the number of occurrences of elements in the array, defined inductively over the size of its array parameter (but it is not the only one, see Ghost Variables):

```plaintext
package Sort_Types with SPARK_Mode is
  subtype Index is Integer range 1 .. 100;
  type Nat_Array is array (Index range <>) of Natural;
end Sort_Types;

package Perm with SPARK_Mode, Ghost is
  subtype Nb_Occ is Integer range 0 .. 100;

  function Remove_Last (A : Nat_Array) return Nat_Array is
    (A (A'First .. A'Last - 1))
  with Pre => A'Length > 0;

  function Occ_Def (A : Nat_Array; E : Natural) return Nb_Occ is
    (if A'Length = 0 then 0
     elsif A (A'Last) = E then Occ_Def (Remove_Last (A), E) + 1
     else Occ_Def (Remove_Last (A), E))
  with Post => Occ_Def'Result <= A'Length;
  pragma Annotate (GNATprove, Terminating, Occ_Def);

  function Occ (A : Nat_Array; E : Natural) return Nb_Occ is (Occ_Def (A, E))
  with Post => Occ'Result <= A'Length;

  function Is_Perm (A, B : Nat_Array) return Boolean is
    (for all E in Natural => Occ (A, E) = Occ (B, E));
end Perm;
```

Note that Occ was introduced as a wrapper around the recursive definition of Occ_Def. This is to work around a current limitation of the tool that only introduces axioms for postconditions of non-recursive functions (to avoid possibly introducing unsound axioms that would not be detected by the tool).

The only property of the function Occ required to prove that swapping two elements of an array is in fact a permutation, is the way Occ is modified when updating a value of the array.

There is no native construction for axioms in SPARK 2014. As a workaround, a ghost subprogram, named “lemma subprogram”, can be introduced with the desired property as a postcondition. An instance of the axiom will then be available whenever the subprogram is called. Notice that an explicit call to the lemma subprogram with the proper
arguments is required whenever an instance of the axiom is needed, like in manual proofs in an interactive theorem prover. Here is how a lemma subprogram can be defined for the desired property of Occ:

```plaintext
package Perm.Lemma_Subprograms with SPARK_Mode, Ghost is

function Is_Set (A : Nat_Array; I : Index; V : Natural; R : Nat_Array) return Boolean is (R'First = A'First and then R'Last = A'Last and then R (I) = V and then (for all J in A'Range => (if I /= J then R (J) = A (J)))) with

procedure Occ_Set (A : Nat_Array; I : Index; V, E : Natural; R : Nat_Array) with Pre => I in A'Range and then Is_Set (A, I, V, R), Post => (if V = A (I) then Occ (R, E) = Occ (A, E) elsif V = E then Occ (R, E) = Occ (A, E) + 1 elsif A (I) = E then Occ (R, E) = Occ (A, E) - 1 else Occ (R, E) = Occ (A, E));

end Perm.Lemma_Subprograms;
```

This “axiom” can then be used to prove an implementation of the selection sort algorithm. Lemma subprograms need to be explicitly called for every natural. To achieve that, a loop is introduced. The inductive proof necessary to demonstrate the universally quantified formula is then achieved thanks to the loop invariant, playing the role of an induction hypothesis:

```plaintext
with Perm.Lemma_Subprograms; use Perm.Lemma_Subprograms;
package body Sort with SPARK_Mode is

----------------------------------------------------------------------------
procedure Swap (Values : in out Nat_Array; X : in Positive; Y : in Positive) with Pre => (X in Values'Range and then Y in Values'Range and then X /= Y), Post => Is_Perm (Values'Old, Values) and Values (X) = Values'Old (Y) and Values (Y) = Values'Old (X) and (for all Z in Values'Range => (if Z /= X and Z /= Y then Values (Z) = Values'Old (Z))) is

Temp : Integer;

-- Ghost variables
Init : constant Nat_Array (Values'Range) := Values with Ghost;
Interm : Nat_Array (Values'Range) with Ghost;

-- Ghost procedure
procedure Prove_Perm with Ghost,
```
Pre => X in Values'Range and then Y in Values'Range and then
    Is_Set (Init, X, Init (Y), Interm)
and then Is_Set (Interm, Y, Init (X), Values),
Post => Is_Perm (Init, Values)
is
begin
    for E in Natural loop
        Occ_Set (Init, X, Init (Y), E, Interm);
        Occ_Set (Interm, Y, Init (X), E, Values);
        pragma Loop_Invariant
            (for all F in Natural'First .. E =>
                Occ (Values, F) = Occ (Init, F));
    end loop;
end Prove_Perm;

begin
    Temp := Values (X);
    Values (X) := Values (Y);
    -- Ghost code
    pragma Assert (Is_Set (Init, X, Init (Y), Values));
    Interm := Values;
    Values (Y) := Temp;
    -- Ghost code
    pragma Assert (Is_Set (Interm, Y, Init (X), Values));
    Prove_Perm;
end Swap;

-- Finds the index of the smallest element in the array
function Index_Of_Minimum (Values : in Nat_Array)
    return Positive
with
    Pre => Values'Length > 0,
    Post => Index_Of_Minimum'Result in Values'Range and then
        (for all I in Values'Range =>
            Values (Index_Of_Minimum'Result) <= Values (I))
is
    Min : Positive;
begin
    Min := Values'First;
    for Index in Values'Range loop
        if Values (Index) < Values (Min) then
            Min := Index;
        end if;
    end loop;
    pragma Loop_Invariant
        (Min in Values'Range and then
            (for all I in Values'First .. Index =>
                Values (Min) <= Values (I)));
    end loop;
    return Min;
end Index_Of_Minimum;

procedure Selection_Sort (Values : in out Nat_Array) is
    Smallest : Positive; -- Index of the smallest value in the unsorted part
begin
    if Values'Length = 0 then
```ada
return;
end if;

for Current in Values'First .. Values'Last - 1 loop
    Smallest := Index_Of_Minimum (Values (Current .. Values'Last));
    if Smallest /= Current then
        Swap (Values => Values,
            X => Current,
            Y => Smallest);
    end if;

    pragma Loop_Invariant (
        for all I in Values'First .. Current =>
            (for all J in I + 1 .. Values'Last =>
                Values (I) <= Values (J)));
    pragma Loop_Invariant (Is_Perm (Values'Loop_Entry, Values));
end loop;

end Selection_Sort;
end Sort;
```

```ada
with Sort_Types; use Sort_Types;
with Perm; use Perm;

package Sort with SPARK_Mode is
    -- Sorts the elements in the array Values in ascending order
    procedure Selection_Sort (Values : in out Nat_Array) with
        Post => Is_Perm (Values'Old, Values) and then
            (if Values'Length > 0 then
                (for all I in Values'First .. Values'Last - 1 =>
                    Values (I) <= Values (I + 1)));
end Sort;
```

The procedure Selection_Sort can be verified using GNATprove, with the default prover CVC4, in less than 1s per verification condition.

```
sort.adb:16:16: info: postcondition proved
sort.adb:17:18: info: index check proved
sort.adb:17:35: info: index check proved
sort.adb:18:18: info: index check proved
sort.adb:18:35: info: index check proved
sort.adb:20:48: info: index check proved
sort.adb:20:65: info: index check proved
sort.adb:22:07: info: initialization of "Temp" proved
sort.adb:25:07: info: range check proved
sort.adb:25:53: info: length check proved
sort.adb:26:07: info: initialization of "Interm" proved
sort.adb:26:07: info: range check proved
sort.adb:31:09: info: precondition proved
sort.adb:31:23: info: range check proved
sort.adb:31:32: info: index check proved
sort.adb:32:18: info: precondition proved
sort.adb:32:34: info: range check proved
```
To complete the verification of our selection sort, the only remaining issue is the correctness of the axiom for Occ. It can be discharged using the definition of Occ. Since this definition is recursive, the proof requires induction, which is
not normally in the reach of an automated prover. For GNATprove to verify it, it must be implemented using recursive calls on itself to assert the induction hypothesis. Note that the proof of the lemma is then conditioned to the termination of the lemma functions, which currently cannot be verified by GNATprove.

```ada
package body Perm.Lemma_Subprograms with SPARK_Mode is

procedure Occ_Eq (A, B : Nat_Array; E : Natural) with
  Pre => A = B,
  Post => Occ (A, E) = Occ (B, E);
procedure Occ_Eq (A, B : Nat_Array; E : Natural) is
  begin
    if A'Length = 0 then
      return;
    end if;

    if A (A'Last) = E then
      pragma Assert (B (B'Last) = E);
    else
      pragma Assert (B (B'Last) /= E);
    end if;

    Occ_Eq (Remove_Last (A), Remove_Last (B), E);
end Occ_Eq;

procedure Occ_Set (A : Nat_Array; I : Index; V, E : Natural; R : Nat_Array)
  is
    B : Nat_Array := Remove_Last (A);
  begin
    if A'Length = 0 then
      return;
    end if;

    if I = A'Last then
      Occ_Eq (B, Remove_Last (R), E);
    else
      B (I) := V;
      Occ_Eq (Remove_Last (R), B, E);
      Occ_Set (Remove_Last (A), I, V, E, B);
    end if;
  end Occ_Set;
end Perm.Lemma_Subprograms;
```

GNATprove proves automatically all checks on the final program, with a small timeout of 1s for the default automatic prover CVC4.

```
perm-lemma_subprograms.adb:5:14: info: postcondition proved
perm-lemma_subprograms.adb:13:14: info: index check proved
perm-lemma_subprograms.adb:14:25: info: assertion proved
perm-lemma_subprograms.adb:14:29: info: index check proved
perm-lemma_subprograms.adb:16:25: info: assertion proved
perm-lemma_subprograms.adb:16:29: info: index check proved
perm-lemma_subprograms.adb:19:07: info: precondition proved
perm-lemma_subprograms.adb:19:15: info: precondition proved
perm-lemma_subprograms.adb:19:32: info: precondition proved
```
Manual Proof Using Coq

This section presents a simple example of how to prove interactively a check with an interactive prover like Coq when GNATprove fails to prove it automatically (for installation of Coq, see also: Coq). Here is a simple SPARK procedure:

```plaintext
procedure Nonlinear (X, Y, Z : Positive; R1, R2 : out Natural) with
  SPARK_Mode,
  Pre => Y > Z,
  Post => R1 <= R2
is
begin
  R1 := X / Y;
  R2 := X / Z;
end Nonlinear;
```

When only the Alt-Ergo prover is used, GNATprove does not prove automatically the postcondition of the procedure, even when increasing the value of the timeout:

```
nonlinear.adb:1:42: info: initialization of "R1" proved
nonlinear.adb:1:46: info: initialization of "R2" proved
nonlinear.adb:4:11: medium: postcondition might fail, cannot prove R1 <= R2
nonlinear.adb:7:12: info: division check proved
nonlinear.adb:7:12: info: range check proved
nonlinear.adb:8:12: info: division check proved
nonlinear.adb:8:12: info: range check proved
```

This is expected, as the automatic prover Alt-Ergo has only a simple support for non-linear integer arithmetic. More generally, it is a known difficulty for all automatic provers, although, in the case above, using prover CVC4 is enough to prove automatically the postcondition of procedure Nonlinear. We will use this case to demonstrate the use of a manual prover, as an example of what can be done when automatic provers fail to prove a check. We will use Coq here.

The Coq input file associated to this postcondition can be produced by either selecting SPARK → Prove Check and specifying Coq as alternate prover in GNAT Studio or by executing on the command-line:

```
gnatprove -P <prj_file>.gpr --limit-line=nonlinear.adb:4:11:VC_POSTCONDITION --prover=Coq
```

The generated file contains many definitions and axioms that can be used in the proof, in addition to the ones in Coq standard library. The property we want to prove is at the end of the file:
**Theorem** WP_parameter_def :

\[
((\text{in\_range1 } x) \land ((\text{in\_range1 } y) \land ((\text{in\_range1 } z) \land (((0\%Z \leq 2147483647\%Z) \rightarrow (\text{in\_range } r1)) \land (((0\%Z \leq 2147483647\%Z) \rightarrow (\text{in\_range } r2)) \land ((z < y) \%Z) \land (((o = (Z\text{Arith.BinInt.Z.quot } x y)) \land (\text{in\_range } (Z\text{Arith.BinInt.Z.quot } x y))) \land (((\text{mk\_int__ref } result) = (\text{mk\_int__ref } r1)) \land (r11 = o))) \land (((o1 = (Z\text{Arith.BinInt.Z.quot } x z)) \land (\text{in\_range } (Z\text{Arith.BinInt.Z.quot } x z))) \land ((\text{result1 } = r2) \land (r21 = o1)))) \land (((r21 = r22) \land (r11 = r12)) \land ((r23 = r21) \land (r13 = r11))) \rightarrow (r12 \leq r22)\%Z.
\]

**intros** r1 r2 o o1 result r11 result1 r21 r12 r22 r13 r23

\(<h1, (h2, h3, h4, h5, h6, (((h7, h8), (h9, h10)), ((h11, h12), (h13, h14)), ((h15, h16), (h17, h18)))))>.

**Qed.**

From the **forall** to the first . we can see the expression of what must be proved, also called the goal. The proof starts right after the dot and ends with the **Qed** keyword. Proofs in Coq are done with the help of different tactics which will change the state of the current goal. The first tactic (automatically added) here is **intros**, which allows to “extract” variables and hypotheses from the current goal and add them to the current environment. Each parameter to the **intros** tactic is the name that the extracted element will have in the new environment. The **intros** tactic here puts all universally quantified variables and all hypotheses in the environment. The goal is reduced to a simple inequality, with all potentially useful information in the environment.

Here is the state of the proof as displayed in a suitable IDE for Coq:
Some expressions are enclosed in \((\)\%Z, which means that they are dealing with relative integers. This is necessarily in order to use the operators (e.g. \(<\) or \(+\)) on relative integers instead of using the associated Coq function or to declare a relative integer constant (e.g. \(0\%Z\)).

Next, we can use the `subst` tactic to automatically replace variables by terms to which they are equal (as stated by the hypotheses in the current environment) and clean the environment of replaced variables. Here, we can get rid of many variables at once with `subst o o1 result1 r11 r12 r21 r22 r23 r13`. (note the presence of the . at the end of each tactic). The new state is:

```
1 subgoal
  r1, r2, result : int
  h1 : in_range x
  h2 : in_range y
  h3 : in_range z
  h4 : (0 <= 2147483647)%Z -> in_range r1
  h5 : (0 <= 2147483647)%Z -> in_range r2
  h6 : (z < y)%Z
  h8 : in_range (x \div y)
  h9 : mk_int__ref result = mk_int__ref r1
  h12 : in_range (x \div z)
  ______________________________(1/1)
  (x \div y <= x \div z)%Z
```

At this state, the hypotheses alone are not enough to prove the goal without proving properties about \(\div\) and \(<\) operators. It is necessary to use theorems from the Coq standard library. Coq provides a command `SearchAbout` to find theorems and definition concerning its argument. For instance, to find the theorems referring to the operator \(\div\), we use `SearchAbout Z.quot`, where `Z.quot` is the underlying function for the \(\div\) operator. Among the theorems displayed, the conclusion (the rightmost term separated by \(\rightarrow\) operator) of one of them seems to match our current goal:

```
Z.quot_le_compat_l:
  forall p q r : int, (0 <= p)%Z -> (0 < q <= r)%Z -> (p \div r <= p \div q)%Z
```

The tactic `apply` allows the use of a theorem or an hypothesis on the current goal. Here we use: `apply Z.quot_le_compat_l`. This tactic will try to match the different variables of the theorem with the terms present in the goal. If it succeeds, one subgoal per hypothesis in the theorem will be generated to verify that the terms matched with the theorem variables satisfy the hypotheses on those variables required by the theorem. In this case, \(p\) is matched with \(x\), \(q\) with \(z\) and \(r\) with \(y\) and the new state is:

```
2 subgoals
  r1, r2, result : int
  h1 : in_range x
  h2 : in_range y
  h3 : in_range z
  h4 : (0 <= 2147483647)%Z -> in_range r1
  h5 : (0 <= 2147483647)%Z -> in_range r2
  h6 : (z < y)%Z
  h8 : in_range (x \div y)
  h9 : mk_int__ref result = mk_int__ref r1
```
As expected, there are two subgoals, one per hypothesis of the theorem. Once the first subgoal is proved, the rest of the script will automatically apply to the second one. Now, if we look back at the SPARK code, X is of type Positive so X is greater than 0 and in_rangeN (where N is a number) are predicates generated by SPARK to state the range of a value from a ranged subtype interpreted as a relative integer in Coq. Here, the predicate in_range1 provides the property needed to prove the first subgoal which is that “All elements of subtype positive have their integer interpretation in the range 1 .. (2^{31} - 1)”. However, the goal does not match exactly the predicate, because one is a comparison with 0, while the other is a comparison with 1. Transitivity on “lesser or equal” relation is needed to prove this goal, of course this is provided in Coq’s standard library:

**Lemma Zle_trans : forall n m p:Z, (n <= m)%Z -> (m <= p)%Z -> (n <= p)%Z.**

Since the lemma’s conclusion contains only two variables while it uses three, using tactic apply Zle_trans. will generate an error stating that Coq was not able to find a term for the variable m. In this case, m needs to be instantiated explicitly, here with the value 1: apply Zle_trans with (m:= 1%Z). There are two new subgoals, one to prove that 0 <= 1 and the other that 1 <= x:

3 subgoals

r1, r2, result : int
h1 : in_range1 x
h2 : in_range1 y
h3 : in_range1 z
h4 : (0 <= 2147483647)%Z -> in_range r1
h5 : (0 <= 2147483647)%Z -> in_range r2
h6 : (z < y)%Z
h8 : in_range (x ÷ y)
h9 : mk_int__ref result = mk_int__ref r1
h12 : in_range (x ÷ z)

______________________________________(1/3)
| (0 <= 1)%Z ______________________(2/3)
| (1 <= x)%Z ______________________(3/3)
| (0 < z <= y)%Z

To prove that 0 <= 1, the theorem **Lemma Zle_0_1 : (0 <= 1)%Z**. is used. apply Zle_0_1 will not generate any new subgoals since it does not contain implications. Coq passes to the next subgoal:

2 subgoals

r1, r2, result : int
h1 : in_range1 x
h2 : in_range1 y
h3 : in_range1 z
h4 : (0 <= 2147483647)%Z -> in_range r1
h5 : (0 <= 2147483647)%Z -> in_range r2
h6 : (z < y)%Z
h8 : in_range (x ÷ y)
h9 : mk_int__ref result = mk_int__ref r1
h12 : in_range (x ÷ z)

______________________________________(1/2)
This goal is now adapted to the in_range1 definition with h1 which does not introduce subgoals, so the subgoal 1 is fully proved, and all that remains is subgoal 2:

Transitivity is needed again, as well as in_range1. In the previous subgoal, every step was detailed in order to show how the tactic apply worked. Now, let’s see that proof doesn’t have to be this detailed. The first thing to do is to add the fact that \( 1 <= z \) to the current environment: \texttt{unfold in_range1 in h3}. will add the range of \( z \) as an hypothesis in the environment:

At this point, the goal can be solved simply using the \texttt{omega} tactic. \texttt{omega} is a tactic made to facilitate the verification of properties about relative integers equalities and inequalities. It uses a predefined set of theorems and the hypotheses present in the current environment to try to solve the current goal. \texttt{omega} either solves the goal or, if it fails, it does not generate any subgoals. The benefit of the latter way is that there are less steps than with the previous subgoal for a more complicated goal (there are two inequalities in the second subgoal) and we do not have to find the different theorems we need to solve the goal without omega.

Finally, here is the final version of the proof script for the postcondition:

```
Theorem WP_parameter_def :
  forall (r1:Z) (r2:Z) (o:Z) (o1:Z) (result:Z)
    (r13:Z) (r23:Z),
    ((in_range1 x)
     /
     ((in_range1 y)
```
/
**(in_range1 \text{ z})**
/
**(\text{ 0\%\ Z} \leq 2147483647\%\ Z \rightarrow (in\_range \text{ r1}))**
/
**(\text{ 0\%\ Z} \leq 2147483647\%\ Z \rightarrow (in\_range \text{ r2}))**
/
**(\text{ z} \leq \text{ y}\%\ Z**
/
**(\text{ (o} = (\text{ ZArith.BinInt.Z.quot x y}))**
/
**(in\_range (\text{ ZArith.BinInt.Z.quot x y}))**
/
**(\text{ (mk\_int\_ref \text{ result}) = (mk\_int\_ref \text{ r1}))**
/
**(\text{ r11} = \text{ o}))**
/
**(\text{ (o1 = (ZArith.BinInt.Z.quot x z))**
/
**(in\_range (ZArith.BinInt.Z.quot x z)))**
/
**(\text{ (result1} = \text{ r2})**
/
**(\text{ (r21} = \text{ o1))])**
/
**(\text{ (r21} = \text{ r22})**
/
**(\text{ (r11} = \text{ r12})**
/
**(\text{ (r23} = \text{ r21})**
/
**(\text{ (r13} = \text{ r11)})**)))))))))) \rightarrow
**(\text{ (r12} \leq \text{ r22})\%\ Z**.

\begin{verbatim}
intros r1 r2 o o1 result r11 result1 r21 r22 r13 r23
(h1, (h2, (h3, (h4, (h5, (h6, ((h7, (h8), (h9, (h10)), ((h11, (h12), (h13, (h14)), ((h15, (h16), (h17, (h18)))))))))))).
subst o o1 result1 r11 r12 r21 r22 r23 r13.
apply Z.quot_le_compat_l.
apply Zle_trans with (m:=1\%\ Z).
(* 0 \leq 1 *)
apply Zle_0_1.
(* 1 \leq x *)
unfold in_range1 in h1.
apply h1.
(* 0 < z \leq y *)
unfold in_range1 in h3.
omega.
Qed.
\end{verbatim}

To check and save the proof:

```bash
gnatprove -P <prj_file>.gpr --limit-line=nonlinear.
```

Now running GNATprove on the project should confirm that all checks are proved:

```
nonlinear.adb:4:11: info: postcondition proved
nonlinear.adb:7:12: info: range check proved
nonlinear.adb:7:12: info: division check proved
nonlinear.adb:8:12: info: range check proved
nonlinear.adb:8:12: info: division check proved
```

**Manual Proof Using GNAT Studio**

This section presents a simple example of how to prove interactively a check with the manual proof feature. We reuse here the example presented in section *Manual Proof Using Coq*. We launch the Manual Proof on the failed check at:

```
nonlinear.adb:4:11:VC_POSTCONDITION
```

Right click on the corresponding location in the Locations terminal of GNAT Studio and select the menu *SPARK → Start Manual Proof*. The manual proof interface immediately starts. Both the Proof Tree and the Verification
The Verification Condition is very similar to the one generated for Coq (as expected: the check is the same). As soon as the menus appear, the user can start using transformations to simplify the goal thus helping automatic provers. We will start the description of a complete proof for this lemma using only altergo. At first, we want to remove the equalities between constants that make the VC very difficult to read. These equalities were generated by the weakest precondition algorithm. They can be safely removed by subst and subst_all. In Manual Proof console, type:

\texttt{subst\_all}

The transformation node was added to the Proof Tree and the current node is now changed making your transformation appear and the new Verification Condition to prove has been simplified:
We should also have replaced the value of $o1$ and $o$ in the goal. These were not replaced because $H6$ and $H7$ are conjunctions. We can destruct both hypotheses $H6$ and $H7$ in order to make the equalities appear at toplevel:

destruct $H6$

Then:

subst $o1$

After simplifications, the goal is the following:

\[
\begin{align*}
\text{axiom } & H2 : \text{dynamic\_property first \ last X} \\
\text{axiom } & H3 : \text{dynamic\_property first \ last Y} \\
\text{axiom } & H4 : \text{dynamic\_property first \ last Z} \\
\text{axiom } & H5 : \text{first1} \leq \text{last1} \rightarrow \text{dynamic\_property1 first1 last1 R14} \\
\text{axiom } & H6 : \text{first1} \leq \text{last1} \rightarrow \text{dynamic\_property1 first1 last1 R23} \\
\text{axiom } & H7 : Y > Z \\
\text{axiom } & H1 : \text{in\_rangel (div X Y)} \\
\text{axiom } & H : \text{in\_rangel (div X Z)}
\end{align*}
\]

----------------------------- Goal ---------------------------

\[
\text{goal WP\_parameter def : } o1 \leq o
\]

This is more readable but altergo still does not manage to prove it:

altergo

answers Unknown as seen in the Proof Tree.

We need to investigate further what we know about div, and what would be useful to prove the goal:

search div

returns in the Manual Proof console:

\[
\begin{align*}
\text{function } & \text{div (x:int) (y:int) : int = div1 x y} \\
\text{axiom } & H1 : \text{in\_rangel (div X Y)} \\
\text{axiom } & H : \text{in\_rangel (div X Z)}
\end{align*}
\]
So, \texttt{div} is actually a shortcut for a function named \texttt{div1}. Let’s search for this one:

```
search div1
```

Now, we get a lot of axioms about \texttt{div} and \texttt{mod} as expected. In particular, the axiom \texttt{Div_mod} looks interesting:

```
axiom Div_mod :
  forall x:int, y:int. not y = 0 -> x = ((y \times \texttt{div1} x y) + \texttt{mod1} x y)
```

Perhaps, it is a good idea to instantiate this axiom with \(X\) and \(Y\) (respectively \(X\) and \(Z\)) and see what is provable from there:

```
instantiate Div_mod X,Y
```

A new hypothesis appears in the context:

```
axiom Div_mod : not Y = 0 -> X = ((Y \times \texttt{div1} X Y) + \texttt{mod1} X Y)
```

After some struggling with those hypotheses, it looks like they won’t actually help proving the goal. Let’s remove these hypotheses:

```
remove Div_mod
```

Alternatively, we can go back to the node above the current one in the Proof Tree by clicking on it. We can also remove the transformation node corresponding to the use of \texttt{instantiate} by selecting it and writing in Manual Proof console:

```
Remove
```

The actual proof is going to use an additional lemma that we are going to introduce with \texttt{assert}. The Coq proof uses this exact same lemma inside the proof of \texttt{Z.quot_le_compat_l}. We could have expected \texttt{altergo} to have this lemma inside its theories but, currently, it does not:

```
assert (forall q a b:int. 0<b \rightarrow 0<a \rightarrow b\times q <= a \rightarrow q <= \texttt{div1} a b)
```

So, two new nodes appear below the current one (the first to prove the formula we just wrote and the second adding it as an hypothesis). We are going to prove this \texttt{assert} by induction on the unbounded integer \(q\) (the base case is 0):

```
induction q from 0
```

Both new goals can be discharged by \texttt{altergo}: this small lemma is proven. Now, we can use it in our proof. We begin by unfolding \texttt{div} to make \texttt{div1} appear:

```
unfold div
```

Then we can apply our new lemma:

```
apply h
```

We are left with the following three subgoals to prove:

```
goal G : (Z \times \texttt{div1} X Y) <= X
goal G : 0 < X
goal G : 0 < Z
```
altergo proves the positivity of X and Z easily but it does not find a proof for the first subgoal. We are going to prove this one by transitivity of less or equal using Y * div1 X Y. Currently, we don’t have a transformation to apply the transitivity directly so we assert it:

```
assert ((Y * div1 X Y <= X && Z) * ((div1 X Y) <= Y * div1 X Y))
```

To make two goals of this conjunction, we are using:

```
split_goal_wp
```

The left part is provable by altergo. On the second part, we are going to apply an axiom CompatOrderMult we found by querying what is known about the multiplication:

```
search (*)
```

We apply it to the current goal:

```
apply CompatOrderMult
```

The remaining goals can all be proven by altergo. This closes the proof. A popup should appear asking if the user wants to save and exit. Answer no because we want to make the proof cleaner (you can still save it by writing `Save` in `Manual Proof` console). Select a node and type:

```
clean
```

All attempted proof that did not succeed are erased and only the successful proofs remain. The proof can now be saved and manual proofs menus closed by clicking on `SPARK → Exit Manual Proof` from the menu. The proof is complete and GNATprove can be called again on the whole project to check that the former failing check is now understood as proved by GNATprove.

### 7.10 Examples in the Toolset Distribution

Further examples of SPARK are distributed with the SPARK toolset. These are contained in the `share/examples/spark` directory below the directory where the toolset is installed, and can be accessed from the IDE (either GNAT Studio or GNATBench) via the `Help → SPARK → Examples` menu item.

These examples range from single subprograms to demo programs with dozens of units. In this section, we describe briefly the code in each example, the properties specified, and the results of GNATprove’s analysis.

#### 7.10.1 Individual Subprograms

These examples contain usually a single subprogram, and are typically very small (a few dozens slocs).

**binary_search and binary_search_unconstrained**

These programs search for a given value in an ordered array. The postcondition of the main function `Binary_Search` expresses that the search is successful if-and-only-if the array contains the value searched, and if so the index returned is one at which the array contains this value. GNATprove proves all checks on these programs. The version with an unconstrained array is the same as the one presented in the section on *How to Write Loop Invariants*, and used in a series of two articles published by Johannes Kanig in Electronic Design to compare dynamic and static verification techniques (see [http://blog.adacore.com/testing-static-formal](http://blog.adacore.com/testing-static-formal)).
euclidian_division

This program implements the Euclidian division of two integers Dividend and Divisor, returning their quotient and remainder in Quotient and Remainder respectively. The postcondition of procedure Linear_Div expresses the expected mathematical relation between inputs and outputs. GNATprove proves all checks on this program.

gcd

This program computes the greatest common divisor between two positive numbers. The postcondition of function GCD checks that the number returned is indeed the greatest common divisor of its arguments. Four versions of the function are provided:

- a simple version that searches linearly for the GCD.
- a modification of the simple version with a more mathematical expression of divisibility in the contract of GCD.
- a modification of the simple version that optimizes the search to skip half the candidates for GCD.
- Euclid’s algorithm for computing the GCD.

Each successive version makes use of more complex Ghost Code to prove that the implementation of GCD satisfies its contract. GNATprove proves all checks on this program, except for some elementary lemmas on modulo operator. This is detailed in the following post on AdaCore blog: https://blog.adacore.com/gnatprove-tips-and-tricks-proving-the-ghost-common-denominator-gcd

intro

This program computes the price of a basket of items. The postcondition of the main function Price_Of_Basket checks that the resulting price is at least the price of the most expensive item. GNATprove proves all checks on this program.

linear_search

This program searches for a given value in an unordered array. The postcondition of the main function Linear_Search expresses that if the search is successful then the index returned is one at which the array contains the value searched. GNATprove proves all checks on this program. This program is the same as the one presented in the SPARK Tutorial.

longest_common_prefix

This program computes the length of the longest common prefix between two substrings of a common text. The postcondition of the main function LCP expresses this property. GNATprove proves all checks on this program. This program was proposed as a formal verification challenge during VerifyThis Verification Competition in 2012 (see http://fm2012.verifythis.org/).

pair_insertion_sort

This program performs a variant of insertion sort, that inserts in place two elements of an array at each loop iteration. This program was proposed as a formal verification challenge during VerifyThis Verification Competition in 2017 (see http://www.pm.inf.ethz.ch/verifythis.html). The postcondition of the main function Sort expresses both that the array is sorted on exit, and that it is a permutation of its input value. GNATprove proves all checks on this program. The
process to progress through all levels of software assurance with SPARK on this example is detailed in the following post on AdaCore blog: https://blog.adacore.com/verifythis-challenge-in-spark

**search_linked_list**

This program searches for a given value in an unordered linked list. The postcondition of the main function Search expresses that the search is successful if-and-only-if the list contains the value searched, and if so the cursor returned is one at which the list contains this value. GNATprove proves all checks on these programs.

**string_search**

This example contains multiple variants of substring search:

- a simple brute force search in Brute_Force and Brute_Force_Slice.
- a more efficient algorithm called quick search in QS.

The postcondition of all variants expresses that the search is successful if-and-only-if the string Haystack contains the substring Needle searched, and if so the index returned is one at which the string contains this substring. GNATprove proves all checks on these programs. A detailed account of the development and verification of this example is given in the following post on AdaCore blog: https://blog.adacore.com/applied-formal-logic-searching-in-strings

**trajectory_computation**

This example contains code from an embedded safety-critical software, which computes the speed of a device submitted to gravitational acceleration and drag from the atmosphere around it. This program was used as challenge example in the article “Automating the Verification of Floating-Point Programs” published at VSTTE 2017 conference.

The Ada files contain multiple variants of the example in increasing order of difficulty, see README file for details. The challenge example used in the article corresponds to files simple_trajectory.ads and simple_trajectory.adb. In this version, only the speed is updated, not the distance. Both absence of run-time errors (including overflows) and safe bounds on the computed speed are proved by using a combination of provers. A dozen intermediate assertions are needed to benefit from this combination, so that different provers can prove different parts of the property.

**7.10.2 Single Units**

These examples contain a single unit, and are usually small (a few hundreds slocs at most).

**adacore_u**

This folder contains the complete source code of the small examples used in the quiz of the SPARK 2014 course available from the AdaCore University website (at http://university.adacore.com/courses/spark-2014/). They include unannotated units, examples with formally verified data flow, functional, or abstraction contracts, as well as erroneous programs, on which GNATprove detects failing checks.

Opening the example in GNAT Studio or GNATbench opens an aggregate project, with separate sub-projects for each lecture.
allocators

This program demonstrates how the specification of a SPARK program can be formalized using an abstract model and how the refinement relation between the model and its implementation can be verified using GNATprove. It is described in the article “Abstract Software Specifications and Automatic Proof of Refinement” published at RSSRail 2016 conference (at http://blog.adacore.com/uploads/rssrail.pdf).

The example contains three versions of an allocator package. They are specified in terms of mathematical structures (sequences and sets). The refinement relation between the mathematical model and the implementation is expressed as a ghost function is_Valid and enforced through contracts. It can be verified automatically using GNATprove.

- **Simple_Allocator** features a naive implementation of the allocator, storing the status (available or allocated) of each resource in a big array. It is specified using a ghost function Model which always returns a valid refinement of the allocator’s data. The refinement relation is verified only once, as a postcondition of the Model function. The functional contracts on modifying procedures as well as the refinement relation are straightforward and can be verified easily at level 2 in a few seconds.

- **List_Allocator** introduces a free list to access more efficiently the first available resource. Here not every possible state of the allocator data can be refined into a valid model. To work around this problem, the model is stored in a global ghost variable which is updated along with the allocator’s data and the refinement relation is expressed as an invariant that must be verified as a postcondition of each modifying procedure. The functional contracts on modifying procedures are straightforward but the refinement relation is now more complicated, as it needs to account for the implementation of the free list. They can be verified at level 4 in less than one minute overall.

- **List_Mod_Allocator** features the same implementation and contracts as List_Allocator, but its model is returned by a ghost function like in Simple_Allocator instead of being stored in a global ghost variable. As not every possible state of the allocator can be refined into a valid model, the refinement relation is not expressed as a postcondition of Model, but as an invariant, as in List_Allocator and must be verified as a postcondition of each modifying procedure. The functional contracts and the refinement relation resemble those of List_Allocator. However, as we don’t construct explicitly the new model after each modification, the proof of the allocator’s functional contracts requires induction, which is beyond the reach of automatic solvers. The induction scheme is given here manually in an auto-active style through calls to ghost procedures. The whole program can then be verified automatically at level 4 in less than one minute overall on an 8-cores machine, or in a few minutes on a single core.

See the relevant sections for more details on Ghost Code and Manual Proof Using Ghost Code.

cartesian_trees

This program is a solution to the second challenge of VerifyThis 2019. For a sequence of distinct numbers $S$, the Cartesian tree of $S$ is the only binary tree $T$ such that $T$ contains a node per element of $S$, $T$ has the heap property, and symmetrical traversal of $T$ encounters elements in the order of $S$. The challenge is split in two parts, first construct all nearest smaller neighbors to the left/right of each element of a sequence using a stack, and then construct the Cartesian tree of the sequence using these neighbors.

Computation of the nearest smaller neighbors is fairly straightforward in SPARK. It still features a relatively involved loop invariant. On the other hand, showing that the tree constructed by the algorithm in the second part is the Cartesian tree of the input sequence is rather involved. It uses ghost code to manually guide automatic solvers (see Manual Proof Using Ghost Code).

database

This program implements a toy interface to a bank account database, with procedures to deposit and withdraw money, and functions to query the account balance and information. This program was used as running example in the
article “Integrating Formal Program Verification with Testing” (at http://www.adacore.com/uploads_gems/Hi-Lite_ERTS-2012.pdf). The API is annotated with full functional contracts, as well as test cases expressed with aspect Test_Case. GNATprove proves all checks on this program.

e-voting

This program implements a toy e-voting interface, to get candidates and votes from a file, compute the winner of the vote and print it. The API is annotated with functional contracts, some partial and some complete. GNATprove proves all checks on this program, except for initialization of an array initialized piecewise (known limitation of flow analysis) and an array access in a string returned by the standard library function Get_Line (which would require using a wrapper with contracts).

formal_queue

This program implements a queue of integers using a doubly linked list, with full functional contracts on the API of the queue. GNATprove proves all checks on this program.

ghc_sort

This program is a partial solution to the first challenge of VerifyThis 2019. It features a sorting algorithm, which works by splitting the input sequence into monotonic subsequences of maximal length. It then reverses the decreasing subsequences and merges them pairwise until the sequence is reconstructed.

Computation of the sequence of cuts is completely verified. On sorting algorithm, we only check that it returns a sorted sequence of the correct length. We did not attempt to prove that the result of the sort function is a permutation of its input. Indeed, this kind of property is complicated both to formalize and to verify, and generally requires ghost code (see Manual Proof Using Ghost Code).

This example does not feature the use of any interactive proof techniques, as proofs attempted were largely in reach of the automated tool. We used support for ownership pointers in SPARK to implement lists of subsequences as a recursive data-type using pointers. It is all proved except for termination of recursive functions used to iterate over the lists.

natural

This program implements an interface to manipulate sets of natural numbers, stored in an array. Contracts on the interface subprograms express partial correctness properties, for example that the set contains an element after it has been inserted. GNATprove proves all checks on this program.

nuclear_systems

This program implements a concurrent system to control a nuclear reactor, in which the state of the reactor is queried every few seconds, and the reactor is stopped if either its state is Uncontrolled, or if was not controlled in the previous two seconds (because not queried or because it did not answer). GNATprove proves all checks on this program. This program was presented as an idiomatic way to support selective delays in SPARK in a blog post on “Selective Delays in SPARK and Ravenscar” (see https://two-wrongs.com/selective-delay-in-spark-and-ravenscar.html).
**n_queens**

This program implements the solution to the N queens problem, to place N queens on an N x N chess board so that no queen can capture another one with a legal move. The API is annotated with full functional contracts. GNATprove proves all checks on this program. This program was proposed as a formal verification challenge during VSTTE Verification Competition in 2010 (see https://sites.google.com/a/vscomp.org/main/).

**patience**

This program implements the game of Patience Solitaire, taking cards one-by-one from a deck of cards and arranging them face up in a sequence of stacks. The invariant maintained when playing is a complex relation between multiple arrays storing the current state of the game. GNATprove proves all checks on this program, when using provers CVC4, Alt-Ergo and Z3. This program was proposed as a formal verification challenge during VSTTE Verification Competition in 2014 (see http://vscomp.org/).

**pointer_based_maps**

This program features a pointer-based implementation of a map as a singly-linked list of pairs. The example is described in a blog post (see https://blog.adacore.com:pointer-based-data-structures-in-spark). It explains how local borrowers and observers can be used to traverse a recursive data-structure, traversal functions, and how to use pledges to supply information about borrowed objects.

In addition to the subprograms presented in the blog post, the example also provides an extended version of Replace_Element. It is completely specified, using the Iterable aspect to allow quantification over keys included in a map.

**prime_numbers**

This program implements two functions Nearest_Number and Nearest_Prime_Number which respectively find the closest coprime number and prime number for a given argument value and a given searching mode among three possibilities: above the value only, below the value only, or both. The spec of both functions is expressed in a Contract_Cases aspect, and proved automatically with GNATprove. GNATprove also proves automatically the functional contract of Initialize_Coprime_List which initializes the list of coprimes for a given argument, using Euclid’s method, and returns this list to be used with Nearest_Number. The list of prime numbers is initialized at package elaboration using the sieve of Erathosthenes, a procedure which is currently not fully proved by GNATprove, due to the use of non-linear integer arithmetic and floating-point square root function.

This program offers a nice display of many SPARK features in a simple setting:

- State Abstraction
- Subprogram Contracts
- Specification Features
- Loop Invariants
- Ghost Code

The original code was contributed by Guillaume Foliard.
**red_black_trees**

This example demonstrates *Type Invariants* and *Manual Proof Using Ghost Code* on an implementation of red black trees. It features a minimalist library of trees providing only membership test and insertion. The complexity of this example lies in the invariants that are maintained on the data-structure. Namely, it implements a balanced binary search tree, balancing being enforced by red black coloring.

The implementation is divided in three layers, each concerned with only a part of the global data structure invariant. The first package, named `Binary_Trees`, is only concerned with the tree structure, whereas `Search_Trees` imposes ordering properties and `Red_Black_Trees` enforces balancing. At each level, the relevant properties are expressed using a *Type Invariant*. It allows to show each independent invariant at the boundary of its layer, assuming that it holds when working on upper layers.

The example features several particularities which make it complex beyond purely automated reasoning. First, the tree structure is encoded using references in an array, which makes it difficult to reason about disjointness of different branches of a tree. Then, reasoning about reachability in the tree structure requires induction, which is often out of the reach of automatic solvers. Finally, reasoning about value ordering is also a pain point for automatic solvers, as it requires coming up with intermediate values on which to apply transitivity.

To achieve full functional verification of this example, it resorts to manually helping automatic solvers using auto-active techniques. For example, ghost procedures are used to introduce intermediate lemmas, loop invariants are written to achieve inductive proofs, and assertions are introduced to provide new values to be used for transitivity relations.


**railway_signaling**

This program implements a simple signaling algorithm to avoid collision of trains. The main procedure `Move` moving a given train along the railroad should preserve the collision-free property `One_Train_At_Most_Per_Track` and the correctness of signaling `Safe_Signaling`, namely that:

- tracks that are occupied by a train are signalled in red, and
- tracks that precede an occupied track are signalled in orange.

As the algorithm in `Move` relies on the correctness of the signaling, the preservation of the collision-free property depends also on the correctness of the signaling. *Pragma Assume* is used to express an essential property of the railroad on which correctness depends, namely that no track precedes itself. GNATprove proves all checks on this program, when using provers CVC4, Alt-Ergo and Z3.

**ring_buffer**

This program implements a ring buffer stored in an array of fixed size, with partial contracts on the API of the ring buffer. GNATprove proves all checks on this program. This program was proposed as a formal verification challenge during VSTTE Verification Competition in 2012 (see https://sites.google.com/site/vstte2012/compet).

**segway**

This program implements a state machine controlling a segway states. The global invariant maintained across states is expressed in an expression function called from preconditions and postconditions. GNATprove proves all checks on this program.
This collection of examples comes from the book *Building High Integrity Applications with SPARK* written by Prof. John McCormick from University of Northern Iowa and Prof. Peter Chapin from Vermont Technical College, published by Cambridge University Press:

The examples follow the chapters of the book:

1. Introduction and overview
2. The basic SPARK language
3. Programming in the large
4. Dependency contracts
5. Mathematical background
6. Proof
7. Interfacing with SPARK
8. Software engineering with SPARK
9. Advanced techniques

Opening the example in GNAT Studio or GNATbench opens a project with all sources. Projects corresponding to individual chapters are available in subdirectories and can be opened manually.

The original source code is available from the publisher’s website at http://www.cambridge.org/us/academic/subjects/computer-science/programming-languages-and-applied-logic/building-high-integrity-applications-spark
stopwatch

This program implements a stopwatch, and is an example of how concurrent programs are verified in SPARK. A user can push buttons to start, stop and reset the clock. The clock has a display to show the elapsed time. This example uses protected objects and tasks.

GNATprove proves all checks on this program, including the safe usage of concurrency.

tagged_stacks

This example features an abstract view of a stack, represented as an abstract tagged type with abstract primitives, as well as two concrete stack implementations deriving from this abstract root. A procedure Test_Stack defined on any object of the type hierarchy uses dispatching to test any concrete stack implementation.

Note that in this example, LSP checks (see Object Oriented Programming and Liskov Substitution Principle) are trivial as no contracts are supplied on overriding subprograms. The differences of behaviors between the two concrete implementations are all accounted for through calls to primitive functions in the classwide contracts.

Also note that we did not provide any loop invariants on the loops of Test_Stack. Instead we rely on Automatic Unrolling of Simple For-Loops to verify the procedure.

GNATprove proves all checks on this program.

tetris

This program implements a simple version of the game of Tetris. An invariant of the game is stated in function Valid_Configuration, that all procedures of the unit must maintain. This invariant depends on the state of the game which if updated by every procedure. Both the invariant and the state of the game are encoded as Ghost Code.

The invariant expresses two properties:

1. A falling piece never exits the game board, and it does not overlap with pieces that have already fallen.
2. After a piece has fallen, the complete lines it may create are removed from the game board.

GNATprove proves all checks on the full version of this program found in tetris_functional.adb. Intermediate versions of the program show the initial code without any contracts in tetris_initial.adb, the code with contracts for data dependencies in tetris_flow.adb and the code with contracts to guard against run-time errors in tetris_integrity.adb. The complete program, including the BSP to run it on the ATMEL SAM4S board, is available online (see http://blog.adacore.com/tetris-in-spark-on-arm-cortex-m4).

tictactoe

This program implements a game of tic-tac-toe. A human player and the computer take turns. Subprograms Player_Play and Computer_Play in tictactoe.ads have partial contracts stating that the number of free slots decreases by one after each play.

GNATprove proves all absence of run-time errors on this program, and that the subprogram contracts are correctly implemented. Interestingly, no loop invariants are needed, although the program contains many loops, thanks to the use of Automatic Unrolling of Simple For-Loops in GNATprove.

traffic_light

This program implements two small simulators of traffic lights:
• **Unit Road_Traffic** defines safety rules for operating traffic lights over a crossroads. All procedures that change the state of the lights must maintain the safety property.

• **Unit Traffic_Lights** defines a concurrent program for operating traffic lights at a pedestrian crossing, using two tasks that communicate over a protected object, where the invariant maintained by the protected data is expressed using a subtype predicate.

GNATprove proves all checks on this program, including the safe usage of concurrency (absence of data races, absence of deadlocks).

### 7.10.3 Multi-Units Demos

These examples contain larger demo programs (of a few hundreds or thousands slocs).

**autopilot**

This program was originally a case study written in SPARK 2005 by John Barnes, presented in section 14.3 of his book “High Integrity Software, The SPARK Approach to Safety and Security” (2003) and section 15.1 of the updated book “SPARK: The Proven Approach to High Integrity Software” (2012). For details on this case study, see one of the above books. The program in the toolset distribution is the SPARK 2014 version of this case study.

The program considers the control system of an autopilot controlling both altitude and heading of an aircraft. The altitude is controlled by manipulating the elevators and the heading is controlled by manipulating the ailerons and rudder.

The values given by instruments are modelled as **External State Abstraction** with asynchronous writers (the sensors) in package **Instruments**. The states of controllers are modelled as a **State Abstraction** called **State** in package **AP**, which is successively refined into finer-grain abstractions in the child packages of **AP** (for example **AP.Altitude** and **AP.Altitude.Pitch**). The actions on the mobile surfaces of the plane are modelled as **External State Abstraction** with asynchronous readers (the actuators) in package **Surfaces**.

Data and flow dependency contracts are given for all subprograms. GNATprove proves all checks on this program, except for 4 runtime checks related to scaling quantities using a division (a known limitation of automatic provers).

**bitwalker**

This program was originally a case study in C from Siemens rewritten by the Fraunhofer FOKUS research group for applying the Frama-C formal verification tool to it. It was later on rewritten in SPARK and formally proved correct with GNATprove (with 100% of checks automatically proved). This work is described in the article “Specification and Proof of High-Level Functional Properties of Bit-Level Programs” published at NFM 2016 conference (at https://hal.inria.fr/hal-01314876).

This program introduces a function and procedure that read and respectively write a word of bits of a given length from a stream of bytes at a given position. It heavily uses bitwise arithmetic and is fully specified with contracts and automatically proved by GNATprove. In addition, two test procedures call read-then-write and write-then-read and GNATprove is able to prove the expected properties on the interplay between reading and writing.

In this program we use an external axiomatization in order to lift some operators from the underlying Why3 theory of bitvectors to SPARK. In particular the **Nth** function, at the core of the specification of the program, lets us check if a specific bit in a modular value is set or not. Note that while such a function could be easily implemented in SPARK, using the one defined in the Why3 theory leads to more automatic proofs because it lets the provers use the associated axioms and lemmas.
crazyflie

This program is a translation of the stabilization system of the Crazyflie 2.0, a tiny drone released by Bitcraze AB in 2013 and originally based on an open-source firmware written in C.

This SPARK code interfaces with the other parts of the firmware (ST peripheral libraries, FreeRTOS libraries, Crazyflie sensors and actuators), which remained in C, by using Ada capabilities for multi-language programs.

The goal was to prove absence of runtime errors on the most critical code parts of the drone’s firmware. The techniques used to achieve this aim were presented in a post on the AdaCore Blog: http://blog.adacore.com/how-to-prevent-drone-crashes-using-spark

Data dependency contracts are given for most subprograms, specially in the Stabilizer_Pack package which uses State Abstraction to specify this type of contracts.

heatingsystem

This program is a standard example of controller, turning on and off the heating depending on the value of the current temperature read by a thermostat and the current mode of operation. Interfaces to the physical world are modelled as External State Abstraction for sensors and actuators. Data and flow dependency contracts are given for all subprograms. GNATprove proves all checks on this program.

ipstack

This program is an implementation of a TCP/IP stack targeted at bare-board embedded applications in certifiable systems. The API is an event driven architecture (based on LWIP design), with an application interface based on callbacks. The protocols supported are:

- IPv4
- ARP
- UDP
- TCP
- ICMP

This TCP/IP stack can be used either on a PowerPC bare-board system or on a Linux host as a native process. In the latter case, the TAP device is used for communication between the stack and the host system. For more details, see the corresponding README file.

Data dependency contracts are given for most subprograms. These contracts are proved by GNATprove flow analysis, which also proves the absence of reads of uninitialized data.

openETCS

This program is a case study performed by David Mentré in the context of the openETCS European project aiming at making an open-source, open-proof reference model of ETCS (European Train Control System). ETCS is a radio-based train control system aiming at unifying train signaling and control over all European countries. The results of this case study are described in the article “Rail, Space, Security: Three Case Studies for SPARK 2014”.

Package Section_4_6 models a subset of the transitions allowed in the overall state automaton that the system should follow. Guards for transitions are expressed by using Expression Functions, and the disjointness of these guards is expressed by using Contract Cases. GNATprove proves all checks on this part of the program.
Package **Step_Function** implements piecewise constant functions used to model for example speed restrictions against distance. Full functional contracts are given for all the services of this package. GNATprove proves all checks on this part of the program, except the more complex postcondition of procedure **Restrictive_Merge**.

**sparkskein**

This program is an implementation of the Skein cryptographic hash algorithm (see [http://www.skein-hash.info/](http://www.skein-hash.info/)). This implementation is readable, completely portable to a wide-variety of machines of differing word-sizes and endianness. This program was originally written in SPARK 2005 by Rod Chapman as a case study for the applicability of SPARK to cryptographic code. For details on this case study, see the article “**SPARKSkein: A Formal and Fast Reference Implementation of Skein**” (at [http://www.adacore.com/knowledge/technical-papers/sparkskein/](http://www.adacore.com/knowledge/technical-papers/sparkskein/)). The program in the toolset distribution is the SPARK 2014 version of this case study.

Compared to the original version written for the previous generation of the SPARK toolset, this version requires much less work to obtain complete assurance of the absence of run-time errors. In the following, we call a **precondition element** a conjunct in a precondition, **postcondition element** a conjunct in a postcondition and **loop invariant element** a conjunct in a loop invariant. The number of such elements in a verified program is directly related (usually proportional) to the verification effort, as each such element requires the user to write it, to debug it, and finally to prove it.

- Contrary to GNATprove, the previous toolset did not include **Generation of Dependency Contracts**. This required writing 17 non-trivial global contracts and 24 non-trivial derives contracts. With GNATprove, no data dependency or flow dependency is needed at all. We have kept 17 trivial null data dependency contracts and a single non-trivial data dependency contract for documentation purposes. Similarly, we have kept 11 trivial null flow dependency contracts for documentation purposes.

- SPARK naturally supports nesting of subprograms, which allows a natural top-down decomposition of the main operations into local procedures. This decomposition aids readability and has a negligible impact on performance, assuming the compiler is able to inline the local procedures, but it previously had a very costly impact on formal verification. The previous toolset required the user to write functional contracts on all local subprograms to be able to prove absence of run-time errors in these subprograms. On the contrary, GNATprove performs **Contextual Analysis of Subprograms Without Contracts**, which allows us to save the effort of writing 19 precondition elements and 12 postcondition elements that were needed in the original version.

- The previous toolset required the insertion of lengthy **Loop Invariants**, totalling 43 loop invariant elements (some of them quite complex), while GNATprove currently requires only 1 simple loop invariant stating which components of a record are not modified in the loop. This is partly due to GNATprove now being able to generate loop invariants for unmodified record components (see **Automatically Generated Loop Invariants**).

- The previous toolset generated a logical formula to prove for each path leading to a run-time check or an assertion. This lead to the generation of 367 formulas overall on the original version, almost 5 times more than the 78 checks generated by GNATprove on the new version. This difference is impressive, given that everything was done in the original version to control the explosion of the number of formulas, with the insertion of 24 special annotations in the source code similar to **Pragma Assert_And_Cut** in SPARK 2014, while no such work was needed in the new version. Despite this and other differences in efficiency between the two toolsets, the analysis time to ensure complete absence of run-time errors is similar between the two toolsets: 5 min with the previous toolset, half of that with GNATprove.

- Out of the 367 generated formulas, 29 were not proved automatically with the previous toolset: 6 formulas required the insertion of user-defined lemmas in the theorem prover, and 23 formulas required manual proof in a proof assistant. With GNATprove and provers CVC4, Z3 and Alt-Ergo, all checks are proved automatically.
**spark_io**

This program is an example wrapping of Ada standard input output library in a SPARK compatible library interface. For example, the standard unit Ada.Text_IO is wrapped in a unit called SPARK.Text_IO that provides the same services, but uses normal control flow to signal errors instead of exceptions. A type File_Status describes either a normal status for a file (Unopened or Success) or an error status (Status_Error, Mode_Error, etc.). The standard type for a file Ada.Text_IO.File_Type is wrapped into a record type SPARK.Text_IO_File_Type together with the status described above.

Wrapper units are also given for most children of the Ada standard input output library Ada.Text_IO, for example the generic unit SPARK.Text_IO.Integer_IO wraps the services of the standard unit Ada.Text_IO.Integer_IO. Partial function contracts are expressed on all subprograms. GNATprove proves all checks on the implementation of these wrapper units.

**text_io_get_line**

This program is a simplified extracted version of the standard library function Ada.Text_IO.Get_Line, which reads a line of text from an input file. The various versions of Ada.Text_IO.Get_Line (procedures and functions) are specified with respect to a simplified model of the file system, with a single file The_File opened at a location Cur_Location. The low-level functions providing an efficient implementation (fgets, memcpy, etc.) are also specified with respect to the same model of the file system.

GNATprove proves automatically that the code is free of run-time errors (apart from a few messages that are either intentional or related to the ghost code instrumentation) and that subprogram bodies respect their functional contracts. The story behind this work was presented in a post on the AdaCore Blog: [http://blog.adacore.com/formal-verification-of-legacy-code](http://blog.adacore.com/formal-verification-of-legacy-code)

**thumper**

This program is a secure time stamp client/server system that implements RFC-3161 (see [https://www.ietf.org/rfc/rfc3161.txt](https://www.ietf.org/rfc/rfc3161.txt)). It allows clients to obtain cryptographic time stamps that can be used to later verify that certain documents existed on or before the time mentioned in the time stamp. Thumper is written in a combination of Ada 2012 and SPARK 2014 and makes use of an external C library. Thumper was developed as a SPARK technology demonstration by Prof. Peter Chapin from Vermont Technical College and his students. It is used as a case study in the book *Building High Integrity Applications with SPARK* written by Prof. John McCormick from University of Northern Iowa and Prof. Peter Chapin, published by Cambridge University Press (see section 8.5).

The program in the toolset distribution is a snapshot of the Thumper project and a supporting project providing ASN.1 support named Hermes, whose up-to-date sources can be obtained separately from GitHub:

- Thumper at [https://github.com/pchapin/thumper](https://github.com/pchapin/thumper)
- Hermer at [https://github.com/pchapin/hermes](https://github.com/pchapin/hermes)

The verification objectives pursued in both projects are currently to *Address Data and Control Coupling* with a focus on ensuring secure information flows (especially important for a cryptographic application) and to *Prove Absence of Run-Time Errors (AoRTE)*.

**tokeneer**

This program is a highly secure biometric software system that was originally developed by Altran. The system provides protection to secure information held on a network of workstations situated in a physically secure enclave. The Tokeneer project was commissioned by the US National Security Agency (NSA) to demonstrate the feasibility of developing systems to the level of rigor required by the higher assurance levels of the Common Criteria. The
The program in the toolset distribution is a translation of the original Tokeneer code into SPARK 2014. The core system now consists of approximately 10,000 lines of SPARK 2014 code. There are also approximately 3,700 lines of supporting code written in Ada which mimic the drivers to peripherals connected to the core system.

Requirements of the system were captured using the Z notation and the implementation was in SPARK 2005. The original development artifacts, including all source code, are publicly available (see http://www.adacore.com/sparkpro/tokeneer).

Data and flow dependency contracts are given for all subprograms. Partial functional contracts are also given for a subset of subprograms. GNATprove currently proves automatically all checks on SPARK code in Tokeneer. The transition from SPARK 2005 to SPARK 2014 was presented in a post on the AdaCore Blog: https://blog.adacore.com/tokeneer-fully-verified-with-spark-2014

Tokeneer can be used as the basis for demonstrating four types of security vulnerabilities that can be detected by GNATprove, when calling GNAT Studio with -XSECURITY_DEMO=True (or changing the value of the scenario variable in GNAT Studio). Analyzing the code in that setting detects:

- an information leak in keystore.adb
- a back door in bio.adb
- a buffer overflow in admintoken.adb
- an implementation flaw in alarm.adb
APPLYING SPARK IN PRACTICE

SPARK tools offer different levels of analysis, which are relevant in different contexts. This section starts with a description of the main Objectives of Using SPARK. This list gathers the most commonly found reasons for adopting SPARK in industrial projects, but it is not intended to be an exhaustive list.

Whatever the objective(s) of using SPARK, any project fits in one of four possible Project Scenarios:

- the brown field scenario: Maintenance and Evolution of Existing Ada Software
- the green field scenario: New Developments in SPARK
- the migration scenario: Conversion of Existing SPARK Software to SPARK 2014
- the frozen scenario: Analysis of Frozen Ada Software

The end of this section examines each of these scenarios in turn and describes how SPARK can be applied in each case.

8.1 Objectives of Using SPARK

8.1.1 Safe Coding Standard for Critical Software

SPARK is a subset of Ada meant for formal verification, by excluding features that are difficult or impossible to analyze automatically. This means that SPARK can also be used as a coding standard to restrict the set of features used in critical software. As a safe coding standard checker, SPARK allows both to prevent the introduction of errors by excluding unsafe Ada features, and it facilitates their early detection with GNATprove’s flow analysis.

Exclusion of Unsafe Ada Features

Once the simple task of Identifying SPARK Code has been completed, one can use GNATprove in check mode to verify that SPARK restrictions are respected in SPARK code. Here we list some of the most error-prone Ada features that are excluded from SPARK (see Excluded Ada Features for the complete list).

- All expressions, including function calls, are free of side-effects. Expressions with side-effects are problematic because they hide interactions that occur in the code, in the sense that a computation will not only produce a value but also modify some hidden state in the program. In the worst case, they may even introduce interferences between subexpressions of a common expression, which results in different executions depending on the order of evaluation of subexpressions chosen by the compiler.

- Handling of exceptions is not permitted. Exception handling can create complex and invisible control flows in a program, which increases the likelihood of introducing errors during maintenance. What is more, when an exception is raised, subprograms that are terminated abnormally leave their variables in a possibly uninitialized or inconsistent state, in which data invariants may be broken. This includes values of out parameters, which
additionally are not copied back when passed by copy, thus introducing a dependency on the parameter mode chosen by the compiler.

- The use of access types and allocators is not permitted. Pointers can introduce aliasing, that is, they can allow the same object to be visible through different names at the same program point. This makes it difficult to reason about a program as modifying the object under one of the names will also modify the other names. What is more, access types come with their own load of common mistakes, like double frees and dangling pointers.

- SPARK also prevents dependencies on the elaboration order by ensuring that no package can write into variables declared in other packages during its elaboration. The use of controlled types is also forbidden as they lead to insertions of implicit calls by the compiler. Finally, backward goto statements are not permitted as they obfuscate the control flow.

**Early Detection of Errors**

GNATprove’s flow analysis will find all the occurrences of the following errors:

- uses of uninitialized variables (see *Data Initialization Policy*)
- aliasing of parameters that can cause interferences, which are often not accounted for by programmers (see *Absence of Interferences*)

It will also warn systematically about the following suspicious behaviors:

- wrong parameter modes (can hurt readability and maintainability or even be the sign of a bug, for example if the programmer forgot to update a parameter, to read the value of an out parameter, or to use the initial value of a parameter)
- unused variables or statements (again, can hurt readability and maintainability or even be the sign of a bug)

**8.1.2 Prove Absence of Run-Time Errors (AoRTE)**

**With Proof Only**

GNATprove can be used to prove the complete absence of possible run-time errors corresponding to:

- all possible explicit raising of exceptions in the program,
- raising exception *Constraint_Error* at run time, and
- all possible failures of assertions corresponding to raising exception *Assert_Error* at run time.

AoRTE is important for ensuring safety in all possible operational conditions for safety-critical software (including boundary conditions, or abnormal conditions) or for ensuring availability of a service (absence of DOS attack that can crash the software).

When run-time checks are enabled during execution, Ada programs are not vulnerable to the kind of attacks like buffer overflows that plague programs in C and C++, which allow attackers to gain control over the system. But in the case where run-time checks are disabled (in general for efficiency, but it could be for other reasons), proving their absence with GNATprove also prevents such attacks. This is specially important for ensuring security when some inputs may have been crafted by an attacker.

Few subprogram contracts (*Preconditions* and *Postconditions*) are needed in general to prove AoRTE, far fewer than for proving functional properties. Even fewer subprogram contracts are needed if types are suitably constrained with *Type Contracts*. Typically, 95% to 98% of run-time checks can be proved automatically, and the remaining checks can be either verified with manual provers or justified by manual analysis.
GNATprove supports this type of combination of results in the summary table of *The Analysis Results Summary File*. Multiple columns display the number of checks automatically verified, while the column *Justified* displays the number of checks manually justified. The column *Unproved* should be empty for all checks to be verified.

**With a Combination of Proof and Test**

It is not always possible to achieve 100% proof of AoRTE, for multiple reasons:

1. Formal verification is only applicable to the part of the program that is in SPARK. If the program includes parts in Ada that are not in SPARK, for example, then it is not possible to prove AoRTE on those parts.
2. Some run-time checks may not be proved automatically due to prover shortcomings (see *Investigating Prover Shortcomings* for details).
3. It may not be cost-effective to add the required contracts for proving AoRTE in a less critical part of the code, compared to using testing as a means of verification.

For all these reasons, it is important to be able to combine the results of formal verification and testing on different parts of a codebase. Formal verification works by making some assumptions, and these assumptions should be shown to hold even when formal verification and testing are combined. Certainly, formal verification cannot guarantee the same properties when part of a program is only tested, as when all of a program is proved. The goal then, when combining formal verification and testing, is to reach a level of confidence as good as the level reached by testing alone.

**At the Level of Individual Run-Time Checks**

One way to get confidence that unproved run-time checks cannot fail during execution is to exercise them during testing. Test coverage information allows guaranteeing a set of run-time checks have been executed successfully during a test run. This coverage information may be gathered from the execution of a unit testing campaign, an integration testing campaign, or the execution of a dedicated testsuite focussing on exercising the run-time checks (for example on boundary values or random ones).

This strategy is already applied in other static analysis tools, for example in the integration between the CodePeer static analyzer and the VectorCAST testing tool for Ada programs.

**Between Proof and Integration Testing**

Contracts can also be exercised dynamically during integration testing. In cases where unit testing is not required (either because proof has been applied to all subprograms, or because the verification context allows it), exercising contracts during integration testing can complement proof results, by giving the assurance that the actual compiled program behaves as expected.

This strategy has been applied at Altran on UK military projects submitted to Def Stan 00-56 certification: AoRTE was proved on all the code, and contracts were exercised during integration testing, which allowed to scrap unit testing.

**Between Proof and Unit Testing**

Contracts on subprograms provide a natural boundary for combining proof and test:

- If proof is used to demonstrate that a subprogram is free of run-time errors and respects its contract, this proof depends on the precondition of the subprogram being respected at the call site. This verification can be achieved by proving the caller too, or by checking dynamically the precondition of the called subprogram during unit testing of the caller.
• If proof is used to demonstrate that a subprogram is free of run-time errors and respects its contract, and this subprogram calls other subprograms, this proof depends on the postconditions of the called subprogram being respected at call sites. This verification can be achieved by proving the callees too, or by checking dynamically the postcondition of the called subprograms during their unit testing.

Thus, it is possible to combine freely subprograms that are proved and subprograms that are unit tested, provided subprogram contracts (Preconditions and Postconditions) are exercised during unit testing. This can be achieved by compiling the program with assertions for testing (for example with switch -gnata in GNAT), or by using GNATtest to create the test harness (see section 7.10.12 of GNAT User’s Guide on Testing with Contracts).

When combining proof and test on individual subprograms, one should make sure that the assumptions made for proof are justified at the boundary between proved subprograms and tested subprograms (see section on Managing Assumptions). To help with this verification, special switches are defined in GNAT to add run-time checks that verify dynamically the assumptions made during proof:

- -gnateA adds checks that parameters are not aliased
- -gnateV adds checks that parameters are valid, including parameters of composite types (arrays, records)
- -gnatVa adds checks that objects are valid at more places than -gnateV, but only for scalar objects

This strategy is particularly well suited in the context of the DO-178C certification standard in avionics, which explicitly allows proof or test to be used as verification means on each module.

### 8.1.3 Prove Correct Integration Between Components

#### In New Developments

GNATprove can be used to prove correct integration between components, where a component could be a subprogram, a unit or a set of units. Indeed, even if components are verified individually (for example by proof or test or a combination thereof), their combination may still fail because of unforeseen interactions or design problems.

SPARK is ideally equipped to support such analysis, with its detailed Subprogram Contracts:

- With Data Dependencies, a user can specify exactly the input and output data of a subprogram, which goes a long way towards uncovering unforeseen interactions.
- With functional contracts (Preconditions and Postconditions), a user can specify precisely properties about the behavior of the subprogram that are relevant for component integration. In general, simple contracts are needed for component integration, which means that they are easy to write and to verify automatically. See section on Writing Contracts for Program Integrity for examples of such contracts.

When using data dependencies, GNATprove's flow analysis is sufficient to check correct integration between components. When using functional contracts, GNATprove's proof should also be applied.

#### In Replacement of Comments

It is good practice to specify properties of a subprogram that are important for integration in the comments that are attached to the subprogram declaration.

Comments can be advantageously replaced by contracts:

- Comments about the domain of the subprogram can be replaced by Preconditions.
- Comments about the effects of the subprogram can be replaced by Postconditions and Data Dependencies.
- Comments about the result of functions can be replaced by Postconditions.
- GNATprove can use the contracts to prove correct integration between components, as in new developments.
Contracts are less ambiguous than comments, and can be accompanied by (or interspersed with) higher level comments that need not be focused on the finer grain details of which variables must have which values, as these are already specified concisely and precisely in the contracts.

**In Replacement of Defensive Coding**

In existing Ada code that is migrated to SPARK, defensive coding is typically used to verify the correct integration between components: checks are made at the start of a subprogram that inputs (parameters and global variables) satisfy expected properties, and an exception is raised or the program halted if an unexpected situation is found.

Defensive code can be advantageously replaced by preconditions:

- The dynamic checks performed by defensive code at run time can be performed equally by preconditions, and they can be enabled at a much finer grain thanks to **Pragma Assertion_Policy**.
- GNATprove can use the preconditions to prove correct integration between components, as in new developments.

**8.1.4 Prove Functional Correctness**

**In New Developments**

GNATprove can be used to prove functional correctness of an implementation against its specification. This strongest level of verification can be applied either to specific subprograms, or specific units, or the complete program. For those subprograms whose functional correctness is to be checked, the user should:

1. express the specification of the subprogram as a subprogram contract (see **Preconditions** and **Postconditions**);
2. use GNATprove to prove automatically that most checks (including contracts) always hold; and
3. address the remaining unproved checks with manual justifications or testing, as already discussed in the section on how to **Prove Absence of Run-Time Errors (AoRTE)**.

As more complex contracts are required in general, it is expected that achieving that strongest level of verification is also more costly than proving absence of run-time errors. Typically, SPARK features like **Quantified Expressions** and **Expression Functions** are needed to express the specification, and features like **Loop Invariants** are needed to achieve automatic proof. See section on **Writing Contracts for Functional Correctness** for examples of such contracts, and section on **How to Write Loop Invariants** for examples of the required loop invariants.

When the functional specification is expressed as a set of disjoint cases, the SPARK feature of **Contract Cases** can be used to increase readability and to provide an automatic means to verify that cases indeed define a partitioning of the possible operational contexts.

**In Replacement of Unit Testing**

In existing Ada code that is migrated to SPARK, unit testing is typically used to verify functional correctness: actual outputs obtained when calling the subprogram are compared to expected outputs for given inputs. A **test case** defines an expected behavior to verify; a **test procedure** implements a **test case** with specific given inputs and expected outputs.

Test cases can be used as a basis for functional contracts, as they define in general a behavior for a set of similar inputs. Thus, a set of test cases can be transformed into **Contract Cases**, where each case corresponds to a test case: the test input constraint becomes the guard of the corresponding case, while the test output constraint becomes the consequence of the corresponding case.

GNATprove can be used to prove this initial functional contract, as in new developments. Then, cases can be progressively generalized (by relaxing the conditions in the guards), or new cases added to the contract, until the full functional behavior of the subprogram is specified and proved.
8.1.5 Ensure Correct Behavior of Parameterized Software

In some domains (railway, space), it is common to develop software which depends on parameterization data, which changes from mission to mission. For example, the layout of railroads or the characteristics of the payload for a spacecraft are mission specific, but in general do not require developing completely new software for the mission. Instead, the software may either depend on data definition units which are subject to changes between missions, or the software may load at starting time (possibly during elaboration in Ada) the data which defines the characteristics of the mission. Then, the issue is that a verification performed on a specific version of the software (for a given parameterization) is not necessarily valid for all versions of the software. In general, this means that verification has to be performed again for each new version of the software, which can be costly.

SPARK provides a better solution to ensure correct behavior of the software for all possible parameterizations. It requires defining a getter function for every variable or constant in the program that represents an element of parameterization, and calling this getter function instead of reading the variable or constant directly. Because GNATprove performs an analysis based on contracts, all that is known at analysis time about the value returned by a getter function is what is available from its signature and contract. Typically, one may want to use Scalar Ranges or Predicates to constrain the return subtype of such getter functions, to reflect the operational constraints respected by all parameterizations.

This technique ensures that the results of applying GNATprove are valid not only for the version of the software analyzed, but for any other version that satisfies the same operational constraints. This is valid whatever the objective(s) pursued with the use of SPARK: Prove Absence of Run-Time Errors (AoRTE), Prove Correct Integration Between Components, Prove Functional Correctness, etc.

It may be the case that changing constants into functions makes the code illegal because the constants were used in representation clauses that require static values. In that case, compilation switch -gnatI should be specified when analyzing the modified code with GNATprove, so that representation clauses are ignored. As representation clauses have no effect on GNATprove’s analysis, and their validity is checked by GNAT when compiling the original code, the formal verification results are valid for the original code.

For constants of a non-scalar type (for example, constants of record or array type), an alternative way to obtain a similar result as the getter function is to define the constant as a deferred constant, whose initial declaration in the visible part of a package spec does not specify the value of the constant. Then, the private part of the package spec which defines the completion of the deferred constant must be marked SPARK_Mode => Off, so that clients of the package only see the visible constant declaration without value. In such a case, the analysis of client units with GNATprove is valid for all possible values of the constant.

8.1.6 Safe Optimization of Run-Time Checks

Enabling run-time checks in a program usually increases the running time by around 10%. This may not fit the timing schedule in some highly constrained applications. In some cases where a piece of code is called a large number of times (for example in a loop), enabling run-time checks on that piece of code may increase the running time by far more than 10%. Thus, it may be tempting to remove run-time checking in the complete program (with compilation switch -gnatp) or a selected piece of code (with pragma Suppress), for the purpose of decreasing running time. The problem with that approach is that the program is not protected anymore against programming mistakes (for safety) or attackers (for security).

GNATprove provides a better solution, by allowing users to prove the absence of all run-time errors (or run-time errors of a specific kind, for example overflow checks) in a piece of code, provided the precondition of the enclosing subprogram is respected. Then, all run-time checks (or run-time errors of a specific kind) can be suppressed in that piece of code using pragma Suppress, knowing that they will never fail at run time, provided the precondition of the enclosing subprogram is checked (for example by using Pragma Assertion_Policy). By replacing many checks with one check, we can decrease the running time of the application by doing safe and controlled optimization of run-time checks.
8.1.7 Address Data and Control Coupling

As defined in the avionics standard DO-178, data coupling is “The dependence of a software component on data not exclusively under the control of that software component” and control coupling is “The manner or degree by which one software component influences the execution of another software component”, where a software component could be a subprogram, a unit or a set of units.

Although analysis of data and control coupling are not performed at the same level of details in non-critical domains, knowledge of data and control coupling is important to assess impact of code changes. In particular, it may be critical for security that some secret data does not leak publicly, which can be rephrased as saying that only the specified data dependencies are allowed. SPARK is ideally equipped to support such analysis, with its detailed Subprogram Contracts:

- With Data Dependencies, a user can specify exactly the input and output data of a subprogram, which identifies the “data not exclusively under the control of that software component”:
  - When taking the subprogram as component, any variable in the data dependencies is in general not exclusively under the control of that software component.
  - When taking the unit (or sets of units) as component, any variable in the data dependencies that is not defined in the unit itself (or the set of units) is in general not exclusively under the control of that software component.

- With Flow Dependencies, a user can specify the nature of the “dependence of a software component on data not exclusively under the control of that software component”, by identifying how that data may influence specific outputs of a subprogram.

- With Flow Dependencies, a user can also specify how “one software component influences the execution of another software component”, by identifying the shared data potentially written by the subprogram.

- With functional contracts (Preconditions and Postconditions), a user can specify very precisely the behavior of the subprogram, which defines how it “influences the execution of another software component”. These contracts need not be complete, for example they could describe the precedence order rules for calling various subprograms.

When using data and flow dependencies, GNATprove’s flow analysis is sufficient to check that the program implements its specifications. When using functional contracts, GNATprove’s proof should also be applied.

8.1.8 Ensure Portability of Programs

Using SPARK enhances portability of programs by excluding language features that are known to cause portability problems, and by making it possible to obtain guarantees that specific portability problems cannot occur. In particular, analyses of SPARK code can prove the absence of run-time errors in the program, and that specified functional properties always hold.

Still, porting a SPARK program written for a given compiler and target to another compiler and/or target may require changes in the program. As SPARK is a subset of Ada, and because in general only some parts of a complete program are in SPARK, we need to consider first the issue of portability in the context of Ada, and then specialize it in the context of SPARK.

Note that we consider here portability in its strictest sense, whereby a program is portable if its observable behavior is exactly the same across a change of compiler and/or target. In the more common sense of the word, a program is portable if it can be reused without modification on a different target, or when changing compiler. That is consistent with the definition of portability in WikiPedia: “Portability in high-level computer programming is the usability of the same software in different environments”. As an example of a difference between both interpretations, many algorithms which use trigonometry are portable in the more common sense, not in the strictest sense.
Portability of Ada Programs

Programs with errors cause additional portability issues not seen in programs without errors, which is why we consider them separately.

Portability of Programs Without Errors

The Ada Reference Manual defines precisely which features of the language depend on choices made by the compiler (see Ada RM 1.1.3 “Conformity of an Implementation with the Standard”):

- **Implementation defined behavior** - The set of possible behaviors is specified in the language, and the particular behavior chosen in a compiler should be documented. An example of implementation defined behavior is the size of predefined integer types (like `Integer`). All implementation defined behaviors are listed in Ada RM M.2, and GNAT documents its implementation for each of these points in section 7 “Implementation Defined Characteristics” of the GNAT Reference Manual.

- **Unspecified behavior** - The set of possible behaviors is specified in the language, but the particular behavior chosen in a compiler need not be documented. An example of unspecified behavior is the order of evaluation of arguments in a subprogram call.

Changes of compiler and/or target may lead to different implementation defined and unspecified behavior, which may or not have a visible effect. For example, changing the order of evaluation of arguments in a subprogram call only has a visible effect if the evaluation of arguments itself has some side-effects.

Section 18.4 “Implementation-dependent characteristics” of the GNAT Reference Manual gives some advice on how to address implementation defined behavior for portability.

A particular issue is that the Ada Reference Manual gives much implementation freedom to the compiler in the implementation of operations of fixed-point and floating-point types:

- The small of a fixed-point type is implementation defined (Ada RM 3.5.9(8/2)) unless specified explicitly.
- The base type of a fixed-point type is implementation defined (Ada RM 3.5.9(12-16)), which has an impact on possible overflows.
- The rounded result of an ordinary fixed-point multiplication or division is implementation defined (Ada RM G.2.3(10)).
- For some combinations of types of operands and results for fixed-point multiplication and division, the value of the result belongs to an implementation defined set of values (Ada RM G.2.3(5)).
- The semantics of operations on floating-point types is implementation defined (Ada RM G.2). It may or may not follow the IEEE 754 floating point standard.
- The precision of elementary functions (exponential and trigonometric functions) is implementation defined (Ada RM G.2.4).

Section 18.1 “Writing Portable Fixed-Point Declarations” of the GNAT Reference Manual gives some advice on how to reduce implementation defined behavior for fixed-point types. Use of IEEE 754 floating-point arithmetic can be enforced in GNAT by using the compilation switches “-msse2 -mfpmath=ssse”, as documented in section 6.3.1.6 “Floating Point Operations” of the GNAT User’s Guide.

Note that a number of restrictions can be used to prevent some features leading to implementation defined or unspecified behavior:

- **Restriction** No_Fixed_Point forbids the use of fixed-point types.
- **Restriction** No_Floating_Point forbids the use of floating-point types.
- **Restriction** No_Implementation_Aspect_Specifications forbids the use of implementation defined aspects.
- **Restriction** No_Implementation_Attributes forbids the use of implementation defined attributes.
- **Restriction** No_Implementation_Pragmas forbids the use of implementation defined pragmas.

**Note:** SPARK defines a few constructs (aspects, pragmas and attributes) that are not defined in Ada. While GNAT supports these constructs, care should be exercised to use these constructs with other compilers, or older versions of GNAT. This issue is detailed in section Portability Issues.

### Portability of Programs With Errors

In addition to the portability issues discussed so far, programs with errors cause specific portability issues related to whether errors are detected and how they are reported. The Ada Reference Manual distinguishes between four types of errors (see Ada RM 1.1.5 “Classification of Errors”):

- **Compile-time errors** - These errors make a program illegal, and should be detected by any Ada compiler. They do not cause any portability issue, as they must be fixed before compilation.

- **Run-time errors** - These errors are signaled by raising an exception at run time. They might be a cause of portability problems, as a change of compiler and/or target may lead to new run-time errors. For example, a new compiler may cause the program to use more stack space, leading to an exception Storage_Error, and a new target may change the size of standard integer types, leading to an exception Constraint_Error.

- **Bounded errors** - These errors need not be detected either at compiler time or at run time, but their effects should be bounded. For example, reading an uninitialized value may result in any value of the type to be used, or to Program_Error being raised. Like for run-time errors, they might be a cause of portability problems, as a change of compiler and/or target may lead to new bounded errors.

- **Erroneous execution** - For the remaining errors, a program exhibits erroneous execution, which means that the error need not be detected, and its effects are not bounded by the language rules. These errors might be a cause of portability problems.

Portability issues may arise in a number of cases related to errors:

- The original program has an error that is not detected (a run-time error, bounded error or erroneous execution). Changing the compiler and/or target causes the error to be detected (an exception is raised) or to trigger a different behavior. Typically, reads of uninitialized data or illegal accesses to memory that are not detected in the original program may result in errors when changing the compiler and/or the target.

- The original program has no error, but changing the compiler and/or target causes an error to appear, which may or not be detected. Typically, uses of low-level constructs like Unchecked_Conversion which depend on the exact representation of values in bits may lead to errors when changing the compiler and/or the target. Some run-time errors like overflow errors or storage errors are also particularly sensitive to compiler and target changes.

To avoid portability issues, errors should be avoided by using suitable analyses and reviews in the context of the original and the new compiler and/or target. Whenever possible, these analyses and reviews should be automated by tools to guarantee that all possible errors of a given kind have been reported.

### Benefits of Using SPARK for Portability

The **Language Restrictions** in SPARK favor portability by excluding problematic language features (see Excluded Ada Features):

- By excluding side-effects in expressions, SPARK programs cannot suffer from effects occurring in different orders depending on the order of evaluation of expressions chosen by the compiler.
• By excluding aliasing, the behavior of SPARK programs does not depend on the parameter passing mechanism (by copy or by reference) or the order of assignment to out and in-out parameters passed by copy after the call, which are both chosen by the compiler.

• By excluding controlled types, SPARK programs cannot suffer from the presence and ordering of effects taking place as part of the initialization, assignment and finalization of controlled objects, which depend on choices made by the compiler.

As permitted by the SPARK language rules (see section 1.4.1 “Further Details on Formal Verification” of the SPARK Reference Manual), GNATprove rejects with an error programs which may implicitly raise a Program_Error in parts of code that are in SPARK. For example, all static execution paths in a SPARK function should end with a return statement, a raise statement, or a pragma Assert (False). GNATprove’s analysis can be further used to ensure that dynamic executions can only end in a return.

GNATprove reduces portability issues related to the use of fixed-point and floating-point values:

• GNATprove supports a subset of fixed-point types and operations that ensures that the result of an operation always belongs to the perfect result set as defined in Ada RM G.2.3. Note that the perfect result set still contains in general two values (the two model fixed-point values above and below the perfect mathematical result), which means that two compilers may give two different results for multiplication and division. Users should thus avoid multiplication and division of fixed-point values for maximal portability. See Tool Limitations.

• GNATprove assumes IEEE 754 standard semantics for basic operations of floating-point types (addition, subtraction, multiplication, division). With GNAT, this is achieved by using compilation switches “-msse2 -mfpmath=sse”. Users should still avoid elementary functions (exponential and trigonometric functions) for maximal portability. See Semantics of Floating Point Operations.

Additionally, GNATprove can detect all occurrences of specific portability issues in SPARK code (that is, parts of the program for which SPARK_Mode=On is specified, see section on Identifying SPARK Code) when run in specific modes (see Effect of Mode on Output for a description of the different modes):

• In all modes (including mode check), when switch --pedantic is set, GNATprove issues a warning for every arithmetic operation which could be re-ordered by the compiler, thus leading to a possible overflow with one compiler and not another. For example, arithmetic operation \(A + B + C\) can be interpreted as \((A + B) + C\) by one compiler, and \(A + (B + C)\) (after re-ordering) by another compiler. Note that GNAT always uses the former version without re-ordering. See Parenthesized Arithmetic Operations.

• In modes flow, prove and all, GNATprove issues high check messages on possible parameter aliasing, when such an aliasing may lead to interferences. This includes all cases where the choice of parameter passing mechanism in a compiler (by copy or by reference) might influence the behavior of the subprogram. See Absence of Interferences.

• In modes flow, prove and all, GNATprove issues check messages on possible reads of uninitialized data. These messages should be reviewed with respect to the stricter Data Initialization Policy in SPARK rather than in Ada. Hence, it is possible when the program does not conform to the stricter SPARK rules to manually validate them, see section Justifying Check Messages.

• In modes prove and all, GNATprove issues check messages on all possible run-time errors corresponding to raising exception Constraint_Error at run time, all possible failures of assertions corresponding to raising exception Assert_Error at run time, and all possible explicit raising of exceptions in the program.

The analysis of GNATprove can take into account characteristics of the target (size and alignment of standard scalar types, endianness) by specifying a Target Parameterization.

How to Use SPARK for Portability

GNATprove’s analysis may be used to enhance the portability of programs. Note that the guarantees provided by this analysis only hold for the source program. To ensure that these guarantees extend to the executable object code, one should independently provide assurance that the object code correctly implements the semantics of the source code.
Avoiding Non-Portable Features

As much as possible, uses of non-portable language features should be avoided, or at least isolated in specific parts of the program to facilitate analyses and reviews when changing the compiler and/or the target.

This includes in particular language features that deal with machine addresses, data representations, interfacing with assembler code, and similar issues (for example, language attribute Size). When changing the compiler and/or the target, the program logic should be carefully reviewed for possible dependences on the original compiler behavior and/or original target characteristics. See also the section 18.4.5 “Target-specific aspects” of the GNAT Reference Manual.

In particular, features that bypass the type system of Ada for reinterpreting values (Unchecked_Conversion) and memory locations (Address clause overlays, in which multiple objects are defined to share the same address, something that can also be achieved by sharing the same Link_Name or External_Name) have no impact on SPARK analysis, yet they may lead to portability issues.

By using the following restrictions (or a subset thereof), one can ensure that the corresponding non-portable features are not used in the program:

```
pragma No_Dependence (Ada.Unchecked_Conversion);
pragma No_Dependence (System.Machine_code);
```

Similarly, the program logic should be carefully reviewed for possible dependency on target characteristics (for example, the size of standard integer types). GNATprove’s analysis may help here as it can take into account the characteristics of the target. Hence, proofs of functional properties with GNATprove ensure that these properties will always hold on the target.

In the specific case that the target is changing, it might be useful to run GNATprove’s analysis on the program in proof mode, even if it cannot prove completely the absence of run-time errors and that the specified functional properties (if any) hold. Indeed, by running GNATprove twice, once with the original target and once with the new target, comparing the results obtained in both cases might point to parts of the code that are impacted by the change of target, which may require more detailed manual reviews.

Apart from non-portable language features and target characteristics, non-portability in SPARK may come from a small list of causes:

- Possible re-ordering of non-parenthesized arithmetic operations. These can be detected by running GNATprove (see Benefits of Using SPARK for Portability). Then, either these operations may not be re-ordered by the compiler (for example, GNAT ensures this property), or re-ordering may not lead to an intermediate overflow (for example, if the base type is large enough), or the user may introduce parentheses to prevent re-ordering.

- Possible aliasing between parameters (or parameters and global variables) of a call causing interferences. These can be detected by running GNATprove (see Benefits of Using SPARK for Portability). Then, either aliasing is not possible in reality, or aliasing may not cause different behaviors depending on the parameter passing mechanism chosen in the compiler, or the user may change the code to avoid aliasing. When SPARK subprograms are called from non-SPARK code (for example Ada or C code), manual reviews should be performed to ensure that these calls cannot introduce aliasing between parameters, or between parameters and global variables.

- Possible different choices of base type for user-defined integer types (contrary to derived types or subtypes, which inherit their base type from their parent type). GNATprove follows GNAT in choosing as base type the smallest multiple-words-size integer type that contains the type bounds (see Base Type of User-Defined Integer Types for more information).

- Issues related to errors. See section Avoiding Errors to Enhance Portability.

- Issues related to the use of fixed-point or floating-point operations. See section Portability of Fixed-Point and Floating-Point Computations below.
Avoiding Errors to Enhance Portability

Because errors in a program make portability particularly challenging (see *Portability of Programs With Errors*), it is important to ensure that a program is error-free for portability. GNATprove’s analysis can help by ensuring that the SPARK parts of a program are free from broad kinds of errors:

- all possible reads of uninitialized data
- all possible explicit raise of exceptions in the program
- all possible run-time errors except raising exception *Storage_Error*, corresponding to raising exception *Program_Error*, *Constraint_Error* or *Tasking_Error* at run time
- all possible failures of assertions corresponding to raising exception *Assert_Error* at run time

When parts of the program are not in SPARK (for example, in Ada or C), the results of GNATprove’s analysis depend on assumptions on the correct behavior of the non-SPARK code. For example, callers of a SPARK subprogram should only pass initialized input values, and non-SPARK subprograms called from SPARK code should respect their postcondition. See section *Managing Assumptions* for the complete list of assumptions.

In particular, when changing the target characteristics, GNATprove’s analysis can be used to show that no possible overflow can occur as a result of changing the size of standard integer types.

GNATprove’s analysis does not detect possible run-time errors corresponding to raising exception *Storage_Error* at run time, which should be independently assessed. Because access types and dynamic allocation are forbidden in SPARK, the only possible cause for raising exception *Storage_Error* in a SPARK program is overflowing the stack.

Portability of Fixed-Point and Floating-Point Computations

Portability issues related to the use of fixed-point or floating-point operations can be avoided altogether by ensuring that the program does not use fixed-point or floating-point values, using:

```ada
pragma Restrictions (No_Fixed_Point);
pragma Restrictions (No_Floating_Point);
```

When fixed-point values are used, the value of the small and size in bits for the type should be specified explicitly, as documented in section 18.1 “Writing Portable Fixed-Point Declarations” of the GNAT Reference Manual:

```ada
My_Small : constant := 2.0**(15);
My_First : constant := -1.0;
My_Last : constant := +1.0 - My_Small;

type F2 is delta My_Small range My_First .. My_Last;
for F2'Small use my_Small;
for F2'Size use 16;
```

The program should also avoid multiplication and division of fixed-point values to ensure that the result of arithmetic operations is exactly defined.

When floating-point values are used, use of IEEE 754 standard semantics for basic operations of floating-point types (addition, subtraction, multiplication, division) should be enforced. With GNAT, this is achieved by using compilation switches “-msse2 -mfpmath=sse”.

The program should also avoid elementary functions (exponential and trigonometric functions), which can be ensured with a restriction:
If elementary functions are used, subject to reviews for ensuring portability, GNATprove’s proof results may depend on the fact that elementary functions can be modeled as mathematical functions of their inputs that always return the same result when taking the same values in arguments. GNAT compiler was modified to ensure this property (see https://blog.adacore.com/how-our-compiler-learnt-from-our-analyzers), which may not hold for other Ada compilers.

### 8.2 Project Scenarios

The workflow for using SPARK depends not only on the chosen Objectives of Using SPARK, but also on the context in which SPARK is used: Is it for a new development? Or an evolution of an existing codebase? Is the existing codebase in Ada or in a version of SPARK prior to SPARK 2014? We examine all these project scenarios in this section.

#### 8.2.1 Maintenance and Evolution of Existing Ada Software

Although SPARK is a large subset of Ada, it contains a number of Language Restrictions which prevent in general direct application of GNATprove to an existing Ada codebase without any modifications. The suggested workflow is to:

1. Identify violations of SPARK restrictions.
2. For each violation, either rewrite the code in SPARK or mark it `SPARK_Mode => Off` (see section on Identifying SPARK Code).
3. Perform the required analyses to achieve the desired objectives (see section on Formal Verification with GNATprove), a process which likely involved writing contracts (see in particular section on How to Write Subprogram Contracts).
4. Make sure that the assumptions made for formal verification are justified at the boundary between SPARK and full Ada code (see section on Managing Assumptions).

#### Identifying Violations of SPARK Restrictions

A simple way to identify violations of SPARK restrictions is by **Setting the Default SPARK_Mode** to `SPARK_Mode => On`, and then running GNATprove either in `check` mode (to report basic violations) or in `flow` mode (to report violations whose detection requires flow analysis).

If only a subset of the project files should be analyzed, one should create a project file for **Specifying Files To Analyze** or **Excluding Files From Analysis**.

Finally, one may prefer to work her way through the project one unit at a time by **Using SPARK_Mode in Code**, and running GNATprove on the current unit only.

#### Rewriting the Code in SPARK

Depending on the violation, it may be more or less easy to rewrite the code in SPARK:

- Access types should in general be rewritten as private types of a package whose public part is marked `SPARK_Mode => On` and whose private part is marked `SPARK_Mode => Off`. Thus, the body of that package cannot be analyzed by GNATprove, but clients of the package can be analyzed.
- Functions with side-effects should be rewritten as procedures, by adding an additional out parameter for the result of the function.
• Aliasing should be either explicitly signed off by Justifying Check Messages or removed by introducing a copy of the object to pass as argument to the call.

• Goto statements should be rewritten into regular control and looping structures when possible.

• Controlled types cannot be rewritten easily.

• Top-level exception handlers can be moved to a wrapper subprogram, which calls the subprogram without handlers and handles the exceptions which may be raised. The callee subprogram (and any callers) can thus be analyzed by GNATprove, while the body of the wrapper subprogram is marked SPARK_Mode => Off. The same result can be obtained for exception handlers not at top-level by first refactoring the corresponding block into a subprogram.

**Using SPARK_Mode to Select or Exclude Code**

Depending on the number and location of remaining violations, SPARK_Mode can be used in different ways:

• If most of the codebase is in SPARK, Setting the Default SPARK_Mode to SPARK_Mode => On is best. Violations should be isolated in parts of the code marked SPARK_Mode => Off by either Excluding Selected Unit Bodies or Excluding Selected Parts of a Unit.

• Otherwise, SPARK_Mode => On should be applied selectively for Verifying Selected Subprograms or Verifying Selected Units. Violations are allowed outside the parts of the code marked SPARK_Mode => On.

• Even when most of the code is in SPARK, it may be more cost effective to apply SPARK_Mode => On selectively rather than by default. This is the case in particular when some units have non-SPARK declarations in the public part of their package spec (for example access type definitions). Rewriting the code of these units to isolate the non-SPARK declarations in a part that can be marked SPARK_Mode => Off may be more costly than specifying no SPARK_Mode for these units, which allows SPARK code elsewhere in the program to refer to the SPARK entities in these units.

When analyzing a unit for the first time, it may help to gradually mark the code SPARK_Mode => On:

1. Start with the unit spec marked SPARK_Mode => On and the unit body marked SPARK_Mode => Off. First run GNATprove in flow mode, then in proof mode, until all errors are resolved (some unproved checks may remain, as errors and checks are different Categories of Messages).

2. Continue with the both the unit spec and body marked SPARK_Mode => On. First run GNATprove in flow mode, then in proof mode, until all errors are resolved.

3. Now that GNATprove can analyze the unit without any errors, continue with whatever analysis is required to achieve the desired objectives.

**8.2.2 New Developments in SPARK**

In this scenario, a significant part of a software (possibly a module, possibly the whole software) is developed in SPARK. Typically, SPARK is used for the most critical parts of the software, with less critical parts programmed in Ada, C or Java (for example the graphical interface). A typical development process for this scenario might be:

1. Produce the high level (architectural) design in terms of package specifications. Determine which packages will be in SPARK, to be marked SPARK_Mode => On.

2. Alternatively, if the majority of packages are to be SPARK, Setting the Default SPARK_Mode to SPARK_Mode => On is best. Those few units that are not SPARK should be marked SPARK_Mode => Off.

3. Add Package Contracts to SPARK packages and, depending on the desired objectives, add relevant Subprogram Contracts to the subprograms declared in these packages. The package contracts should identify the key elements of State Abstraction which might also be referred to in Data Dependencies and Flow Dependencies.
4. Begin implementing the package bodies. One typical method of doing this is to use a process of top-down decomposition, starting with a top-level subprogram specification and implementing the body by breaking it down into further (nested) subprograms which are themselves specified but not yet implemented, and to iterate until a level is reached where it is appropriate to start writing executable code. However the exact process is not mandated and will depend on other factors such as the design methodology being employed. Provided unimplemented subprograms are stubbed (that is, they are given dummy bodies), GNATprove can be used at any point to analyze the program.

5. As each subprogram is implemented, GNATprove can be used (in mode flow or proof depending on the objectives) to verify it (against its contract, and/or to show absence of run-time errors).

8.2.3 Conversion of Existing SPARK Software to SPARK 2014

If an existing piece of software has been developed in a previous version of SPARK and is still undergoing active development/maintenance then it may be advantageous to upgrade to using SPARK 2014 in order to make use of the larger language subset and the new tools and environment. This requires more efforts than previous upgrades between versions of SPARK (SPARK 83, SPARK 95 and SPARK 2005) because the new version SPARK 2014 of SPARK is incompatible with those previous versions of the language. While the programming language itself in those previous versions of SPARK is a strict subset of SPARK 2014, the contracts and assertions in previous versions of SPARK are expressed as stylized comments that are ignored by GNATprove. Instead, those contracts and assertions should be expressed as executable Ada constructs, as presented in the Overview of SPARK Language.

The SPARK Language Reference Manual has an appendix containing a SPARK 2005 to SPARK 2014 Mapping Specification which can be used to guide the conversion process. Various options can be considered for the conversion process:

1. Only convert annotations into contracts and assertions, with minimal changes to the executable code - Note that some changes to the code may be required when converting annotations, for example adding with-clauses in a unit to give visibility over entities used in contracts in this unit but defined in another units (which was performed in previous versions of SPARK with inherit annotations). This conversion should be relatively straightforward by following the mapping of features between the two languages.

   The SPARK tools should be used to analyze the work in progress throughout the conversion process (which implies that a bottom-up approach may work best) and any errors corrected as they are found. This may also be an occasion to dramatically simplify annotations, as GNATprove requires far fewer of them. See the description of the conversion of SPARKSkein program in the section about Examples in the Toolset Distribution, for which a majority of the annotations are not needed anymore.

   Once the conversion is complete, development and maintenance can continue in SPARK.

2. In addition to converting annotations, benefit from the larger language and more powerful tools to simplify code and contracts - SPARK 2014 is far less constraining than previous versions of SPARK in terms of dependencies between units (which can form a graph instead of a tree), control structures (for example arbitrary return statements and exit statements are allowed), data structures (for example scalar types with dynamic bounds are allowed), expressions (for example local variables can be initialized with non-static expressions at declaration). In addition, useful new language constructs are available:
   - Contract Cases can be used to replace complex postconditions with implications.
   - Predicates can be used to state invariant properties of subtypes, so that they need not be repeated in preconditions, postconditions, loop invariants, etc.
   - Expression Functions can be used to replace simple query functions and their postcondition.
   - Ghost Code can be used to mark code only used for verification.
   - Loop Variants can be used to prove the termination of loops.
Changing the code to use these new features may favor readability and maintenance. These changes can be performed either while converting annotations, or as a second stage after all annotations have been converted (the case discussed above). Like in the previous case, the SPARK tools should be used to analyze the work in progress throughout the conversion process (which implies that a bottom-up approach may work best) and any errors corrected as they are found. Once the conversion is complete, development and maintenance can continue in SPARK.

3. Gradually convert annotations and code - It is possible to keep annotations in comments for the previous versions of SPARK while gradually adding contracts and assertions in SPARK 2014. The latest version of the SPARK 2005 toolset facilitates this gradual migration by ignoring SPARK pragmas. Thus, new contracts (for example Preconditions and Postconditions) should be expressed as pragmas rather than aspects in that case.

Typically, annotations and code would be converted when it needs to be changed. The granularity of how much code needs to be converted when a module is touched should be considered, and is likely to be at the level of the whole package.

The latest version of the SPARK 2005 toolset can be used to continue analyzing the parts of the program that do not use the new features of SPARK 2014, including units which have the two versions of contracts in parallel. GNATprove can be used to analyze parts of the program that have contracts in SPARK 2014 syntax, including units which have the two versions of contracts in parallel.

Note that some users may wish to take advantage of the new SPARK contracts and tools whilst retaining the more restrictive nature of SPARK 2005. (Many of the restrictions from SPARK 2005 have been lifted in SPARK because improvements in the tools mean that sound analysis can be performed without them, but some projects may need to operate in a more constrained environment.) This can be achieved using pragma Restrictions (SPARK_05).

For further details of this restriction please see the GNAT Reference Manual.

8.2.4 Analysis of Frozen Ada Software

In some very specific cases, users may be interested in the results of GNATprove’s analysis on an unmodified code. This may be the case for example if the only objective is to Ensure Portability of Programs for existing Ada programs that cannot be modified (due to some certification or legal constraints).

In such a case, the suggested workflow is very similar to the one described for Maintenance and Evolution of Existing Ada Software, except the code cannot be rewritten when a violation of SPARK restrictions is encountered, and instead that part of the code should be marked SPARK_Mode => Off. To minimize the parts of the code that need to be marked SPARK_Mode => Off, it is in general preferable to apply SPARK_Mode => On selectively rather than by default, so that units that have non-SPARK declarations in the public part of their package spec (for example access type definitions) need not be marked SPARK_Mode => Off. See Using SPARK_Mode to Select or Exclude Code for details.
GNATprove is executed with the following command line:

```bash
Usage: gnatprove -Pproj [switches] [-cargs switches]

proj is a GNAT project file
-cargs switches are passed to gcc

All main units in proj are analyzed by default. Switches to change this:
-  -u [files]    Analyze only the given files
    [files]    Analyze given files and all dependencies
-  -U          Analyze all files (including unused) of all projects

gnatprove basic switches:
-  -aP=p        Add path p to project path
-  --assumptions Output assumptions information
-  --codepeer=c Enable or disable CodePeer analysis (c=on,off*)
-  --clean      Remove GNATprove intermediate files, and exit
-  --cwe        Include CWE ids in message output
-  -f           Force recompilation/analysis of all units
-  -h, --help   Display this usage information
-  --info       Output info messages about the analysis
-  -j N         Use N parallel processes (default: 1; N=0 will use
         all cores of the machine)
-  -k           Do not stop analysis at the first error
-  --level=n    Set the level of proof (0 = faster to 4 = more powerful)
-  --list-categories Output a list of all message categories and exit
-  -m           Minimal reanalysis
-  --mode=m     Set the mode of GNATprove (m=check, check_all, flow,
         prove, all*, stone, bronze, silver, gold)
-  --no-subprojects Do not analyze subprojects, only the root project
-  --output-msg-only Do not run any provers, output current flow and proof
         results
-  -q, --quiet  Be quiet/terse
-  --replay     Replay proofs, do not attempt new proofs
-  --report=r   Set the report mode of GNATprove (r=fail*, all,
         provers, statistics)
-  --subdirs=p  Create all artifacts in this subdir
-  -v, --verbose Output extra verbose information
-  --version    Output version of the tool and exit
-  --warnings=w Set the warning mode of GNATprove
         (w=off, continue*, error)

* Main mode values
  . check         - Fast partial check for SPARK violations
  . check_all, stone - Full check for SPARK violations
```
flow, bronze — Prove correct initialization and data flow
prove — Prove absence of run-time errors and contracts
all, silver, gold — Activates all modes (default)

* Report mode values
  . fail — Report failures to prove checks (default)
  . all — Report all results of proving checks
  . provers — Same as all, plus prover usage information
  . statistics — Same as provers, plus timing and steps information

* Warning mode values
  . off — Do not issue warnings
  . continue — Issue warnings and continue (default)
  . error — Treat warnings as errors

gnatprove advanced switches:
  --checks-as-errors Treat unproved check messages as errors
  -d, --debug Debug mode
  --debug-save-vcs Do not delete intermediate files for provers
  --flow-debug Extra debugging for flow analysis (requires graphviz)
  --limit-line=f:l Limit analysis to given file and line
  --limit-line=f:l:c:k Limit analysis to given file, line, column and kind of check
  --limit-region=f:l:l Limit analysis to given file and range of lines
  --limit-subp=s Limit analysis to subprogram defined by file and line
  --memcached-server=host:portnumber Specify a memcached instance that will be used for caching of proof results.
  --memlimit=nnn Set the prover memory limit in MB. Use value 0 for no limit (default when no level set)
  --no-axiom-guard Do not generate guards for axioms defining contracts of functions
  --no-counterexample Do not generate a counterexample for unproved formulas
  --no-global-generation Do not generate Global and Initializes contracts from code, instead assume "null". Note that this option also implies --no-inlining.
  --no-inlining Do not inline calls to local subprograms for proof
  --no-loop-unrolling Do not unroll loops with static bounds and no (in)variant for proof
  --output-header Add a header with extra information in the generated output file
  --pedantic Use a strict interpretation of the Ada standard
  --proof-warnings Issue warnings by proof
  --proof=g[:l] Set the proof modes for generation of formulas
(g=per_check*, per_path, progressive) (l=lazy*, all)
  --prover=s[,s]* Use given provers (s=altergo, cvc4*, z3, ..., or s=all for using all built-in provers)
  --RTS=dir Specify the Ada runtime name/location
  --steps=nnn Set the maximum number of proof steps (prover-specific) Use value 0 for no steps limit.
  --timeout=nnn Set the prover timeout in seconds. Use value 0 for no timeout (default when no level set)
  --why3-conf=f Specify a configuration file for why3

* Proof mode values for generation
  . per_check — Generate one formula per check (default when no level set)
  . per_path — Generate one formula per path for each check
<table>
<thead>
<tr>
<th>Mode</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>progressive</td>
<td>Start with one formula per check, then split into paths when needed</td>
</tr>
</tbody>
</table>

* Proof mode values for laziness
  - lazy - Stop at first unproved formula for each check (most suited for fully automatic proof) (default)
  - all - Attempt to prove all formulas (most suited for combination of automatic and manual proof)

* Prover name values
  (Default prover is cvc4.)
  (Provers marked with [steps] support the --steps switch.)
  - altergo - [steps] Use Alt-Ergo
  - cvc4 - [steps] Use CVC4
  - z3 - [steps] Use Z3
  - ... - Any other prover configured in your .why3.conf file
**ALTERNATIVE PROVERS**

**B.1 Installed with SPARK Pro**

The provers Alt-Ergo, CVC4 and Z3 are installed with the SPARK tool. By default, GNATprove uses prover CVC4 only. Switch `--level` changes the default to use one or more provers depending on the chosen level (see *Running GNATprove from the Command Line*). Switch `--prover` allows to use another prover, or a list of provers. Prover names `altergo`, `cvc4` and `z3` are used to refer to the versions of provers Alt-Ergo, CVC4 and Z3 that are installed with the SPARK toolset. The string `alt-ergo` can also be used to refer to Alt-Ergo. Using the switch `--prover=all`, one can select all three built-in provers, in the order `cvc4`, `z3`, `altergo`. More information on Alt-Ergo, CVC4 and Z3 can be found on their respective websites:

- Alt-Ergo: https://alt-ergo.ocamlpro.com
- Z3: https://github.com/Z3Prover/z3

**B.2 Installed with SPARK Discovery**

In this case, only prover Alt-Ergo is installed with the SPARK tool. Hence, by default GNATprove only uses prover Alt-Ergo. In particular, switch `--level` has no impact on the use of different provers, and `--prover=all` will only select Alt-Ergo.

**B.3 Installed with SPARK Community**

The provers Alt-Ergo, CVC4 and Z3 are installed with the SPARK tool.

**B.4 Other Automatic or Manual Provers**

**B.4.1 Updating the Why3 Configuration File**

GNATprove can call other provers, as long as they are supported by the Why3 platform (see complete list on Why3 webpage). To use another prover, it must be listed in your Why3 configuration file.

To create or update automatically a Why3 configuration file, call the command `<spark2014-install>/libexec/spark/bin/why3config --detect-provers`. It searches your `PATH` for any supported provers and adds them to the default configuration file `.why3.conf` in your `HOME`, or a configuration file given in argument with switch `-C <file>`. This file consists of a few general settings and a section for each prover which is supported.
Note that GNATprove never reads the default configuration file .why3.conf in your HOME. You need to pass the configuration file explicitly with switch --why3-conf=<file>. Any prover name configured in this configuration file can be used as an argument to switch --prover.

Note that using this mechanism, you cannot replace the definitions provided with the SPARK tools for the provers altergo, cvc4 and z3.

If more than one prover is specified, the provers are tried in order on each VC, until one of them succeeds or all fail. Interactive provers cannot be combined with other provers, so must appear on their own.

### B.4.2 Sharing Libraries of Theorems

When GNATprove is used with a manual prover, the user can provide libraries of theorems to use during the proof process.

To do so, the user will need to set a proof directory (see Project Attributes for more details on this directory). The user needs to create a folder with the same name as the chosen manual prover (the casing of the name is the same as the one passed to the switch --prover) and put the library sources inside this folder.

Finally, some additional fields need to be added to the prover configuration in the Why3 configuration file (a basic example of prover configuration can be found in the section on Coq):

- **configure_build**: this field allows you to specify a command to configure the compilation of the library of theorems. This command will be called each time a source file is added to the library.

- **build_commands**: this field allows you to specify a set of command which will be called sequentially to build your library. These commands will be called each time GNATprove runs the corresponding manual prover. (In order to define multiple commands for this field, just set the field multiple times with different values, each time the field is set it adds a new element to the set of build_commands).

Inside these commands, pattern %f refers to the name of the library file considered, and %o to the name of the main gnatprove repository generated by GNATprove. This allows referring to the path of the compiled library of theorems inside these commands with %o/user/<prover_name>.

### B.5 Coq

gnatprove has support for the Coq interactive prover, even though Coq is not part of the SPARK distribution. If you want to use Coq with SPARK, you need to install it yourself on your system and put it in your PATH environment variable. Then, you can simply provide --prover=coq to gnatprove. Note that the only supported version currently is Coq 8.5.
GNATprove reads the package `Prove` in the given project file. This package is allowed to contain the following attributes:

- **Proof_Switches**, which defines additional command line switches that are used for the invocation of GNATprove. This attribute can be used in two different settings:
  
  - to define switches that should apply to all files in the project. As an example, the following package in the project file sets the default report mode of GNATprove to `all`:
    ```plaintext
    package Prove is
    for Proof_Switches ("Ada") use ("--report=all");
    end Prove;
    ```
  
  - to define switches that should apply only to one file. The following example sets timeout for provers run by GNATprove to 10 seconds for `file.adb`:
    ```plaintext
    package Prove is
    for Proof_Switches ("file.adb") use ("--timeout=10");
    end Prove;
    ```

  Switches given on the command line have priority over switches given in the project file, and file-specific switches have priority over switches that apply to all files. A special case is the `--level` switch: the values for `--timeout` etc implied by the `--level` switch are always overridden by more specific switches, regardless of where they appear. For example, the timeout for the analysis of `file.adb` is set to 10 seconds below, despite the `--level=0` switch (which implies a lower timeout) specified for this file:

  ```plaintext
  package Prove is
  for Proof_Switches ("Ada") use ("--timeout=10");
  for Proof_Switches ("file.adb") use ("--level=0");
  end Prove;
  ```

  The following switches cannot be used inside project files: `-P`, `-aP`, `--subdirs`, `--clean`, `--list-categories`, `--version`.

  Only the following switches are allowed for file-specific switches: `--steps`, `--timeout`, `--memlimit`, `--proof`, `--prover`, `--level`, `--no-counterexample`, `--no-inlining`, `--no-loop-unrolling`.

  - **Switches.** This deprecated attribute is the same as `Proof_Switches ("Ada")`.
  
  - **Proof_Dir**, which defines the directory where are stored the files concerning the state of the proof of a project. This directory contains a sub-directory `sessions` with one directory per source package analyzed for proof. Each of these package directories contains a Why3 session file. If a manual prover is used to prove some VCs, then a sub-directory called by the name of the prover is created next to `sessions`, with the same organization.
of sub-directories. Each of these package directories contains manual proof files. Common proof files to be used across various proofs can be stored at the toplevel of the prover-specific directory.
D.1 Pragma SPARK_Mode

SPARK_Mode is a three-valued aspect. At least until we get to the next paragraph, a SPARK_Mode of On, Off, or Auto is associated with each Ada construct. Roughly, the meaning of the three values is the following:

- a value of On means that the construct is required to be in SPARK, and the construct will be analyzed by GNATprove.
- a value of Off means that the construct will not be analyzed by GNATprove, and does not need to obey the SPARK restrictions. The construct also cannot be referenced from other parts that are required to be in SPARK.
- a value of Auto means that the construct will not be analyzed, and GNATprove will infer whether this construct can be used in other SPARK parts or not.

We now explain in more detail how the SPARK_Mode pragma works.

Some Ada constructs are said to have more than one “section”. For example, a declaration which requires a completion will have (at least) two sections: the initial declaration and the completion. The SPARK_Modes of the different sections of one entity may differ. In other words, SPARK_Mode is not an aspect of an entity but rather of a section of an entity.

For example, if a subprogram declaration has a SPARK_Mode of On while its body has a SPARK_Mode of Off, then an error would be generated if the subprogram took a parameter of a general access type but not if the subprogram declared a local variable of a general access type (recall that general access types are not in SPARK).

A package is defined to have 4 sections: its visible part, its private part, its body declarations, and its body statements. A protected or task unit has 3 sections: its visible part, its private part, and its body. Other declarations which require a completion have two sections, as noted above; all other entities and constructs have only one section.

If the SPARK_Mode of a section of an entity is Off, then the SPARK_Mode of a later section of that entity shall not be On. [For example, a subprogram can have a SPARK declaration and a non-SPARK body, but not vice versa.]

If the SPARK_Mode of a section of an entity is Auto, then the SPARK_Mode of a later section of that entity shall not be On, and it shall not be Off unless that entity is a generic entity, or an instance of such a generic. [This makes it possible to mark a later section of a generic unit as Off, in cases where its initial section is Auto to allow instantiations to have any value of SPARK_Mode.]

The SPARK_Mode aspect can be specified either via a pragma or via an aspect_specification. In some contexts, only a pragma can be used because of syntactic limitations. In those contexts where an aspect_specification can be used, it has the same effect as a corresponding pragma.

The form of a pragma SPARK_Mode is as follows:

```
pragma SPARK_Mode [ (On | Off) ]
```
The form for the aspect_definition of a SPARK_Mode aspect_specification is as follows:

```
[ On | Off ]
```

For example:

```
package P
  with SPARK_Mode => On
is
```

The pragma can be used as a configuration pragma. The effect of such a configuration pragma is described below in the rules for determining the SPARK_Mode aspect value for an arbitrary section of an arbitrary Ada entity or construct.

Pragma `SPARK_Mode` shall be used as a local pragma in only the following contexts and has the described semantics:

<table>
<thead>
<tr>
<th>Pragma placement</th>
<th>Affected construct</th>
<th>Alternative aspect form</th>
</tr>
</thead>
<tbody>
<tr>
<td>Start of the visible declarations (preceded only by other pragmas) of a package declaration</td>
<td>Visible part of the package</td>
<td>As part of the package_specification</td>
</tr>
<tr>
<td>Start of the visible declarations (preceded only by other pragmas) of a task or protected unit</td>
<td>Visible part of the unit</td>
<td>As part of the declaration</td>
</tr>
<tr>
<td>Start of the private declarations of a package, a protected unit, or a task unit (only other pragmas can appear between the <code>private</code> keyword and the <code>SPARK_Mode</code> pragma)</td>
<td>Private part</td>
<td>None</td>
</tr>
<tr>
<td>Immediately at the start of the declarations of a package body (preceded only by other pragmas)</td>
<td>Body declarations of the package</td>
<td>As part of the package_body</td>
</tr>
<tr>
<td>Start of the elaboration statements of a package body (only other pragmas can appear between the <code>begin</code> keyword and the <code>SPARK_Mode</code> pragma)</td>
<td>Body statements of the package</td>
<td>None</td>
</tr>
<tr>
<td>Start of the declarations of a protected or task body (preceded only by other pragmas)</td>
<td>Body</td>
<td>As part of the protected or task body</td>
</tr>
<tr>
<td>After a subprogram declaration (with only other pragmas intervening). [This does not include the case of a subprogram whose initial declaration is via a subprogram_body_stub. Such a subprogram has only one section because a subunit is not a completion.]</td>
<td>Subprogram's specification</td>
<td>As part of the subprogram_declaration</td>
</tr>
<tr>
<td>Start of the declarations of a subprogram body (preceded only by other pragmas)</td>
<td>Subprogram's body</td>
<td>As part of the subprogram_body</td>
</tr>
</tbody>
</table>

A default argument of On is assumed for any `SPARK_Mode` pragma or aspect_specification for which no argument is explicitly specified.

A `SPARK_Mode` of Auto cannot be explicitly specified; the cases in which a `SPARK_Mode` of Auto is implicitly specified are described below. Roughly speaking, Auto indicates that it is left up to the formal verification tools to determine whether or not a given construct is in SPARK.

A `SPARK_Mode` pragma or aspect_specification shall only apply to a (section of a) package, generic package, subprogram, or generic subprogram.

A `SPARK_Mode` of On shall only apply to a (section of a) library-level entity, except for the case of `SPARK_Mode` specifications occurring within generic instances. A `SPARK_Mode` of On applying to a non-library-level entity within a generic instance has no effect.
The SPARK Mode aspect value of an arbitrary section of an arbitrary Ada entity or construct is then defined to be the following value (except if this yields a result of Auto for a non-package; see below):

- If SPARK Mode has been specified for the given section of the given entity or construct, then the specified value;
- else for the private part of a public child unit whose parent unit’s private part has a SPARK Mode of Off, the SPARK Mode is Off;
- else for the private part of a package or a protected or task unit, the SPARK Mode of the visible part;
- else for a package body’s statements, the SPARK Mode of the package body’s declarations;
- else for the first section (in the case of a package, the visible part) of a public child unit, the SPARK Mode of the visible part of the parent unit;
- else for the first section (in the case of a package, the visible part) of a private child unit, the SPARK Mode of the private part of the parent unit;
- else for any of the visible part or body declarations of a library unit package or either section of a library unit subprogram, if there is an applicable SPARK Mode configuration pragma then the value specified by the pragma; if no such configuration pragma applies, then an implicit specification of Auto is assumed;
- else the SPARK Mode of the enclosing section of the nearest enclosing package or subprogram;
- Corner case: the SPARK Mode of the visible declarations of the limited view of a package is always Auto.

If the above computation yields a result of Auto for any construct other than one of the four sections of a package, then a result of On or Off is determined instead based on the legality (with respect to the rules of SPARK) of the construct. The construct’s SPARK Mode is On if and only if the construct is in SPARK. [A SPARK Mode of Auto is therefore only possible for (sections of) a package.]

In code where SPARK Mode is On (also called “SPARK code”), the rules of SPARK are enforced. In particular, such code shall not reference non-SPARK entities, although such code may reference a SPARK declaration with one or more non-SPARK subsequent sections (e.g., a package whose visible part has a SPARK Mode of On but whose private part has a SPARK Mode of Off; a package whose visible part has a SPARK Mode of Auto may also be referenced).

Code where SPARK Mode is Off shall not enclose code where SPARK Mode is On. However, if an instance of a generic unit is enclosed by code where SPARK Mode is Off and if any SPARK Mode specifications occur within the generic unit, then the corresponding SPARK Mode specifications occurring within the instance have no semantic effect. [In particular, such an ignored SPARK Mode specification could not violate the preceding “Off shall not enclose On” rule because the SPARK Mode of the entire instance is Off. Similarly, such an ignored SPARK Mode specification could not violate the preceding rule that a SPARK Mode specification shall only apply to a (section of a) library-level entity.]

For purposes of the “Off shall not enclose On” rule just described, the initial section of a child unit is considered to occur immediately within either the visible part (for a public child unit) or the private part (for a private child unit) of the parent unit. In addition, the private part of a public child package is considered to occur immediately within the private part of the parent unit. [This follows Ada’s visibility rules for child units. This means, for example, that if a parent unit’s private part has a SPARK Mode of Off, then the private part of a public child package shall not have a SPARK Mode of On. Note also that a SPARK Mode configuration pragma which applies only to the specification (not the body) of a child unit is always ineffective; this is a consequence of the rules given above for determining the SPARK Mode of the first section of a child unit.]

The rules for a protected unit follow from the rules given for other constructs after notionally rewriting the protected unit as a package.

A protected unit declaration such as
protected type Prot
  with SPARK_Mode => On
is
  procedure Op1 (X : in out Integer);
  procedure Op2;
  procedure Non_SPARK_Profile (Ptr : access Integer)
    with SPARK_Mode => Off;
private
  Aaa, Bbb : Integer := 0;
end Prot;

can be thought of, for purposes of SPARK_Mode rules, as being a lot like

package Pkg
  with SPARK_Mode => On
is
  type Prot is limited private;
  procedure Op1 (Obj : in out Prot; X : in out Integer);
  procedure Op2 (Obj : in out Prot);
  procedure Non_SPARK_Profile (Obj : in out Prot; Ptr : access Integer)
    with SPARK_Mode => Off;
private
  type Prot is
    limited record
      Aaa, Bbb : Integer := 0;
    end record;
end Pkg;

which is legal. The point is that a protected type which is in SPARK can have protected operation whose declaration is not in SPARK.

SPARK_Mode is an implementation-defined Ada aspect; it is not (strictly speaking) part of the SPARK language. It is used to notionally transform programs which would otherwise not be in SPARK so that they can be viewed (at least in part) as SPARK programs.

Note that if you would like to mark all your code in SPARK_Mode, the simplest solution is to specify in your project file:

package Builder is
  for Global_Configuration_Pragmas use "spark.adc";
end Builder;

and provide a file spark.adc which contains:

pragma SPARK_Mode;
EXTERNAL AXIOMATIZATIONS

E.1 What is it?

It is a feature of the SPARK toolset that allows to manually supply a WhyML translation for the public specification of a library level package that is in SPARK. This feature is still experimental.

E.2 Why is it useful?

• For features that cannot easily be described using contracts, like transitivity, counting, or summation
• To link functions to the logic world, like trigonometry functions

E.3 How does it work?

• To say that a library package has an external axiomatization, we annotate it using:

```plaintext
pragma Annotate (GNATprove, External_Axiomatization);
```

• These packages should have SPARK_Mode On on their public specification and SPARK_Mode Off on their private part.
• The WhyML translation for the package should be stored in a subdirectory named _theories of the proof directory specified for the project.

E.4 What should the translation look like?

• For each publicly visible entity E in the package P, it should provide the same elements (types as well as logic and program functions) as the automatic translation, all grouped in one single module named P__e. For example, the module for a function F should provide both a logic function declaration named f__logic and a program function declaration named f.
• For most types, a model module in defined in ada__model.mlw that can be cloned to get most of the required declarations.
• The manual translation may use any type, constant and function that is visible from the Ada package declaration.
• A good way to start an axiomatization file on a package is to launch the toolset on it and copy paste the modules created for each entity of the package. A WhyML file created by the tool on a package P contains a module for every declaration visible from it, only declarations from P itself should be copied. The generated file usually
contains two modules for each entity, one named P__e and one named P__e_axiom. Both should be put together in P__e for the manual translation. The toolset will replace statically known expressions with their value. Beware that they might be architecture dependent.

**E.5 Example**

For example, let us consider the following package, stored in a file sum.ads, providing a summation function for slices of arrays of integers:

```haskell
package Sums with SPARK_Mode is
pragma Annotate (GNATprove, External_Axiomatization);

subtype Extended_Index is Integer range 0 .. 2 ** 16;
subtype Index is Integer range 1 .. Extended_Index'Last;

subtype Vector_Element is Integer range Integer'First / Index'Last .. Integer'Last / Index'Last;

type Vector is array (Index range <>) of Vector_Element;

type Slice_Bounds is
record
  Lo : Index;
  Hi : Extended_Index;
end record;

function Sum (X : Vector; Bounds : Slice_Bounds) return Integer with
  Pre => (Bounds.Lo > Bounds.Hi) or else
  (X'First <= Bounds.Lo and Bounds.Hi <= X'Last);
end Sums;
```

We can provide the following Why3 translation for it, that we should store in a file named sum.mlw:

```why3
module Sums__extended_index
use import "_gnatprove_standard".Main
use "_gnatprove_standard".Integer
use import "int".Int

type extended_index

function first : int = 0
function last : int = 65536

predicate in_range (x : int) = first <= x \/
  x <= last

(* Clone of the model module for discrete types with static bounds *)
clonexport "ada__model".Static_Discrete with
type t = extended_index,
function first = first,
function last = last,
predicate in_range = in_range

(* Type for mutable variables of type extended_index *)
type extended_index__ref = {mutable extended_index__content : extended_index}
```
val extended_index__havoc (x : extended_index__ref) : unit
  writes { x }

(* All values of type extended_index are in range *)
predicate dynamic_invariant (expr : int) bool bool bool =
  dynamic_property first last expr

(* We know nothing for default initialization of variables of type
  extended_index *)
predicate default_initial_assumption int bool = true
end

module Sums__extended_index__rep
use import Sums__extended_index
use import "_gnatprove_standard".Main

(* Projection functions from extended_index to int *)
clone export "ada__model".Rep Proj Int with
  type t = extended_index,
  predicate in_range = in_range
end

module Sums__index
use import "_gnatprove_standard".Main
use "_gnatprove_standard".Integer
use import "int".Int

type index
function first : int = 1
function last : int = 65536
predicate in_range (x : int) = first <= x /\ x <= last

(* Clone of the model module for discrete types with static bounds *)
clone export "ada__model".Static Discrete with
  type t = index,
  function first = first,
  function last = last,
  predicate in_range = in_range

(* Type for mutable variables of type index *)
type index__ref = { mutable index__content : index }
val index__havoc (x : index__ref) : unit
  writes { x }

(* All values of type index are in range *)
predicate dynamic_invariant (expr : int) bool bool bool =
  dynamic_property first last expr

(* We know nothing for default initialization of variables of type index *)
predicate default_initial_assumption int bool = true
end

module Sums__index__rep
use import Sums__index
use import "_gnatprove_standard".Main
(* Projection functions from index to int *)
clone export "ada__model".Rep_Proj_Int with
type t = index,
predicate in_range = in_range
end
module Sums__vector_element
use import "_gnatprove_standard".Main
use
"_gnatprove_standard".Int_Division
use import Standard__integer
use import "int".Int
type vector_element
function first : int = Int_Division.div Standard__integer.first 65536
function last

: int = Int_Division.div Standard__integer.last 65536

predicate in_range (x : int)

= first <= x /\ x <= last

(* Clone of the model module for discrete types with static bounds *)
clone export "ada__model".Static_Discrete with
type t = vector_element,
function first = first,
function last = last,
predicate in_range = in_range
(* Type for mutable variables of type vector_element *)
type vector_element__ref = { mutable vector_element__content : vector_element }
val vector_element__havoc (x : vector_element__ref) : unit
writes { x }
end
module Sums__vector_element__rep
use import Sums__vector_element
use import "_gnatprove_standard".Main
(* Projection functions from vector_element to int *)
clone export "ada__model".Rep_Proj_Int with
type t = vector_element,
predicate in_range = in_range
end
(* Module for any array type ranging over signed integer types and
containing vector_element *)
module Array__Int__Sums__vector_element
use import "_gnatprove_standard".Main
use import "int".Int
use
Sums__vector_element
use
Sums__vector_element__rep
function one : int = 1
type component_type = Sums__vector_element.vector_element


_clone export "_gnatprove_standard".Array__1 with
type I1.t = int,
predicate I1.le = Int.(<=),
predicate I1.lt = Int.<),
predicate I1.gt = Int.(>),
function I1.add = Int.(+),
function I1.sub = Int.(-),
function I1.one = one,
type component_type = component_type

(* Primitive equality between arrays *)
function bool_eq (a:map) (af:int) (al:int) (b:map) (bf:int) (bl:int) : bool =
(if af <= al
   then al - af = bl - bf
   else bf > bl) /
   (forall idx : int. af <= idx <= al ->
         (get a idx) = (get b (bf - af + idx)))

(* Clone of the model module for comparison of arrays *)
clone export "ada__model".Array_Int_Rep_Comparison_Axiom with
type component_type = component_type,
function to_rep = Sums__vector_element__rep.to_rep,
type map = map,
type Index.t = int,
predicate Index.le = Int.(<=),
predicate Index.lt = Int.<),
predicate Index.gt = Int.(>),
function Index.add = Int.(+),
function Index.sub = Int.(-),
function Index.one = one,
function get = get,
function bool_eq = bool_eq
end

module Sums__vector
use import "int".Int
use import "_gnatprove_standard".Main
use "_gnatprove_standard".Integer
use import Standard__integer
use import Sums__index
use import Sums__vector_element
use Array__Int__Sums__vector_element
use Standard__integer__rep
use Sums__vector_element__rep

predicate index_dynamic_property (first : int) (last : int) (x : int) =
   first <= x /
   x <= last

(* Clone of the model module for unconstrained arrays *)
type component_type =
   Sums__vector_element.vector_element
function id (x : int) : int = x
(* Clone of the model module for unconstrained arrays *)
clone export "ada_model".Unconstr_Array with
type map = Array__Int__Sums__vector_element.map,
function array_bool_eq = Array__Int__Sums__vector_element.bool_eq,
type index_base_type = Standard__integer.integer,
type index_rep_type = int,
function to_rep = Standard__integer__rep.to_rep,
function rep_to_int = id,
predicate in_range_base = Standard__integer.in_range,
predicate index_dynamic_property = index_dynamic_property,
predicate index_rep_le = Int.(<=)
type vector = __t
(* Type for mutable variables of type vector *)
type vector__ref = { mutable vector__content : vector }
val vector__havoc (x : vector__ref) : unit
writes { x }
(* Helper function *)
function _get "inline" (v : vector) (i : int) : int =
Sums__vector_element__rep.to_rep (Array__Int__Sums__vector_element.get 
(to_array v) i)
(* If vectors are not empty, their bounds are between Index.first and 
Index.last *)
predicate dynamic_invariant (expr : vector) bool (skip_bounds : bool) bool = 
(if skip_bounds then true 
else dynamic_property Sums__index.first Sums__index.last 
(first expr) (last expr))
end
module Sums__slice_bounds
use import "int".Int
use import "gnatprove_standard".Main
use "gnatprove_standard".Integer
use import Sums__index
use Sums__index__rep
use import Sums__extended_index
use Sums__extended_index__rep
(* Fields for record type *)
type __split_fields =
{ rec__sums__slice_bounds__lo : index; rec__sums__slice_bounds__hi : extended_index;
} 
type __split_fields__ref = { mutable __split_fields__content : __split_fields }
val __split_fields__havoc (x : __split_fields__ref) : unit
writes { x }
(* Record type *)
type slice_bounds =
{ __split_fields : __split_fields }
(* Type for mutable variables of type slice_bounds *)
type slice_bounds__ref = { mutable slice_bounds__content : slice_bounds }
val slice_bounds__havoc (x : slice_bounds__ref) : unit
writes { x }
function _rec__lo "inline" (b : slice_bounds) : int = 
    Sums__index__rep.to_rep (rec__sums__slice_bounds__lo (__split_fields, 
                        b))

function _rec__hi "inline" (b : slice_bounds) : int = 
    Sums__extended_index__rep.to_rep (rec__sums__slice_bounds__hi (__split_ 
                        fields (b)))

predicate sums__slice_bounds__lo__pred (a : slice_bounds) = 
    true
val rec__sums__slice_bounds__lo_ 
    (a : slice_bounds) : Sums__index.index 
    requires { sums__slice_bounds__lo__pred a } 
    ensures { result = a.__split_fields.rec__sums__slice_bounds__lo }

predicate sums__slice_bounds__hi__pred (a : slice_bounds) = 
    true
val rec__sums__slice_bounds__hi_ 
    (a : slice_bounds) : Sums__extended_index.extended_index 
    requires { sums__slice_bounds__hi__pred a } 
    ensures { result = a.__split_fields.rec__sums__slice_bounds__hi }

function bool_eq (a : slice_bounds) (b : slice_bounds) : bool = 
    _rec__lo a = _rec__lo b /
    _rec__hi a = _rec__hi b

function dummy : slice_bounds

predicate dynamic_invariant slice_bounds bool bool bool = true

predicate default_initial_assumption slice_bounds bool = true
end

dummy
function _sum "inline" (x : vector) (bounds : slice_bounds) : int = 
  sum__logic x bounds

(* Helper function *)
function _sum "inline" (x : vector) (bounds : slice_bounds) : int = 
  sum__logic x bounds

(* Axiom for defining the sum function *)
axiom sum_def:
  forall v : vector, b : slice_bounds
  [sum__logic v b].

  Standard__integer.in_range (sum__logic v b) /
  (* Case of the empty slice *)
  (_rec__lo b > _rec__hi b -> _sum v b = 0) /

  (* Case of a non-empty slice *)
  (first v <= _rec__lo b <= _rec__hi b <= last v ->
   (* If the slice only contains one element *)
   (_rec__lo b = _rec__hi b -> _sum v b = _get v (_rec__lo b)) /

   (* Link to smaller slices of the same vector *)
   (forall b1 : slice_bounds [sum__logic v b1].
    (* Ending at the same index *)
    (if _rec__hi b1 = _rec__hi b /
     _rec__lo b < _rec__lo b1 <= _rec__hi b ->
     let b2 = (_split_fields =
       rec__sums__slice_bounds__lo = rec__sums__slice_bounds__hi
     rep ((_rec__lo b1) - 1))) in
      _sum v b = _sum v b1 + _sum v b2) /

    (* Sartind at the same index *)
    (if _rec__lo b1 = _rec__lo b /
     _rec__lo b <= _rec__hi b1 < _rec__hi b ->
     let b2 = (_split_fields =
       rec__sums__slice_bounds__lo = Sums__extended_index__rep.of_reps
       _split_fields b);
      rec__sums__slice_bounds__hi = Sums__extended_index__rep.of_reps
       (_rec__lo b1) + 1);)

    _sum v b = _sum v b1 + _sum v b2))

(* Program partial function with a precondition for sum *)
val sum (x : vector) (bounds : slice_bounds) : int
  requires { _rec__lo bounds > _rec__hi bounds \/
    first x <= _rec__lo bounds \/
    _rec__hi bounds <= last x }
  ensures { result = sum__logic x bounds }
end
ASPECTS OR PRAGMAS SPECIFIC TO GNATPROVE

This appendix lists all the aspects or pragmas specific to GNATprove, in particular all the uses of aspect or pragma Annotate for GNATprove. Aspect or pragma Annotate can also be used to control other AdaCore tools. The uses of such annotations are explained in the User’s guide of each tool.

Annotations in GNATprove are useful in two cases:

1. for justifying check messages using Direct Justification with Pragma Annotate, typically using a pragma rather than an aspect, as the justification is generally associated to a statement or declaration.

2. for influencing the generation of proof obligations, typically using an aspect rather than a pragma, as the annotation is generally associated to an entity in that case. Some of these uses can be seen in SPARK Libraries for example. Some of these annotations introduce additional assumptions which are not verified by the GNATprove tool, and thus should be used with care.

When the annotation is associated to an entity, both the pragma and aspect form can be used and are equivalent, for example on a subprogram:

```ada
function Func (X : T) return T
  with Annotate => (GNATprove, <annotation name>);
```

or

```ada
function Func (X : T) return T;
pragma Annotate (GNATprove, <annotation name>, Func);
```

In the following, we use the aspect form whenever possible.

**F.1 Using Annotations to Justify Check Messages**

You can use annotations of the form

```ada
pragma Annotate (GNATprove, False_Positive,
  "message to be justified", "reason");
```

to justify an unproved check message that cannot be proved by other means. See the section Direct Justification with Pragma Annotate for more details about this use of pragma Annotate.

**F.2 Using Annotations to Specify Possibly Nonreturning Procedures**

You can use annotations of the form
to specify that a procedure might not return. See the section *Nonreturning Procedures* for more details about this use of annotations.

**F.3 Using Annotations to Request Proof of Termination**

By default, GNATprove does not prove termination of subprograms. You can instruct it to do so using annotations of the form:

```plaintext
procedure Proc
  with Annotate => (GNATprove, Terminating);
```

See the section *Subprogram Termination* about details of this use of annotations.

**F.4 Using Annotations to Request Overflow Checking on Modular Types**

The standard semantics of arithmetic on modular types is that operations wrap around, hence GNATprove issues no overflow checks on such operations. You can instruct it to issue such checks (hence detecting possible wrap-around) using annotations of the form:

```plaintext
type T is mod 2**32
  with Annotate => (GNATprove, No_Wrap_Around);
```

or on a derived type:

```plaintext
type T is new U
  with Annotate => (GNATprove, No_Wrap_Around);
```

This annotation is inherited by derived types. It must be specified on a type declaration (and cannot be specified on a subtype declaration). All three binary arithmetic operations + - * are checked for possible overflows. Division cannot lead to overflow. Unary negation is checked for possible non-nullity of its argument, which leads to overflow.

**F.5 Customize Quantification over Types with the Iterable Aspect**

In SPARK, it is possible to allow quantification over any container type using the *Iterable* aspect. This aspect provides the primitives of a container type that will be used to iterate over its content. For example, if we write:

```plaintext
type Container is private with
  Iterable => (First => First,
               Next  => Next,
               Has_Element => Has_Element);
```

where

```plaintext
function First (S : Set) return Cursor;
function Has_Element (S : Set; C : Cursor) return Boolean;
function Next (S : Set; C : Cursor) return Cursor;
```
then quantification over containers can be done using the type Cursor. For example, we could state:

\[(\text{for all } C \text{ in } S \Rightarrow P (\text{Element } (S, C)))\]

to say that \(S\) only contains elements for which a property \(P\) holds. For execution, this expression is translated as a loop using the provided First, Has_Element, and Next primitives. For proof, it is translated as a logic quantification over every element of type Cursor. To restrict the property to cursors that are actually valid in the container, the provided function Has_Element is used. For example, the property stated above becomes:

\[(\text{for all } C : \text{Cursor} \Rightarrow (\text{if Has_Element } (S, C) \text{ then } P (\text{Element } (S, C))))\]

Like for the standard Ada iteration mechanism, it is possible to allow quantification directly over the elements of the container by providing in addition an Element primitive to the Iterable aspect. For example, if we write:

```ada
type Container is private with
  Iterable => (First => First,
                Next => Next,
                Has_Element => Has_Element,
                Element => Element);

function Element (S : Set; C : Cursor) return Element_Type;
```

then quantification over containers can be done directly on its elements. For example, we could rewrite the above property into:

\[(\text{for all } E \text{ of } S \Rightarrow P (E))\]

For execution, quantification over elements of a container is translated as a loop over its cursors. In the same way, for proof, quantification over elements of a container is no more than syntactic sugar for quantification over its cursors. For example, the above property is translated using quantification over cursors:

\[(\text{for all } C : \text{Cursor} \Rightarrow (\text{if Has_Element } (S, C) \text{ then } P (\text{Element } (S, C))))\]

Depending on the application, this translation may be too low-level and introduce an unnecessary burden on the automatic provers. As an example, let us consider a package for functional sets:

```ada
package Sets with SPARK_Mode is

  type Cursor is private;
  type Set (<>) is private with
   Iterable => (First => First,
                 Next => Next,
                 Has_Element => Has_Element,
                 Element => Element);

  function Mem (S : Set; E : Element_Type) return Boolean with
    Post => Mem'Result = (for some F of S => F = E);

  function Intersection (S1, S2 : Set) return Set with
    Post => (for all E of Intersection'Result => Mem (S1, E) and Mem (S2, E))
      and (for all E of S1 => (if Mem (S2, E) then Mem (Intersection'Result, E)));

Sets contain elements of type Element_Type. The most basic operation on sets is membership test, here provided by the Mem subprogram. Every other operation, such as intersection here, is then specified in terms of members.
Iteration primitives First, Next, Has_Element, and Element, that take elements of a private type Cursor as an argument, are only provided for the sake of quantification.

Following the scheme described previously, the postcondition of Intersection is translated for proof as:

\[
\text{(for all } C : \text{Cursor} \Rightarrow \\
\text{ (if Has_Element (Intersection'Result, C) then) \\
\text{ Mem (S1, Element (Intersection'Result, C)) \\
\text{ and Mem (S2, Element (Intersection'Result, C))}) \\
\text{ and (for all } C1 : \text{Cursor} \Rightarrow \\
\text{ (if Has_Element (S1, C1) then \\
\text{ (if Mem (S2, Element (S1, C1)) then \\
\text{ Mem (Intersection'Result, Element (S1, C1)))))}}
\]

Using the postcondition of Mem, this can be refined further into:

\[
\text{(for all } C : \text{Cursor} \Rightarrow \\
\text{ (if Has_Element (Intersection'Result, C) then \\
\text{ (for some } C1 : \text{Cursor} \Rightarrow \\
\text{ Has_Element (S1, C1) and Element (Intersection'Result, C) = Element(S1, C1)) \\
\text{ and (for some } C2 : \text{Cursor} \Rightarrow \\
\text{ Has_Element (S2, C2) and Element (Intersection'Result, C) = Element(S2, C2))}) \\
\text{ and (for all } C1 : \text{Cursor} \Rightarrow \\
\text{ (if Has_Element (S1, C1) then \\
\text{ (if (for some } C2 : \text{Cursor} \Rightarrow \\
\text{ Has_Element (S2, C2) and Element (S1, C1) = Element (S2, C2)) \\
\text{ then (for some } C : \text{Cursor} \Rightarrow \\
\text{ Has_Element (Intersection'Result, C) \\
\text{ and Element (Intersection'Result, C) = Element (S1, C1))})}))})
\]

Though perfectly valid, this translation may produce complicated proofs, especially when verifying complex properties over sets. The GNATprove annotation Iterable_For_Proof can be used to change the way for ... of quantification is translated. More precisely, it allows to provide GNATprove with a Contains function, that will be used for quantification. For example, on our sets, we could write:

```plaintext
function Mem (S : Set; E : Element_Type) return Boolean;
pragma Annotate (GNATprove, Iterable_For_Proof, "Contains", Mem);
```

With this annotation, the postcondition of Intersection is translated in a simpler way, using logic quantification directly over elements:

\[
\text{(for all } E : \text{Element_Type} \Rightarrow \\
\text{ (if Mem (Intersection'Result, E) then Mem (S1, E) and Mem (S2, E)) \\
\text{ and (for all } E : \text{Element_Type} \Rightarrow \\
\text{ (if Mem (S1, E) then \\
\text{ (if Mem (S2, E) then Mem (Intersection'Result, E))))}}
\]

Note that care should be taken to provide an appropriate function contains, which returns true if and only if the element E is present in S. This assumption will not be verified by GNATprove.

The annotation Iterable_For_Proof can also be used in another case. Operations over complex data structures are sometimes specified using operations over a simpler model type. In this case, it may be more appropriate to translate for ... of quantification as quantification over the model’s cursors. As an example, let us consider a package of linked lists that is specified using a sequence that allows accessing the element stored at each position:
package Lists with SPARK_Mode is

type Sequence is private with
  Ghost,
  Iterable => (...,
    Element => Get);
function Length (M : Sequence) return Natural with Ghost;
function Get (M : Sequence; P : Positive) return Element_Type with
  Ghost,
  Pre => P <= Length (M);

type Cursor is private;
type List is private with
  Iterable => (...,
    Element => Element);
function Position (L : List; C : Cursor) return Positive with Ghost;
function Model (L : List) return Sequence with
  Ghost,
  Post => (for all I in 1 .. Length (Model'Result) =>
    (for some C in L => Position (L, C) = I));
function Element (L : List; C : Cursor) return Element_Type with
  Pre => Has_Element (L, C),
  Post => Element'Result = Get (Model (L), Position (L, C));
function Has_Element (L : List; C : Cursor) return Boolean with
  Post => Has_Element'Result = (Position (L, C) in 1 .. Length (Model (L)));
procedure Append (L : in out List; E : Element_Type) with
  Post => length (Model (L)) = Length (Model (L))'Old + 1
  and Get (Model (L), Length (Model (L))'Old) = E
  and (for all I in 1 .. Length (Model (L))'Old =>
    Get (Model (L), I) = Get (Model (L'Old), I));
function Init (N : Natural; E : Element_Type) return List with
  Post => length (Model (Init'Result)) = N
  and (for all F of Init'Result => F = E);

Elements of lists can only be accessed through cursors. To specify easily the effects of position-based operations such as Append, we introduce a ghost type Sequence, that is used to represent logically the content of the linked list in specifications. The sequence associated to a list can be constructed using the Model function. Following the usual translation scheme for quantified expressions, the last line of the postcondition of Init is translated for proof as:

(for all C : Cursor =>
  (if Has_Element (Init'Result, C) then Element (Init'Result, C) = E));

Using the definition of Element and Has_Element, it can then be refined further into:

(for all C : Cursor =>
  (if Position (Init'Result, C) in 1 .. Length (Model (Init'Result))
    then Get (Model (Init'Result), Position (Init'Result, C)) = E));

To be able to link this property with other properties specified directly on models, like the postcondition of Append, it needs to be lifted to iterate over positions instead of cursors. This can be done using the postcondition of Model that states that there is a valid cursor in L for each position of its model. This lifting requires a lot of quantifier reasoning from the prover, thus making proofs more difficult.
The GNATprove \texttt{Iterable\_For\_Proof} annotation can be used to provide GNATprove with a \textit{Model} function, that will be to translate quantification on complex containers toward quantification on their model. For example, on our lists, we could write:

```ada
function Model (L : List) return Sequence;
pragma Annotate (GNATprove, Iterable\_For\_Proof, "Model", Entity => Model);
```

With this annotation, the postcondition of \texttt{Init} is translated directly as a quantification on the elements of the result’s model:

```ada
(for all I : Positive =>
  if I in 1 .. Length (Model (Init'Result)) then
    Get (Model (Init'Result), I) = E));
```

Like with the previous annotation, care should be taken to define the model function such that it always return a model containing exactly the same elements as \texttt{L}.

### F.6 Inlining Functions for Proof

Contracts for functions are generally translated by GNATprove as axioms on otherwise undefined functions. As an example, consider the following function:

```ada
function Increment (X : Integer) return Integer with
  Post => Increment'Result >= X;
```

It will be translated by GNATprove as follows:

```ada
function Increment (X : Integer) return Integer;
axiom : (for all X : Integer. Increment (X) >= X);
```

For internal reasons due to ordering issues, expression functions are also defined using axioms. For example:

```ada
function Is\_Positive (X : Integer) return Boolean is (X > 0);
```

will be translated exactly as if its definition was given through a postcondition, namely:

```ada
function Is\_Positive (X : Integer) return Boolean;
axiom : (for all X : Integer. Is\_Positive (X) = (X > 0));
```

This encoding may sometimes cause difficulties to the underlying solvers, especially for quantifier instantiation heuristics. This can cause strange behaviors, where an assertion is proven when some calls to expression functions are manually inlined but not without this inlining.

If such a case occurs, it is sometimes possible to instruct the tool to inline the definition of expression functions using \texttt{pragma Annotate Inline\_For\_Proof}. When such a pragma is provided for an expression function, a direct definition will be used for the function instead of an axiom:

```ada
function Is\_Positive (X : Integer) return Boolean is (X > 0);
pragma Annotate (GNATprove, Inline\_For\_Proof, Is\_Positive);
```

The same pragma will also allow to inline a regular function, if its postcondition is simply an equality between its result and an expression:
In this case, GNATprove will introduce a check when verifying the body of `Is_Positive` to make sure that the inline annotation is correct, namely, that `Is_Positive (X)` and `X > 0` always yield the same result. This check may not be redundant with the verification of the postcondition of `Is_Positive` if the `=` symbol on booleans has been overridden.

Note that, since the translation through axioms is necessary for ordering issues, this annotation can sometimes lead to a crash in GNATprove. It is the case for example when the definition of the function uses quantification over a container using the `Iterable` aspect.

### F.7 Supplying a Pledge for a Borrower

Local borrowers are objects of an anonymous access-to-variable type. At their declaration, the ownership of (a part of) an existing data-structure is temporarily transferred to the new object. The borrowed data-structure will regain ownership afterward.

During the lifetime of the borrower, the borrowed object can be modified indirectly through the borrower. It is forbidden to modify or even read the borrowed object during the borrow. It can be problematic in some cases, for example if a borrower is modified inside a loop, as GNATprove will need information supplied in a loop invariant to know how the borrowed object and the borrower are related in the loop and after it.

In assertions, we are still allowed to express properties over a borrowed object using a pledge. The notion of pledges was introduced by researchers from ETH Zurich to verify Rust programs (see [https://2019.splashcon.org/details/splash-2019-oopsla/31/Leveraging-Rust-Types-for-Modular-Specification-and-Verification](https://2019.splashcon.org/details/splash-2019-oopsla/31/Leveraging-Rust-Types-for-Modular-Specification-and-Verification)). Conceptually, a pledge is a property involving a borrower and/or the object it borrows which is known to always hold during the scope of the borrow, no matter the modifications that may be done to either the borrower or the borrowed object. As pledges are not yet supported at a language level in SPARK, it is possible to mark (a part of) an assertion as a pledge by using an expression function which is annotated with a `Pledge Annotate` pragma:

```plaintext
function Pledge (Borrower : access constant T; Prop : Boolean) return Boolean is
  (Prop)
with Ghost,
  Annotate => (GNATProve, Pledge);
```

Note that the name of the function could be something other than `Pledge`, but the annotation should use the string `Pledge`. GNATprove will check that a function associated with the `Pledge` annotation is a ghost expression function which takes a borrower and a property and simply returns the property.

When GNATprove encounters a call to such a function, it knows that the property given as a second parameter to the call must be handled as a pledge of the local borrower given as a first parameter. It will not interpret it as a property which should hold over the current values of the borrower and the borrowed object, but as a sort of invariant, which should be known to always hold during the scope of `Borrower`. Access to a borrowed variable inside a pledge is allowed by the SPARK reference manual, which gives a provision for reading borrowed variables at any time and in any context during the borrow. However, GNATprove will reject such reads if they do not occur as part of a pledge.

As an example, let us consider a recursive type of doubly-linked lists:
Using this type, let us construct a list $X$ which stored the numbers from 1 to 5:

```plaintext
X := new List'(1, null);
X.Next := new List'(2, null);
X.Next.Next := new List'(3, null);
X.Next.Next.Next := new List'(4, null);
X.Next.Next.Next.Next := new List'(5, null);
```

We can borrow the structure designated by $X$ in a local borrower $Y$:

```plaintext
declare
   Y : access List := X;
begin
   ...
   end;
```

While in the scope of $Y$, the ownership of the list designated by $X$ is transferred to $Y$, so that it is not allowed to access it from $X$ anymore. After the end of the declare block, ownership is restored to $X$, which can again be accessed or modified directly.

Let us now define a pledge function that can be used to relate the values designated by $X$ and $Y$ during the time of the borrow:

```plaintext
function Pledge (Borrower : access constant List; Prop : Boolean) return Boolean is
  (Prop)
with Ghost,
   Annotate => (GNATProve, Pledge);
```

We can use this function to give properties that are known to hold during the scope of $Y$. Since $Y$ and $X$ designate the same value, we can state in a pledge that the Val and Next components of $X$ and $Y$ always match:

```plaintext
pragma Assert (Pledge (Y, X.Val = Y.Val));
pragma Assert (Pledge (Y, X.Next = Y.Next));
```

However, even though at the beginning of the declare block, the first value of $X$ is 1, it is not correct to assert that it will remain so inside a pledge:

```plaintext
pragma Assert (Y.Val = 1); -- proved
pragma Assert (Pledge (Y, X.Val = 1)); -- incorrect
```

Indeed, $Y$ could be modified later so that $X$.Val is not 1 anymore:

```plaintext
declare
   Y : access List := X;
begin
   Y.Val := 2;
   end;
pragma Assert (X.Val = 2);
```

Note that the pledge above is invalid even if $Y$.Val is not modified in the following statements. A pledge is a contract about what is known to necessarily hold in the scope of $Y$, not what will happen in practice. The analysis performed by GNATprove remains a forward analysis, which should not be impacted by statements occurring after the current one.

Let us now consider a case where $X$ is not borrowed completely. In the declaration of $Y$, we can decide to borrow only the last three elements of the list:
Here, like in the previous example, we can state in a pledge that `X.Next.Next.Val` is `Y.Val`. Additionally, since `Y.Next` has been borrowed, we know that `Y.Next` will remain a valid path throughout the borrow. This is why we can state in a pledge that `X.Next` will never be null. Like in the previous example, we cannot assume anything about the part of `X` designated by `Y`, so we won’t be able to prove that `X.Next.Next.Val` will remain 3.

This is also true for parts of `X` which have not been borrowed by `Y`. During the scope of `Y`, we are allowed to modify `X.Val` for example, so we cannot assert in a pledge that it will remain 1.

Inside the scope of `Y`, it is possible to modify the variable `Y` itself, as opposed to modifying the structure it designates, so that it gives access to a subcomponent of the borrowed structure. It is called a reborrow. In case of reborrow, the pledge of the borrower is modified so that it corresponds to the relation between the object borrowed initially and the new borrower. For example, let’s use `Y` to borrow `X` entirely and then modify it to only designate `X.Next.Next`:

```plaintext
declare
    Y : access List := X;
begin
    Y := Y.Next.Next;
    pragma Assert (Pledge (Y, X.Next.Next /= null));
    pragma Assert (Pledge (Y, X.Val = 1));
    pragma Assert (Pledge (Y, X.Next.Val = 2));
    pragma Assert (Pledge (Y, X.Next.Next.Val = 3)); -- incorrect
    pragma Assert (Pledge (Y, X.Next.Next.Next /= null)); -- incorrect
end;
```

After the assignment, the part of `X` still accessible from the borrower is reduced, but since `X` was borrowed entirely to begin with, the ownership policy of SPARK still forbids direct access to any components of `X` while in the scope of `Y`. As a result, we have a bit more information about the final value of `X` than in the previous case. As before, we know that `X` will hold at least three elements, that is `X.Next.Next /= null`. Additionally, the first and second components of `X` are no longer accessible from `Y`, and since they cannot be accessed directly through `X`, we know that they will keep their current values. This is why we can now assert in a pledge that `X.Val` is 1 and `X.Next.Val` is 2.

However, we still cannot know anything about the part of `X` still accessible from `Y` as these properties could be modified later in the borrow:

```plaintext
Y.Val := 42;
Y.Next := null;
```

Pledge functions are also useful in postconditions of borrowing traversal functions. A borrowing traversal function is a function which returns a local borrower of its first parameter. As GNATprove works modularly on a per subprogram basis, it is necessary to specify the pledge of the result of such a function in its postcondition, or proof would not be able to recompute the value of the borrowed parameter after the returned borrower goes out of scope.

As an example, we can define a `Tail` function which returns the `Next` component of a list if there is one, and `null`
otherwise:

```plaintext
function Tail (L : access List) return access List is
begin
    if L = null then
        return null;
    else
        return L.Next;
    end if;
end Tail;
```

In its postcondition, we want to consider the two cases, and, in each case, specify both the value returned by the function and how the parameter L is related to the returned borrower:

```plaintext
function Tail (L : access List) return access List with
    Contract_Cases =>
        (L = null =>
            Tail'Result = null and Pledge (Tail'Result, L = null),
        others => Tail'Result = L.Next
            and Pledge (Tail'Result, L.Val = L.Val'Old)
            and Pledge (Tail'Result, L.Next = Tail'Result));
```

If L is null then Tail returns null and L will stay null for the duration of the borrow. Otherwise, Tail returns L.Next, the first element of L will stay as it was at the time of call, and the rest of L stays equal to the object returned by Tail.

Thanks to this postcondition, we can verify a program which borrows a part of L using the Tail function and modifies L through this borrower:

```plaintext
declare
    Y : access List := Tail (Tail (X));
begin
    Y.Val := 42;
end;

pragma Assert (X.Val = 1);
pragma Assert (X.Next.Val = 2);
pragma Assert (X.Next.Next.Val = 42);
pragma Assert (X.Next.Next.Next.Val = 4);
```
G.1 Tool Limitations

1. The Global contracts generated automatically by GNATprove for subprograms without an explicit one do not take into account indirect calls (through access-to-subprogram and dynamic binding) and indirect reads/writes to global variables (through access variables).

2. Checks related to tasking, subprogram termination, or recursive calls do not take into account dispatching calls.

3. A subset of all Ada conversions between array types is supported:
   - element types must be exactly the same
   - matching index types must either be both modular with a base type of the same size, or both non modular

4. A subset of all Ada fixed-point types and fixed-point operations is supported:
   - multiplication and division between different fixed-point types and floating-point types are rejected
   - multiplication and division between different fixed-point types are rejected if their smalls are not compatible as defined in Ada RM G.2.3(21).
   - conversions from fixed-point types to floating-point types are rejected
   These restrictions ensure that the result of fixed-point operations always belongs to the perfect result set as defined in Ada RM G.2.3.

5. Multidimensional array types are supported up to 4 dimensions.

6. Loop_Invariant and Loop_Variant pragmas must appear before any non-scalar object declaration.

7. Inheriting the same subprogram from multiple interfaces is not supported.

8. Formal object parameters of generics of an unconstrained record type with per-object constrained fields are badly supported by the tool and may result in crashes in some cases.

9. Quantified expressions with an iterator over a multi dimensional array (for example for all Elem of Arr where Arr is a multi dimensional array) are not supported.

10. Constrained subtypes of class-wide types and ‘Class attributes of constrained record types are not supported.

11. Abstract states cannot be marked Part_Of a single concurrent object (see SPARK RM 9(3)). An error is raised instead in such cases.

12. Classwide Global and Depends contracts as defined in SPARK RM 6.1.6 are not supported.

13. Task attributes Identity and Storage_Size are not supported.

14. Type_Invariant and Invariant aspects are not supported:
   - on private types declared in nested packages or child packages
• on protected types
• on tagged types
• on components of tagged types if the tagged type is visible from inside the scope of the invariant bearing type.

15. Calls to protected subprograms and protected entries whose prefix denotes a formal subprogram parameter are not supported. Similarly, suspension on suspension objects given as formal subprogram parameters is not supported.

G.2 Legality Rules

1. SPARK Reference Manual rule 4.3(1), concerning use of the box symbol “<>” in aggregates, is not currently checked.

2. The rule concerned with asserting that all child packages which have state denoted as being Part_Of a more visible state abstraction are given as constituents in the refinement of the more visible state is not checked (SPARK Reference Manual rule 7.2.6(6)).

3. The case of a state abstraction whose Part_Of aspect denotes a task or protected unit is not currently supported.

4. The case of a Refined_Post specification for a (protected) entry is not currently supported.

5. The use of Ada.Synchronous_Barriers.Synchronous_Barrier type is not currently allowed in SPARK.

6. Entry families are not currently allowed in SPARK.

G.3 Flow Analysis Limitations

1. Flow dependencies caused by record assignments is not captured with perfect accuracy. This means that the value of one field might incorrectly be considered to participate in the derivation of another field that it does not really participate in.

2. Initialization of multi-dimensional arrays with nested FOR loops can be only detected if the array bounds are given by static expressions.

G.4 Proof Limitations

1. Postconditions of recursive functions called in contracts and assertion pragmas are not available, possibly leading to unproved checks. The current workaround is to use a non-recursive wrapper around those functions. Using the switch --info reveals where the information about postcondition may be lost.

2. Attribute ‘Valid is currently assumed to always return True.

3. Values read from an external source are assumed to be valid values. Currently there is no model of invalidity or undefinedness. The onus is on the user to ensure that all values read from an external source are valid. The use of an invalid value invalidates any proofs associated with the value.

4. The following attributes are not yet supported in proof: Adjacent, Aft, Bit_Order, Body_Version, Copy_Sign, Definite, Denorm, First_Valid, Fore, Last_Valid, Machine, all Machine_* attributes, Model, all Model_* attributes, Partition_Id, Remainder, Round, Safe_First, Safe_Last, Scale, Scaling, Small, Unbiased_Rounding, Version, Wide_Image, Wide_Value, Wide_Width, Wide_Wide_Image, Wide_Wide_Value, Wide_Wide_Width, Width.
The attributes First_Bit, Last_Bit and Position are supported but if there is no record representation clause then we assume that their value is nonnegative.

5. The ‘Update attribute on multidimensional unconstrained arrays is not yet fully supported in proof. Checks might be missing so currently an error is emitted for any use of the ‘Update attribute on multidimensional unconstrained arrays.

6. GNATprove does not follow the value of tags for tagged objects. As a consequence, tag checks are currently unprovable in most cases.

7. Constants declared in loops before the loop invariant are handled as variables by the tool. This means in particular that any information about their values needed after the loop invariant must be stated explicitly in the loop invariant.


9. Preconditions on arithmetic and conversion operators (including Time_Of) in Ada.Calendar package are not yet implemented.
H.1 Compiling with a non-SPARK Aware Compiler

To execute a SPARK program, it is expected that users will compile the program (as an Ada program) using an Ada compiler. The SPARK language definition defines a number of implementation-defined (with respect to the Ada language definition) aspects, attributes, pragmas, and conventions. Ideally a SPARK program will be compiled using an Ada compiler that supports all of these constructs. Portability problems may arise if this is not the case.

This section is a discussion of the strategies available for coping with this situation.

Probably the most important rule is that pragmas should be used instead of aspect_specification syntax wherever this option is available. For example, use pragma Abstract_State rather than specifying the Abstract_State aspect of a package using aspect_specification syntax. Ada specifies that unrecognized pragmas shall be ignored, as opposed to being rejected. This is not the case for (syntactic) aspect specifications (this terminology is a bit confusing because a pragma can be used to specify an aspect; such a pragma is semantically, but not syntactically, an aspect specification). Furthermore, aspect specification syntax was introduced in Ada 2012 and will be rejected if the program is compiled as, for example, an Ada 95 program.

Many SPARK-defined constructs have no dynamic semantics (e.g., the Global, Depends, and Abstract_State aspects), so the run-time behavior of a program is unaffected if they are ignored by a compiler. Thus, there is no problem if these constructs are expressed as pragmas which are then ignored by the Ada compiler.

Of those constructs which do have dynamic semantics, most are run-time assertions. These include Loop_Variant, Loop_Invariant, Assert_And_Cut, Contract_Cases, Initial_Condition, and Refined_Postcondition. Because SPARK requires that the success of these assertions must be statically proven (and that the evaluation of the asserted condition can have no side effects), the run-time behavior of a program is unaffected if they are ignored by a compiler.

The situation with pragma Assume is slightly different because the success of the given condition is not statically proven. If ignoring an Assume pragma at run time is deemed to be unacceptable, then it can be replaced with an Assert pragma (at the cost of introducing a source code difference between the SPARK program that is analyzed statically and the Ada program that is executed). An ignored Assume pragma is the only case where the use of a SPARK-specific construct can lead to a portability problem which is not detected at compile time. In all other cases, either the Ada compiler will reject (as opposed to ignore) an unrecognized construct or the construct can safely be ignored.

An Ada compiler which does not support convention Ghost will reject any use of this convention. Two safe transformations are available for dealing with this situation - either replace uses of convention Ghost with convention Ada or delete the entities declared with a convention of Ghost. Just as was mentioned above in the case of modifying an Assume pragma, either choice introduces an analyzed/executed source code difference.

There are two SPARK attributes which cannot be used if they are not supported by the Ada compiler in question: the Update and Loop_Entry attributes.

SPARK includes a rule that a package which declares a state abstraction requires a body. In the case of a library unit package (or generic package) which requires a body only because of this rule, an Ada compiler that knows nothing
about state abstractions would reject the body of the package because of the rule (introduced in Ada 95) that a library unit package (or generic package) body is never optional; if it is not required then it is forbidden. In the unlikely event that this scenario arises in practice, the solution is to force the library unit package to require a body for some other reason, typically by adding an Elaborate_Body pragma.

If a SPARK program is to be compiled and executed as an Ada 95 program (or any other pre-2012 version of Ada), then of course any construct introduced in a later version of Ada must be avoided (unless it is expressed as a safely-ignored pragma). This seems worth mentioning because Ada 2012 constructs such as quantified expressions and conditional expressions are often heavily used in SPARK programs.

**H.2 Implementation-specific Decisions**

To make analysis as precise as possible and avoid producing too many false alarms, GNATprove makes some assumptions about the behavior of constructs which are listed in the reference manual of Ada as implementation specific. Note that GNATprove always adopts the same choices as the GNAT compiler, so these assumptions should be adequate when compiling with GNAT. However, when another compiler is used, it may be better to avoid these implementation specific constructs (see Benefits of Using SPARK for Portability for more details on how this can be achieved).

**H.2.1 Parenthesized Arithmetic Operations**

In Ada, non-parenthesized arithmetic operations could be re-ordered by the compiler, which may result in a failing computation (due to overflow checking) becoming a successful one, and vice-versa. By default, GNATprove evaluates all expressions left-to-right, like GNAT. When the switch --pedantic is used, a warning is emitted for every operation that could be re-ordered:

- any operand of a binary adding operation (+,-) that is itself a binary adding operation;
- any operand of a binary multiplying operation (*,/,mod,rem) that is itself a binary multiplying operation.

**H.2.2 Base Type of User-Defined Integer Types**

GNATprove follows GNAT in choosing as base type the smallest multiple-words-size integer type that contains the type bounds. For example, a user-defined type ranging from 1 to 100 will be given a base type ranging from -128 to 127 by both GNAT and GNATprove. The choice of base types influences in which cases intermediate overflows may be raised during computation. The choice made in GNATprove is the strictest one among existing compilers, as far as we know, which ensures that GNATprove’s analysis detects a superset of the overflows that may occur at run time.

**H.2.3 Size of ‘Image and ‘Img attributes**

To avoid spurious range checks on string operations involving occurrences of the 'Img, 'Image, 'Wide_Image, and 'Wide_Wide_Image attributes, GNATprove makes an assumption about the maximal length of the returned string. If the attribute applies to an integer type, the bounds are the maximal size of the result of the attribute as specified in the language depending of the type’s base type. Otherwise, GNATprove assumes that the length of such a string cannot exceed 255 (the maximal number of characters in a line) times 8 (the maximal size of a Wide_Wide_Character).
SPARK assumes that floating point operations are carried out in single precision (binary32) or double precision (binary64) as defined in the IEEE-754 standard for floating point arithmetic. You should make sure that this is the case on your platform. For example, on x86 platforms, by default some intermediate computations may be carried out in extended precision, leading to unexpected results. With GNAT, you can specify the use of SSE arithmetic by using the compilation switches “-msse2 -mfpmath=sse” which cause all arithmetic to be done using the SSE instruction set which only provides 32-bit and 64-bit IEEE types, and does not provide extended precision. SSE arithmetic is also more efficient. Note that the ABI allows free mixing of units using the two types of floating-point, so it is not necessary to force all units in a program to use SSE arithmetic.

SPARK considers the floating point values which represent positive, negative infinity or NaN as invalid. Proof obligations are generated that such values cannot occur.

SPARK considers rounding on floating point arithmetic operations to follow Round-Nearest-Even (RNE) mode, where a real result is rounded to the nearest floating point value, and ties are resolved to the floating-point with a zero in the last place. This mode of rounding should be forced if needed on the hardware to be able to rely on the results of GNATprove regarding floating point arithmetic.
SPARK ARCHITECTURE, QUALITY ASSURANCE AND MATURITY

J.1 Development Process and Quality Assurance

The SPARK development process and quality assurance are following the Adacore Quality Procedures in place for all development at AdaCore. This includes:

- The use of a report tracking system;
- Mechanisms for detecting and fixing defects;
- The usage of repositories and configuration management, the use of continuous integration technology, the stringent requirements on check-ins of source changes;
- The process for implementing new functionality;
- The process for maintaining user documentation;
- Ensuring quality of sources and technical documentation;
- Preparation of releases

As an extension to Chapter 2, section “AdaCore internal testsuite”, SPARK contains its own testsuites:

- The SPARK main testsuite: This testsuite contains 1700 tests. These tests are specifically targeted at the SPARK software and cover typical use cases, often represented by code sent to us by customers, as well as specific features of the SPARK software.
- The ACATS testsuite in SPARK mode: A selection of the ACATS testsuite mentioned in the AdaCore Quality Procedures for the compiler is also used to test the SPARK tools.

These tests are run on various occasions (see also Chapter 2 of the Adacore Quality Procedures): * During nightly testing, once with assertions enabled, once without (the actual SPARK product); * After every check-in, during continuous integration; * To test a patch before check-in using the Mailserver technology.

J.2 Structure of the SPARK Software

At a high level, SPARK reads source files in the Ada programming language, with some annotations specific to SPARK, processes them, and in the end issues a report about errors found and proved or unproved properties. Looking more closely at how this is achieved, one can see this high-level structure of SPARK:
The development of the GNAT front-end and GNAT2Why components entirely follows the procedures outlined in AdaCore Quality Procedures and the previous section. The other components, however, are mostly developed by third parties. Their development process and the relationship to AdaCore and Altran will be outlined below.

For the nightly testing of SPARK, the GNAT and GNAT2Why components are updated every night according to the changes made during the day by AdaCore and Altran developers. The other tools, however, contain also check-ins by other persons. We update these tools in a controlled way, and after careful testing of the consequences. In other words, a check-in made e.g. to Z3 at some specific date, will not be part of the SPARK package of the same day, instead it will be integrated into SPARK after some time and after thorough testing in the SPARK environment.

J.2.1 GNAT front-end

SPARK shares its front-end (parsing and semantic analysis) with the GNAT compiler technology, which is very mature and has been used in countless projects for the last 20 years. The GNAT front-end is developed by AdaCore and follows the AdaCore quality procedures.

J.2.2 GNAT2Why

This part of SPARK serves two purposes:

- Implement Flow Analysis, the part of the SPARK analysis which detects uninitialized variables, and computes and checks the use of global variables and parameters.
- Translate the Ada source code to the Why language, for further processing by the Why3 tools. GNAT2Why is developed by AdaCore and Altran and follows the AdaCore quality procedures.

J.2.3 Why3

This part of SPARK takes the information in the Why language produced by GNAT2Why, translates it further into a format suitable for SMT solvers such as Z3 and CVC4, and runs these tools. The results are reported back to gnat2why.

History: Started around the year 2000 by Jean-Christophe Filliâtre as “Why” (see Jean-Christophe Filliâtre. Why: a multi-language multi-prover verification tool. Research Report 1366, LRI, Université Paris Sud, March 2003), it has undergone a number of redevelopments until its current version Why3 (since 2010).

Track record: Apart from SPARK, it is used by Frama-C, Atelier B, and other program verification tools.

Relationship with AdaCore/Altran: The Inria team around Why3 has strong ties with AdaCore and Altran. A number of research projects have been and are being carried out in collaboration with this team. This includes the Hi-Lite...
project, which led to the current version of SPARK based on Why3, and the still ongoing project SOPRANO and joint laboratory ProofInUse. In addition, while Why3 is mainly developed at Inria, AdaCore and Altran have made important contributions to the technology, such as the so-called fast-WP, a more efficient implementation of the main algorithm of Why3, and the why3server, a more scalable method of running external tools such as SMT solvers.

- Main developers: Inria research institute
- Version Management: Git
- License: Open Source, LGPL 2.1
- Public mailing-list: why3-club@lists.gforge.inria.fr
- Bug tracking: https://gforge.inria.fr/tracker/?group_id=2990

### J.2.4 Alt-Ergo

History: Started around the year 2005 at Inria by Sylvain Conchon and Evelyne Contejean as “Ergo” (see CC(X): Efficiently combining equality and solvable theories without canonizers. Sylvain Conchon, Évelyne Contejean, and Johannes Kanig. SMT Workshop, 2007). Starting from 2013, developed and distributed mainly by OCamlPro. Since then, OCamlPro issues every year a private release and a public release (lagging one year behind the private release). SPARK uses the public release of Alt-Ergo.

Track record: Apart from SPARK, it is used by Frama-C and Atelier B. In particular, used by Airbus for the qualification DO-178C of an aircraft [10].

Relationship with AdaCore/Altran: AdaCore and OCamlPro collaborate in the SOPRANO. AdaCore has contributed some minor changes to Alt-Ergo, including a deterministic resource limiting switch.

- Main developers: OCamlPro
- Main website: https://alt-ergo.ocamlpro.com/
- Version Management: Git
- License: CeCill-C (GPL compatible)
- Public mailing-list: alt-ergo-users@lists.gforge.inria.fr
- Bug tracking: https://github.com/OCamlPro/alt-ergo/issues

### J.2.5 Z3


Track record: Apart from SPARK, used by Dafny and PEX projects inside Microsoft. Has won the SMT competition several times in several categories.

Relationship with AdaCore/Altran: AdaCore and Altran have provided bug reports, feature requests and small fixes to the Z3 team, in particular related to a deterministic resource limiting switch.

- Main developers: Microsoft
- Main website: https://github.com/Z3Prover/z3
- Version Management: Git
J.2.6 CVC4

History: CVC4 is the fourth in the Cooperating Validity Checker family of tools, which dates back to 1996, but does not directly incorporate code from any previous version. CVC4 development started in 2012.

Track record: Very good results in various SMT competitions. Used in TNO tool.

Relationship with AdaCore/Altran: AdaCore and Altran have provided bug reports, feature requests and small fixes to the CVC4 team, in particular related to a deterministic resource limiting switch.

- Main developers: New York University
- Main website: http://cvc4.cs.nyu.edu/web/
- Version Management: Git
- License: Modified BSD License
- Mailing List: cvc-users@cs.nyu.edu
- Bug tracking: http://cvc4.cs.nyu.edu/bugs/
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